Sub-Nanometer Active Seismic Isolator Control

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ABSTRACT: Ambitious projects such as the design of the future Compact Linear Collider (CLIC) require challenging parameters and technologies. Stabilization of the CLIC particle beam is one of these challenges. Ground motion (GM) is the main source of beam misalignment. Beam dynamics controls are however efficient only at low frequency ($<4\text{Hz}$), due to the sampling of the beam at 50 Hz. Hence, ground motion mitigation techniques such as active stabilization are required. This paper shows a dedicated prototype able to manage vibration at a sub-nanometer scale. The use of cutting edge sensor technology is however very challenging for control applications as they are usually used for measurement purposes. Limiting factors such as sensor dynamics and noise lead to a performance optimization problem. The current state of the art in GM measurement and GM mitigation techniques is pointed out and shows limits of the technologies. The proposed active device is then described and a realistic model of the process has been established. A dedicated controller design combining feedforward and feedback techniques is presented and theoretical results in terms of Power Spectral Density (PSD) of displacement are compared to real time experimental results obtained with a rapid control prototyping tool.

Key Words: Control, actuator, sensor, piezoelectric, optimization

Nomenclature

		QM	Quadrupole Motion
CERN	European Organization for Nuclear Research	$\text{RMS}_x(f)$	Root Mean Square of signal x in the frequency range $[f \infty]$
PSD	Power Spectral Density	$A(s), V(s)$	Accelerometer and velocity sensor transfer function
CLIC	Compact Linear Collider	A_{ff}, V_{ff}	FF controllers for accelerometer and velocity sensor

CMS	Compact Muon Solenoid	A_{fb}, V_{fb}	FB controllers for accelerometer and velocity sensor
FB	Feedback	$F_{a,v}$	Extra filters applied to acceleration (a) or velocity (v) FF controllers
FF	Feedforward	$M_{a,v}$	Accelerometer and velocity sensor measurements
FFT	Fast Fourier Transform	$N_{a,v}$	Noise model of the accelerometer (a) or velocity (v) sensors,
GM	Ground motion	S_c	Model of the active support
IP	Interaction Point	S_g	Transfer function from ground to support position
LAPP	Laboratoire d'Annecy-le-Vieux de Physique des Particules	S	Top support position
LHC	Large Hadron Collider	$U_{a,v}$	Acceleration and velocity commands
ML	Main Linac	W_n	White noise with PSD = 1

INTRODUCTION

The future Compact Linear Collider (CLIC), (CERN collaboration, 2012) currently under study will accelerate electrons and positrons in two linear accelerators over a total length of about 48 km, colliding them at the Interaction Point (IP) with a nominal luminosity of $2 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$. The beam is accelerated and guided thanks to several thousands of accelerating structures and heavy quadrupoles along the Main Linac (ML), see **Figure 1**. The former accelerate the particles at the required energy, the latter maintain the beam inside the vacuum chamber to reach the required luminosity at the IP.

Figure 1. Simplified layout of CLIC.

The luminosity requirement imposes tight constraints on the particle beams' motion and consequently on the Quadrupoles' Motion (QM) subject to Ground Motion (GM). As the shape of the beam is elliptic, its vertical dimension being 45 times smaller than its horizontal one, requirements on the vertical position of the beam are tighter. This paper focuses on the most critical case that is the vertical motion. The desired performances are expressed in terms of displacement RMS (Root Mean Square), which

is the integral of the Power Spectral Density (PSD) within a given frequency range, as detailed in Eq. 1:

$$RMS_x(f_{min}) = \sqrt{\int_{f_{min}}^{\infty} PSD_x(f) df}, \quad (1)$$

x being the signal to analyze. $RMS_x(f_{min})$ is the square root of the power of the signal x calculated in the frequency range $[f_{min}, \infty[$. The displacement $RMS_x(f_{min})$ specifications depend on the localisation along the accelerator. For the whole Main Linac (ML), $f_{min} = 1$ Hz and $RMS_{QM}(1)$ shouldn't exceed 1.5 nm. Regarding the IP, $f_{min} = 4$ Hz and $RMS_{QM}(4)$ should be less than 0.15 nm. Frequency specification f_{min} is due to beam-based feedbacks in the ML (Pfungstner et al., 2011) and at IP (Balik et al., 2011; Caron et al., 2012) able to mitigate only low frequency displacements.

As the future CLIC location site is still unknown, the reference GM is the one measured at LAPP (Annecy - France). This is also the location where the experimental tests were done. However, it is expected that the future accelerator will benefit from better conditions, like the Large Hadron Collider (LHC) (Virdee, 2010) at CERN, safely shielded by 50 – 100 meters of rock below ground. **Figure 2** shows the PSD of the GM displacement and $RMS_{GM}(f)$ at LAPP and at the Compact Muon Solenoid (CMS) (The CMS Collaboration, 2008) experimental hall, one of the multi-purpose detectors on the LHC, representative of the detectors of the future CLIC.

Figure 2. PSD and RMS of GM measured at LAPP and CMS detector.

Before CLIC, such specifications have never been needed for a particle accelerator (or any other system) but in order to meet these tight constraints on the QM, sub-nanometer active stabilization is envisaged. In precision engineering studies, most

active controls have been carried out at micrometer scale in many fields (automotive, aeronautic...) or only positioning, without active control, at nanometer scale (optical system...). It is very exceptional to have active stabilization requirements at nanometer scale, and it is a huge challenge. However, they are necessary for the future particle physics discoveries.

This section summarizes a non-exhaustive list of key experiments built to stabilize the quadrupoles. **Table 1** lists some of their characteristics.

Table 1. Summary of current vibration stabilization strategies.

Institution	CERN (Collette et al., 2011)	CERN (Gaddi et al., 2012)	DESY (Montag, 1996)	SLAC (Frisch, Chang, et al., 2004)
Technology	Active	Passive	Active	Active
System rigidity	Stiff	Soft	Stiff	Soft
Actuator	Piezoelectric	N/A	Piezoelectric	Electrostatic
Sensors	Guralp CMG-6T	N/A	Kebe ¹ geophones	GS-1 seismometers ²
DOF	6	1	1	6
RMS_{GM}/RMS_{QM}	3 at 4 Hz, 2.5 at 1 Hz	2 at 4 Hz, 0.1 at 1 Hz	4 at 4 Hz, 3 at 1 Hz	5 at 4 Hz, 3 at 1 Hz

A performance index defined by the ratio between the displacement RMS of the ground RMS_{GM} and of the quadrupole to stabilize RMS_{QM} gives the global efficiency of the different experiments at a given frequency.

Although efficient, none has been tested in a quiet environment at the sub-nanometer scale except the first one (Collette et al., 2011) so the limitations of the whole instrumentation (noise, sensitivity...) is not completely taken into account. Each of these strategies has its own advantages and drawbacks; although the softness increases the isolation at low frequencies, an overall stiff support like in this paper (or in (Collette et al., 2011) and (Montag, 1996)), would be less sensitive against external forces (Artoos et al., 2011). The sensor is one of the most important parts of the stabilization system and should be chosen according to the control strategy. Thus, SLAC³ and CERN have built their own sensors (Frisch, Decker, et al., 2004; Janssens et al., 2011), more suitable for an accelerator environment and for control. Another important point, is the number of degrees of freedom (DOF) of the support that determines the ability to control GM vibration in any direction (Collette et al., 2011; Frisch, Chang, et al., 2004). Albeit the developed support has been designed with three DOF, this paper is limited to the control of one degree of freedom.

This paper describes in detail the control strategy applied on a prototype already presented briefly in (Balik et al., 2010) of an active support aimed to reduce the $RMS_x(f)$ displacement of ML and IP quadrupoles. Second section provides a technical description of the active support i.e. realistic model of the sensors, actuator, noises and support. Third section explains in detail the control strategy. The experimental setup is described in section 4 and simulation and experimental results are compared. The last section of this paper draws the conclusions and opens to future work.

ACTIVE SUPPORT

Electromechanical system

The most commonly used technology to generate nanometer displacements is a piezoelectric actuator. Although electrostatic actuators (Sarajlic et al., 2003) are sometimes used (Frisch, Chang, et al., 2004) for this type of application, they are not able to reach a sub-nanometer resolution. Moreover, the GM displacement amplitude in the frequency range of interest (i.e. $[1 - 100]$ Hz) can reach 10 nm (see **Figure 2**). The actuators also need to support heavy magnets. Thus, the choice corresponding to our need is a PPA10M from Cedrat⁴, resonant frequency: 65 kHz, response time: 0.01 ms, max tensile force: 800 N, max displacement: 8 μm . The resolution of this actuator is limited by the noise of the driving voltage. To increase the resolution, stiffness is added in parallel with the actuator and decreases the generated displacement (see **Figure 3**). This solution is suitable because the maximal actuator elongation is 8 times greater than required. By applying the appropriate stiffness, it is then possible to lower the resolution by a factor 5, leading to a max displacement of 1.6 μm and a resolution of about 10 nm/V.

Figure 3. Layout of the active Isolation System with parallel stiffness.

Figure 4 shows the sketch of the proposed active isolation with a quadrupole support. Capacitive sensors are only used for the identification of the model of the mechanical part. The elastomeric strips allow on the one hand the vertical guidance of the upper part of the support and on the other hand, further development with increased number of degrees of freedom, especially for horizontal vibration damping.

Figure 4. 3D view with the quadrupole support.

Figure 5 represents the frequency response $S_c(s)$ of the active support from control command to the support position. The gain corresponds to the piezoelectric actuator sensitivity of 10 nm/V.

Figure 5. Frequency response of the active support $S_c(s)$ [m/V].

The transfer function from ground to support position $S_g(s)$ has the same dynamics but with a unity gain (Balik et al., 2010). In the final experiment, each IP quadrupole will be installed on 5 supports. In this paper the control of one support without load will be tested as the design of the quadrupole is not definitive and a representative prototype is not yet available.

Sensors

Beam components like quadrupoles have to be stabilized down to the sub-nanometer level. The vibration isolation is a problem that has led to many approaches (Preumont et al., 2002; Tjepkema et al., 2012), but sub-nanometer stabilization requires state of the art electronic devices such as very low noise sensors, high resolution actuators or an ultra-low noise acquisition chain.

The use of cutting edge sensor technology is very challenging for control applications as they are usually used for measurement purposes. It induces complex management of the given sensor transfer function with limited bandwidth, spurious frequencies, delays... For these reasons, two types of commercial sensors are used in this paper for the measurements and controls: the velocity sensor Güralp CMG-6T for the low frequency range and the acceleration sensor Wilcoxon 731A for the upper frequency range, despite its internal delay. The experimental transfer function of the velocity sensor $V(s)$ and the accelerometer $A(s)$ are shown in **Figure 6**.

The Güralp sensors are high sensitive electromagnetic geophones measuring velocity in 3 directions (vertical and 2 horizontal). They have a flat frequency response from 0.03 Hz to 100 Hz. The operating range is yet closer to [1.5 - 90] Hz as their internal noise at low frequency is rather high when the ground velocity is very low. Wilcoxon sensors are high sensitive piezoelectric accelerometers measuring in the vertical direction with a flat frequency response between 0.01 Hz and 500 Hz, but with an operating range of [10 - 200] Hz due to the noise.

Figure 6. Velocity sensor and accelerometer transfer functions.

When measuring nano-displacements, resolution and noise of the measurement chain is also a limiting factor. Consequently, these noises and those of the sensors have been measured and are described in the next section.

Acquisition chain, sensors and analog converter noises

The Analog to Digital Converter (ADC) as well as the Digital to Analog converter (DAC) (respectively ds2004 and ds2102 from dSPACE, compatible with Matlab/Simulink) are high-speed, 16 bits resolution boards. The noise of these converters has been characterized as shown in **Figure 7**.

Signal conditioning is done thanks to active high-pass and low-pass filters and amplifiers from Krohn-Hite Corporation. The Krohn-Hite Model 3384 has four independent channels and provides a tunable frequency range from 0.005 Hz to 200 kHz. The level of noise of this system has been measured and is negligible compared to the ADC' noise in the range of interest (i.e. [0.1 100] Hz).

The performances of the measuring system (including sensors) have been characterized by the data that were taken with the sensors of the same model placed side-by-side. The sensor's noise is then calculated by using the corrected difference method (The NLC Design Group, 1996). Results in terms of PSD are given in **Figure 7**.

Figure 7. PSD displacement equivalent noise of sensors, D/A and A/D converters compared to ground motion

All these noises have been measured using the test bench presented in **Figure 13**. In order to compare their respective influence, they are all expressed in m^2/Hz . For that, the corresponding transfer functions (inverse of sensors, amplifiers and actuators) have been used.

Noise models

The sensors' models are driven by a white noise (W_n) with a PSD equal to 1 whatever the frequencies. In order to fit experimental results, the transfer functions of the noise models for the accelerometer and the velocity sensors were found to be:

$$N_a(s) = \frac{0.02s + 1}{1.06s + 1} 2.13 \times 10^{-4}, \quad (2)$$

$$N_v(s) = \frac{1.866 \times 10^{-11}s^3 + 1.829 \times 10^{-9}s^2 + 6.897 \times 10^{-8}s + 10^{-6}}{2.533 s^3 + 2.546 s^2 + s} \hat{V}(s), \quad (3)$$

where $\hat{V}(s)$ is the identification of the transfer function of the velocity sensor.

The ADC noise is modeled by W_n multiplied by a gain equal to 1.42×10^{-6} corresponding to a 97dB S/N ratio at a sampling period of 50×10^{-6} s while the D/A converter noise is modeled by $2 \times 10^{-6}W_n$ corresponding to a 94dB S/N ratio.

CONTROL STRATEGY

The objective of the control strategy is to reject GM. The control strategy has to take into account:

- noises of sensors all through the acquisition chain,
- noise of digital to analog converter,
- sensor and support transfer function characteristics.

The GM can be measured on the floor and on top of the support; the control strategy will then use 4 measurements coming from 2 accelerometers and 2 geophones.

Control scheme

FF control is best deployed in control systems design applications where the process and the disturbances are well understood. This is indeed the case, on the one hand, for the active support and the sensors which can easily be characterized and on the other hand for the GM which can be measured. Due to the limited but complementary characteristics of the sensors, the operating range of the FF control can be extended by using both sensors. **Figure 8** represents the block diagram of the FF control.

Figure 8. Block diagram of FF controls.

The velocity FF controller V_{ff} is given by:

$$V_{ff} = \hat{V}^{-1} \hat{S}_c^{-1} \hat{S}_g F_v. \quad (4)$$

Where F_v represents high and low pass filters as well as some extra poles to obtain proper transfer function and upper ^ denotes the identification of the corresponding transfer function. In the same way, the acceleration FF controller A_{ff} is given by:

$$A_{ff} = \hat{A}^{-1} \hat{S}_c^{-1} \hat{S}_g F_a. \quad (5)$$

Where F_a plays the same role as F_v . The efficiency of FF controllers is nevertheless limited by imperfections and modeling errors. The control has therefore been extended with two feedback (FB) controllers that have been added to the control scheme, see **Figure 9**.

Figure 9. Block diagram of feedback controls.

The loop with the velocity sensor includes 3 derivatives and the loop with the accelerometer sensor includes 2 derivatives. The two controllers A_{fb} and V_{fb} are adjusted using loop shaping of the Nichols plot. Both controllers are computed with the following constraints on the open-loop:

- max gain close to 25 dB,
- low-frequency 0dB cross below 1 Hz,
- high-frequency 0dB cross above 100 Hz.

The FF and the FB controls are then added together, and lead to the theoretical attenuation given in **Figure 10**:

Figure 10. Theoretical attenuation of the whole control compared to FF and FB only.

Noise considerations

The obtained attenuation given in **Figure 10** is ideal but the experimental one is limited by the presence of noise. Indeed, due to Bode's theorem, a high attenuation at low frequency increases the noise effect at high frequency. Hence, the controller settings must take into account all the noise sources discussed in section “**Acquisition chain, sensors and analog converter noises**”. **Figure 11** summarizes the noises that affect the output S .

Figure 11. Noise sources.

W_n through noise model N_1 or N_2 represents any of the noise sources (sensors, ADC and DAC) for the velocity and the acceleration loops, C_1 , C_2 , H_1 and H_2 are the transfer

functions after and before the noise sources, S is the signal affected by the noises.

For example, for the velocity sensor noise, we have:

$$C_1 = S_c V_{fb}, \quad (6)$$

$$H_1 = V, \quad (7)$$

$$N_1 = N_v. \quad (8)$$

Inside the bandwidth of the loops where $C_1 H_1 \gg 1$ and $C_2 H_2 \gg 1$ then:

$$S = \frac{N_1}{H_1} + \frac{N_2}{H_2}. \quad (9)$$

Outside the bandwidth of the loops where $C_1 H_1 \ll 1$ and $C_2 H_2 \ll 1$ then:

$$S = C_1 N_1 + C_2 N_2. \quad (10)$$

Inside the bandwidth of the loops, high gains are needed for H_1 and H_2 and outside it is important that C_1 and C_2 have a low gain. This has been taken into account for the controller structure design and the needed performances.

Concerning the noises introduced by the FF controllers, they can easily be introduced using N_1 or N_2 . The analytical effect of all noises (i.e. total equivalent output noise) is shown in **Figure 12** and compared to a simulation plot of the top support motion obtained with the proposed control framework.

Figure 12. Effect of all noises on the output.

At low and high frequencies, **Figure 12** shows that it is not possible to reduce further the support displacement due to the different noises in the control scheme where the top support motion is at the same level as the noises. An improvement can be expected around 20 Hz. **Figure 12** also shows that the main limitation of the attenuation

is due to the different noise sources.

Based on this control scheme, a simulation program using MATLAB has been used in order to help define the two controllers:

- low and high pass filters for the FF controllers,
- loop-shaping of the FB controllers,
- best result for a given set of sensors

One of the main limitations being the sensor noise, this simulation program helps us define the sensor characteristics needed (noise characteristics and transfer function) for a given performance keeping in mind the need for reasonable costs. This is discussed in section “**Results and improvements**”.

TEST BENCH

Experimental setup

The whole setup is shown in **Figure 13**. Sensor signals have been filtered using a real time 8th order Butterworth 20 kHz low pass filter and amplified to fit optimally in the range $\pm 5V$ of the ADC channels.

All controllers are implemented using a digital scheme. For the controller discretization, the delta operator has been used (Goodwin et al., 1992) with a sampling period of 50 μs . The delta operator is useful in the presence of slow and fast dynamics and very small sampling period that could lead to bad numerical conditioning.

Figure 13. Experimental setup.

Results

For a better understanding of the results, we will distinguish between the “real” support displacement as obtained through the control process, and the “observed” support displacement as measured by the sensors. The objective is to come as close as possible to the “real” displacement. The sensors being more or less accurate according to the frequency range and the sensor type, as shown in **Figure 7**, the “observed” PSD of the support motion has been reconstituted by taking the PSD at frequencies where the sensors are less noisy, that is (velocity sensors at low frequency and accelerometers at higher frequency):

$$\widehat{PSD}_S = [PSD_{M_v \hat{v}^{-1}}(0 - 16 \text{ Hz}) ; PSD_{M_a \hat{a}^{-1}}(16 \text{ Hz} - \infty)]. \quad (11)$$

The experimental attenuation, compared to the simulation is given in **Figure 14**. The theoretical attenuation, corresponding to the “real” values that can be obtained by the system is also plotted on the figure.

Figure 14. Theoretical attenuation and experimental attenuation compared to simulation.

The experimental results show a really good fit between theory and experiment. Albeit the obtained attenuation is an important criterion, the displacement RMS remains the reference. This leads to the experimental support motion RMS given in **Figure 15**. It is nevertheless not possible to reconstruct the GM outside the operating range of the sensors (i.e. $f \in [1.5, 200]$ Hz), where the real PSD should obviously be lower.

Figure 15. RMS comparison.

RESULTS AND IMPROVEMENTS

Concerning the ML, the needed performances of 1.5 nm at 1Hz were reached with the proposed control strategy. Concerning the IP, the RMS is three times the needed performances. In order to obtain an RMS of 0.15 nm at 4 Hz, the noises need to be further reduced. **Figure 16(a)** shows the sensors and hardware limitations;

Figure 16. (a) Noises of FB velocity sensor, (b) Noises of FF velocity sensor.

The velocity sensors introduce too much noise at low and at high frequency. New commercial sensors have to be tested or a complete original design could be considered in order to increase the loop gain and then the system attenuation. The accelerometer has been used to reach higher frequencies, but its delay limits its usability in this range of frequencies, a new accelerometer has to be introduced in the control. Above 400 Hz,

the seismic attenuation is limited by the D/A converter noise. As the simulation and the experiment have similar behavior, it is possible to use the simulation results to find the new sensor and D/A characteristics needed to increase the system's performance further.

CONCLUSION

This study attempts to solve one of the most critical technical aspects of the future CLIC particle collider. In this prospect, a dedicated control strategy for ground motion mitigation is detailed. Based on a dedicated interpretation of classical loop shaping control design methods for controller tuning, the innovation consists in using sensors not intended for control at the sub-nanometer scale. Furthermore, the original control strategy consists in the cumulative action of acceleration and velocity feedforward control combined with feedback loops. In our approach, the Matlab/Simulink simulation results of the control are also compared with the real time experimental results. Theoretical results match the real time results with a small deviation, which is due to model imperfections and the limitation of the D/A converter resolution. The performance of the control, defined by the ratio $\text{RMS_GM}/\text{RMS_QM}$ is about 5 at 4 Hz and 2.5 at 1 Hz, comparable to the best stabilization strategy performances presented in Table 1. The results lead to a RMS displacement of the top support of about 1.5 nm at 1 Hz and 0.6 nm at 4 Hz. Specifications are reached concerning the ML ($\text{RMS_QM}(1) < 1.5$ nm) but not for the IP ($\text{RMS_QM}(4) < 0.15$ nm). Possible ways for improving performance in GM mitigation are outlined. The main limitation concerns the sensors' noise, thus ongoing research efforts concentrate on sensors with better performances for this dedicated study with the help of the validated simulation program. Another avenue of improvement concerns the ADC resolution which induces limitations at high frequency. The next step will be to consider a representative heavy quadrupole on top of the support to address additional specifications.

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NOTE

1. KEBE Scientific Instruments, Schwingungsmesser SMK-1 manual, Halstenbek 1994.
2. OYO Geospace Inc.
3. Stanford Linear Accelerator Center.
4. CEDRAT Group.

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