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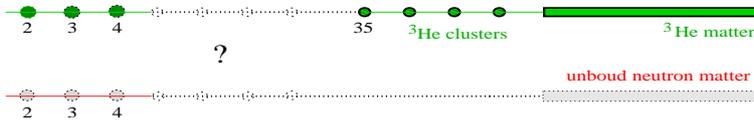
## Small clusters of fermions

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Several theoretical studies [1] indicate that there is no any reasonable chance for  $3n$  and  $4n$  to be bound. GANIL experiment [2] suggesting tetra-neutron has not been confirmed but these no-result had however the merit of pushing theoreticians at work to clarify the possible existence of small  $n$ -clusters. If the situation seems clear for  $A=3$  and  $4$ , it is less well established for a larger number of neutrons. The search of multi-neutron resonances raises also some interest and a recent experiment scanning the  $4n$  continuum in the  $d(^8\text{He}, ^6\text{Li})4n$  reaction reports a 2-3 MeV width structure [3].

In this issue it is enlightening to make a parallel with a similar, better-known, fermionic system: the  $^3\text{He}$  atomic clusters. Since small  $^3\text{He}$  droplets can exist [4], should we expect some stability islands (see figure below) in the continuum neutron states going from  $N=2$  to  $N=\infty$ . If yes, where? If not, why?



The two-body interactions of these systems look at first glance quite similar. We have compared in Fig. 1 the  $n$ - $n$  AV18 [5] and the  $^3\text{He}$ - $^3\text{He}$  Aziz [6] S-wave potentials. They have been rescaled by the corresponding masses  $\frac{M}{\hbar^2}$  and the resulting length units, as well as the inter-particle distance  $d$  are  $fm$  and  $\text{\AA}$  respectively. Corresponding low energy parameters are given in Table 1. In the  $n$ - $n$  case we have also considered Reid93 [7] and MT13 [8] potentials, the latter being adjusted to reproduce the experimental scattering length. None of these system supports a bound dimer ( $a < 0$ ) but  $^3\text{He}$  seems less favorable

Table 1

Low energy  $n$ - $n$  and  $^3\text{He}$ - $^3\text{He}$  parameters.

	n-n(fm)				He-He( $\text{\AA}$ )
	Av18	Reid	MT13	Exp.	Aziz 91
a	-18.49	-17.54	-18.59	$-18.59 \pm 0.4$	-7.24
$r_0$		2.85	2.94	$2.75 \pm 0.1$	13.5
$\eta_c$	1.08	1.09	1.10		1.30

to make clusters. This can be seen by calculating the critical values of the scaling factor  $\eta_c$  introduced in the potential  $V^{(\eta)}(r) = \eta V_{nn}(r)$ , which bounds a dimer. For  $n$ - $n$ , this value is around  $\eta_c = 1.08$  whereas for He-He is sensibly greater  $\eta_c = 1.30$  (see Table 1).

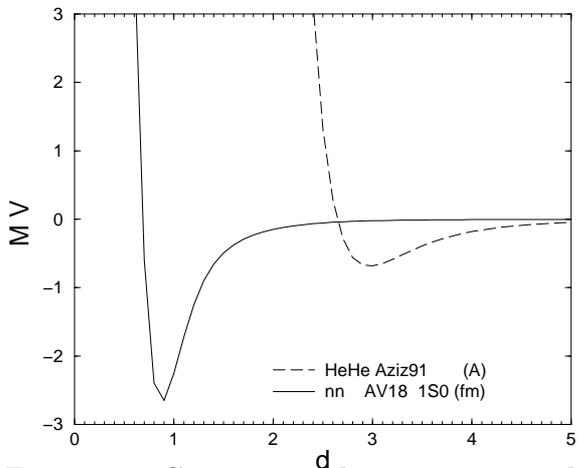


Figure 1. Comparison between  $n$ - $n$  and  ${}^3\text{He}$ - ${}^3\text{He}$  potentials.

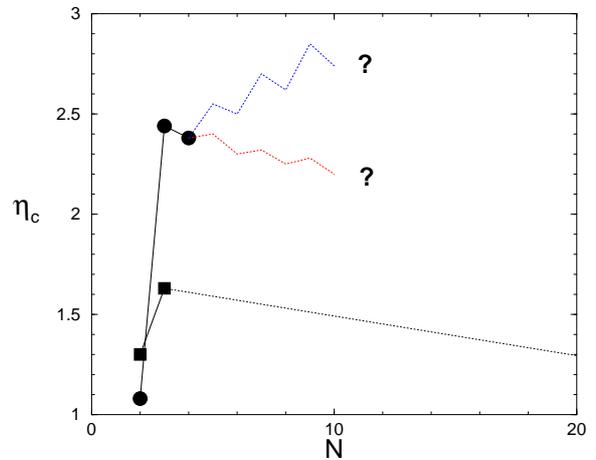


Figure 2. Critical value of the scaling factor for  $n$  (circles) and  ${}^3\text{He}$  (squares)

When examining larger systems we first consider the bosonic case. Despite the absence of dimers, "bosonic" neutron trimers and tetramers do exist with binding energies  $B_{n_3} \approx 1$  MeV and  $B_{n_4} \approx 10$  MeV. This is however not the case for atomic  ${}^3\text{He}$ , suggesting once more that neutron clusters should be favored with respect to atomic  ${}^3\text{He}$ . They all disappear when the Pauli principle is imposed, but can reappear – as in  ${}^3\text{He}$  – if the number of interacting particles is increased. The existence of small clusters results thus from a compromise between an attractive pairwise interaction and the effective Pauli repulsion.

In order to study such a balance, we have investigated in several directions [9]: (i) scaling factor in  $V_{nn}$ , (ii) three-neutron interactions (TnI), (iii) influence of  $n$ - $n$  P- waves (iv) confining the system in an harmonic oscillator (HO) trap and (iv) "dimer"-"dimer" scattering. It is always possible to bind 3- and 4- $n$  states by modifying the usual  $n$ - $n$  and/or TnI models but the violation has to be very strong, producing serious anomalies. Thus, in case (i) one needs a large scaling factor  $\eta_c \sim 3$ . Using ad-hoc TnI, one gets a very compact object in which NN force becomes even repulsive. Keeping the usual S-wave  $n$ - $n$  potential, the enhancement of  $n$ - $n$  P-waves required to bound a 3- or 4- $n$  system is such that they become themselves resonant!

We have confined  $N=2,3,4$   $n$  in an HO trap with fixed frequency  $\omega$  and size parameter  $b = \sqrt{\frac{\hbar}{m\omega}}$ . HO is the only external field in which "internal" and "center of mass" energies can be properly separated. In absence of  $n$ - $n$  forces the "internal" energies are known analytically but can be obtained as well by solving the  $N$ -body "internal" problem, with pairwise HO potential of frequency  $\left(\frac{\omega}{\sqrt{N}}\right)$ . The effect of  $n$ - $n$  interaction has been evaluated by solving the internal problem with

$$V_{ij} = \frac{1}{2} m \left( \frac{\omega}{\sqrt{N}} \right)^2 r_{ij}^2 + V_{nn}(r_{ij})$$

and calculating the difference between the pure HO energy and the  $HO + V_{nn}$  one:  $B_N = E_{HO}^{(N)} - E_{HO+nn}^{(N)}$ .

Results concerning the ground state are given in Table 2 for several values of  $b$ . Some comments are in order: (i) there is a clear indication of pairing effect when going from

Table 2

Binding energies  $B_N$  of  $N$  neutrons in an HO trap with size parameter  $b$ .

$N$	$J^\pi$	$b=2$				$b=3$				$b=4$			
		$E_{HO}^{(N)}$	$B_N$	$\frac{B_N}{N}$	$\frac{B_N}{E_{HO}}$	$E_{HO}^{(N)}$	$B_N$	$\frac{B_N}{N}$	$\frac{B_N}{E_{HO}}$	$E_{HO}^{(N)}$	$B_N$	$\frac{B_N}{N}$	$\frac{B_N}{E_{HO}}$
2	$0^+$	15.55	6.34	3.17	0.41	6.91	3.13	1.56	0.45	3.89	1.81	0.93	0.47
3	$\frac{3}{2}^-$	41.47	9.74	3.25	0.23	18.43	4.41	1.47	0.24	10.36	2.55	0.85	0.25
4	$0^+$	67.39	15.30	3.58	0.23	29.95	7.40	1.69	0.25	16.82	4.31	1.08	0.26

$N=2 \rightarrow 3 \rightarrow 4$  (ii) one has always  $B_4 > 2B_2$ , suggesting an effective attraction between dineutrons (iii) the binding energy per particle increases when going from  $N=2$  to  $N=4$  (iv) the ratio  $\frac{B_N}{E_{HO}}$  tends to a constant value independent of  $b$ . The preceding results tend to indicate that there is a benefit when going from 2 to 4. The main difference in respect to  ${}^3\text{He}$  has been found in the role of P-waves. Their influence in  $n$  case is attractive but very small whereas they significantly contribute to the  ${}^3\text{He}$  binding energy ( $\sim 40\%$ ). The reason for such a different behaviour is the hard core radius of the corresponding potentials, which differ by a factor 3 (see Fig. 1). The centrifugal barrier is one order of magnitude smaller in  ${}^3\text{He}$  and the effective potential is, contrary to  $n$  case, still attractive in regions where it can play a role. This difference can be dramatic in binding larger fermion systems.

Despite the negative results quoted in [1], the question of larger neutron clusters merits some attention. At present, the strongest argument against their existence are the mean-field results, all concluding to an unbounded infinite nuclear matter but it should be possible to reach the same conclusion "from below", i.e. from a systematic study of few-neutron systems. This can be performed by studying the  $N$ -dependence of the critical scaling factor  $\eta_c$ , calculated simultaneously for  $n$  and  ${}^3\text{He}$ . Our technology allow us to reach only  $N=4$  with the results displayed on Fig. 2. The value  $\eta_c^{(n)}$  makes a large jump when passing from  $N=2$  to  $N=3$  but starts to decrease when going from  $N=3$  to  $N=4$ . Is that a pure numerical accident or, as in  ${}^3\text{He}$ , an indication of a descent towards the  $\eta = 1$  axis?. More powerful methods could go far beyond  $N=4$  and draw a definite conclusion on this problem.

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