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Electron shakeoff following the $\beta^+$ decay of trapped $^{35}$Ar$^+$ ions

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The electron shakeoff of $^{35}$Cl atoms resulting from the $\beta^+$ decay of $^{35}$Ar$^+$ ions has been investigated using a Paul trap coupled to a recoil-ion spectrometer. The charge-state distribution of the recoiling daughter nuclei is compared to theoretical calculations accounting for shakeoff and Auger processes. The calculations are in excellent agreement with the experimental results and enable to identify the ionization reaction routes leading to the formation of all charge states.

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Precision measurements of the recoil-ion energy spectra in nuclear $\beta$ decay constituted sensitive tools to establish the vector axial vector structure of the weak interaction [1–3]. In particular, these measurements provide access to the so-called $\beta - \nu$ angular correlation coefficient, $a_{3\nu}$, which is sensitive to scalar and tensor exotic couplings excluded by the Standard Model of elementary particles [4]. The search for such exotic interactions has motivated new experiments using modern trapping techniques coupled to intense radioactive beams with high production rates [4]. Most of ongoing experiments detect the $\beta$ particles and the recoil-ions in coincidence, providing a precise recoil-ion energy measurement using time of flight (TOF) techniques, and a precise control of systematic effects [5–7]. The LPCTrap setup [8, 9], installed at GANIL, is based on the use of a Paul trap, to confine radioactive ions, coupled to a recoil-ion spectrometer. It has been recently upgraded to perform simultaneous measurements of both the charge-state and the energy of the recoil-ions. Fundamental atomic processes such as electron shakeoff (SO) resulting from the sudden change of the central potential can thus also be addressed through a measurement of the charge-state distribution of the recoiling ions. The setup has already enabled the measurement of electron SO in the decay of $^6$He$^+$ [10]. For this ideal textbook case, with only one electron, simple quantum calculations based on the sudden approximation (SA) could be tested with a relative precision better than $4 \times 10^{-4}$. Beyond the prototypical $^6$He$^+$ case, heavier systems such as $^{35}$Ar$^+$ can reveal the role of more subtle shakeoff dynamics involving several electrons, and of subsequent relaxation processes such as the emission of Auger electrons. These multi-electron processes, of paramount importance in atomic and molecular physics, have mainly been studied as post-collision mechanisms following the absorption of a photon in the X-ray spectral range (see for instance [11–14]). Alternatively, SO and Auger processes can conveniently be decoupled within multi-electron rearrangements induced by sudden nuclear $\beta$-decay. These ionization mechanisms have been explored for a large variety of $^{35}$Ar$^+$ emitters [15]. In contrast, information is scarce for $\beta^+$ decaying parent atoms [6, 16, 17] and even totally missing, up to our knowledge, for multi-electronic singly-charged systems. We thus investigate here the charge-state distribution following $\beta^+$ emission of $^{35}$Ar$^+$. In addition to be interesting per se, it is worth noting that SO can further be a source of systematic error for $\beta - \nu$ angular correlation coefficient measurements. This systematic error, that was found to be small in a previous LPCTrap experiment on $^6$He$^+$ decay [7], would become problematic for many electron systems. For the WITCH setup [18] installed at ISOLDE-CERN, whose main goal is to measure $a_{3\nu}$ in the decay of $^{35}$Ar$^+$ ions confined in a Penning trap, an independent measurement of the charge-state distribution of the recoil ions will ease the analysis and improve the precision [19].

The experimental setup has been described in detail previously [8–10]. The radioactive $^{35}$Ar nuclei were produced at the SPIRAL target-ECR ion source system of GANIL, Caen, France, by a primary beam of $^{36}$Ar ions impinging on a graphite target. After mass separation the $^{35}$Ar$^+$ ions were guided at 10 keV through the LIRAT low energy beam line. At the entrance of the LPCTrap apparatus, the $^{35}$Ar$^+$ beam intensity was typically 10$^6$ pps. The ions were first injected in a Radio Frequency Cooler and Buncher (RFQCB) [20] for the beam preparation. This linear Paul trap, mounted on a high voltage platform to decelerate the ions down to 50 eV, was filled...
The detector calibrations was identical to that described in Ref. [7]. Only events corresponding to a $\beta$ particle depositing more than 0.4 MeV in the scintillator were kept in the analysis. The TOF distribution measured for the $^{35}$Cl$^+$ recoil ions resulting from $^{35}$Ar$^+$ decay is shown in Fig. 2(a). A constant background in TOF due to uncorrelated signals from the recoil ion and $\beta$ detectors has been subtracted from the data.

The experimental charge-state branching ratios and their associated statistical uncertainty were simply deduced from the integration of counts within the TOF selection windows displayed on Fig. 2(a). Two additional corrections, labeled Tail$_{corr.}$ and MCP$_{corr.}$ in Table I, were then applied. The first takes into account the tails of charge distributions extending beyond their respective integration windows. TOF spectra associated to each charge-state were generated using Monte-Carlo simulations [7, 10] and were adjusted to the experimental data. Several ingredients of the simulations, such as the exact size of the trapped ion cloud, weak decay branches of $^{35}$Ar towards excited states, and possible scattering of the $\beta$ particles on parts of the trapping chamber were neglected or approximated. Therefore, a conservative relative uncertainty of 10% was applied on these corrections.

The second correction concerns the dependence of the MCPPSD detection efficiency on the charge-state of the recoil ions. The loss of detected events due to electronic threshold was precisely estimated by fitting the charge distributions collected from the recoil ion detector with gaussian functions (Fig. 2(b)). The data were then corrected for the relative detection efficiency obtained for each charge-state. For charged recoil ions, the experimental charge-state branching ratios including these corrections are given in Table I. Electron capture probabilities from He buffer gas between the Paul trap and the spectrometer have also been estimated using experimental cross sections measured for Kr$^{q+}$ + He collisions in...
the same velocity regime [22]. Kr and Cl having similar ionization potentials, the charge exchange cross sections for Kr$^{2+}$ ions constitute a good approximation of what one would expect with Cl$^{3+}$ ions. Even for the higher charge states involved here ($q=5$ and 6), these probabilities are only of the order of a few $10^{-4}$. They were therefore neglected at the present level of precision. For a dominant part of the decay events, there is no electron shakeoff and the $\beta^-$ decay of a 35 Ar$^+$ ion results in the recoil of a neutral 35 Cl atom. For Cl recoil atoms, both the collection efficiency and the MCPPSD detection efficiency are very low, and depends strongly on their initial energy. The TOF associated to such detected events being larger than 11 $\mu$s, they do not appear on the spectrum shown in the Fig. 2(a). To estimate the number of 35 Cl atoms produced during the experiment, we have used the number of $\beta$ particles detected in "singles" (without condition on the detection of a recoil). Knowing the overall absolute detection efficiency for ions, the fraction of the "singles" events associated to charged 35 Cl recoils could be inferred, the rest being associated to 35 Cl atoms. This estimate leads to 72(10)% of neutral 35 Cl recoils, with an uncertainty dominated here by the error on the overall ion detection efficiency. This result is in good agreement with the 73.9% ratio obtained from the theoretical calculations that we detail hereinafter.

Subsequently to the sudden decay of 35 Ar$^+$, primary Cl$^{q+}$ ions are formed by ionization. In the framework of the independent electron model (IPM,[23]), well suited to describe the dynamics of multielectronic systems, the probability to ionize $q_S = q$ electrons among the $N = 17$ total ones reads

$$\tag{1} P_{qS}^{\text{ion}} = \sum_{i_1=1}^{N} p_{i_1} \sum_{i_2 \geq i_1}^{N} p_{i_2} \cdots \sum_{i_{qS} \geq i_{qS-1}}^{N} p_{i_{qS}} \prod_{j \neq i_1, \ldots, i_{qS}} (1 - p_j)$$

where $p_i$ is the one-electron ionization probability for the $i^{th}$ electron. In our work, $p_i$ results from SO, with the underlying assumptions: (i) the so-called direct ionization mechanism, in which the $\beta$ particle knocks out orbital electrons, is neglected, and (ii) shakeup processes, which would imply electron excitation(s) as a result of the $\beta$-decay, are also neglected. Assumption (i) is consistent with the fact that the $\beta$ emission energy (with end point $E_{\text{max}}^\beta = 4.94$ MeV) is considerably larger than the energy of bound electrons, so that direct ionization is unlikely [24]. Most of the inelastic processes involving electron vacancies in intermediate- and large-Z species consist of transitions to the continuum [25], justifying (ii). Therefore, the one-electron ionization probability $p_i$, with $i$ initially belonging to the $(n_i, l_i)$ subshell, is expressed as

$$\tag{2} p_i = 1 - \sum_{n \leq 3} \left| \langle \varphi_{n_i l_i}^{(\text{CI})} | e^{-iK \mathbf{r}} | \varphi_{n_i l_i}^{(\text{Ar})+} \rangle \right|^2$$

in the rest frame of the daughter nucleus of mass $M$ which recoils with energy $E_R$ and momentum $K = \sqrt{2E_R/M}$ (in atomic units). $\varphi_{n_i l_i}^{(\text{Ar}+\text{Cl})}$ is the wavefunction describing one electron orbiting in the $nl$-subshell of Ar$^+$ or Cl. Because of the small values of $K$ ($E_R^{\text{max}} = 452$ eV), $e^{-iK \mathbf{r}}$ can be expanded in eq. (2) in order to highlight the mechanisms underlying $\beta^-$ induced SO. Up to second order in $K^2$, we obtain [26]

$$\tag{3} p_i = 1 - \sum_{n \leq 3} \left\{ \left| \langle \varphi_{n_i l_i}^{(\text{CI})} | \varphi_{n_i l_i}^{(\text{Ar})+} \rangle \right|^2 + K^2 \left( \langle \varphi_{n_i l_i}^{(\text{CI})} | \varphi_{n_i l_i}^{(\text{Ar})+} \rangle \right)^2 - K^2 \text{Re} \left( \langle \varphi_{n_i l_i}^{(\text{CI})} \varphi_{n_i l_i}^{(\text{Ar})+} \rangle \langle \varphi_{n_i l_i}^{(\text{CI})} | \varphi_{n_i l_i}^{(\text{Ar})+} \rangle \right) \right\}.$$ 

It is thus clear that ionization stems from the coherent superposition of two effects: the static Ar$^+/\text{Cl}$ orbital mismatch, through the $\langle \varphi_{n_i l_i}^{(\text{CI})} | \varphi_{n_i l_i}^{(\text{Ar})+} \rangle^2$ terms, and the recoil of the Cl daughter nucleus, through the $K^2$-dependent terms in (3).

For the calculation of the recoil-induced ionization terms involved in (3), we have used the mean recoil energy obtained in our experiment, $E_R = 376$ eV, to define the numerical value of $K$ ($0.02074$ a.u.). As Ar$^+$ and Cl are open-shell valence systems, the wavefunctions $\varphi_{n_i l_i}^{(\text{Ar}+\text{Cl})}$ have been computed by means of Restricted Open-shell Hartree-Fock (ROHF) calculations using the GAMESS-US quantum-chemistry package [27]. These wavefunctions can alternatively be obtained in terms of Unrestricted Hartree-Fock (UHF) computations [28], and we found that the ROHF and UHF $p_i$ probabilities differ by less than 1% for all the 1s, ..., 3p levels [29].

Once inner-shell vacancies have been created in Cl through ionization, radiative and Auger transitions involving higher-lying electrons tend to fill these vacancies. The probabilities associated to these transitions have to be properly introduced in our calculations, especially as Auger processes are known to contribute significantly to the production of high charge states [17]. Kaastra and Mewe [31] have computed the probabilities $\tilde{p}_i^{s,m_i}$ corresponding to the ejection of $m_i$ electrons through Auger cascades after the electron $i$, element of the inner $n_i l_i$-subshell, has been removed from Cl$^{q+}$. $s$ is the ionization stage of Cl and corresponds to the number of electrons previously pulled out from the outermost subshells. Consistently with the treatment of multiple SO ionization, the description of multiple vacancies, and related Auger cascades, is performed in the IPM framework. The probability for ejection of $q_S$ electrons by SO followed by Auger removal of $q_A$ electrons thus reads

$$\tag{4} P_{qS,qA} = \sum_{m_1 = 0}^{m_{\text{max}}} \cdots \sum_{m_{qS} = 0}^{m_{\text{max}}} \sum_{i_1 = 1}^{N} p_{i_1} \tilde{p}_{i_1}^{s,m_{i_1}} \sum_{i_2 > i_1}^{N} p_{i_2} \tilde{p}_{i_2}^{s,m_{i_2}} \cdots \sum_{i_{qS} > i_{qS-1}}^{N} p_{i_{qS}} \tilde{p}_{i_{qS}}^{s,m_{i_{qS}}} \prod_{j \neq i_1, \ldots, i_{qS}} (1 - p_j)$$
where \( q_s + q_A = q \), the charge state finally observed.

The computed charge-state branching ratios, which consist of the relative populations of \( \text{Cl}^{q+} \) species among the total ion yield, are compared to their experimental counterparts in Table I. Eq. (4) provides a very good agreement with the measurements.

The calculations can then be used to discriminate between the roles of SO and Auger transitions in the production of \( \text{Cl}^{q+} \) ions. Neglecting Auger decays, \( i.e. \) computing the charge-state distribution according to Eq. (1), severely distorts the \( \text{Cl}^{q+} \) populations: the \( q = 1 \) population is overestimated by \( \sim 13\% \) while multiple SO is inefficient to explain the abundance of \( q \geq 3 \) states. Such an importance of Auger processes has to be contrasted with previous studies on lighter systems where differences between full and SO-restricted calculations did not exceed a few percent (see e.g. [17]). The increase of the Auger importance with increasing \( Z \) can simply be related to the higher multiplicity of Auger cascades; for instance, we derive from [31] that \( \text{Cl}^+(1s^{-1}) \) preferentially stabilizes by emitting 3 electrons while \( \text{Na}^+(1s^{-1}) \) relaxes by ejecting only 1 electron.

The calculations can also be employed to estimate the role of recoil-induced ionization by artificially setting \( K = 0 \) in eq. (4). The static orbital mismatch explains most of SO ionization (see Table I). However, accounting for the recoil changes the final population of neutral Cl from 74.5 to 73.9\%. Even if it looks small at first sight, such a variation can significantly influence the precise determination of the \( a_{\beta\nu} \) correlation coefficient [17]. The nuclear recoil is almost inconsequential to the charge-state distribution (Table I). Multiple ionization from primary SO is small (\( \sim 3\% \)) so that the relative populations of \( \text{Cl}^{q+} \) high charge states are mainly monitored by the subsequent Auger cascades.

Finally, we can search within Eq. (4) the electronic probabilities which mostly contribute to the formation of a given \( \text{Cl}^{q+} \) state. The ionization routes contributing more than 1\% to the formation of \( \text{Cl}^{q+} \), with \( 1 \leq q \leq 5 \), are presented in Table II. Single SO from \( n = 3 \) states explains \( \sim 100\% \) of \( \text{Cl}^+ \) formation since ionization in inner shells leads to the formation of higher charge states through Auger cascades with almost 100\% probability.

For \( \text{Cl}^{2+} \), twofold SO from the outer \( n = 3 \) shell, eventually followed by radiative stabilization when 3s holes are involved, represents \( \sim 50\% \) of the population and single Auger transitions filling the 2p\(^{-1}\) SO-hole make the rest. The relevance of SO ionization with multiplicity greater than 2 rapidly falls down (see Table I). As a result, the creation of \( \text{Cl}^{5+} \) ions with \( q \geq 3 \) mostly involves Auger decays subsequent to one- and two-fold SO ionization. Moreover, multiple Auger emission, involving intermediate core-hole states and emission of several electrons during a single-hole decay, becomes increasingly important for high \( q \); it participates to almost 100\% of \( \text{Cl}^{5+} \) ion creation.

To sum up, our joined experimental/theoretical endeavour has provided a quite complete picture of ion formation resulting from the \( \beta^+ \) decay of \( ^{35}\text{Ar}^+ \). We plan to apply the same techniques to \( ^{19}\text{Ne}^+ \) and also revisit previous studies [17] in the near future. Besides the intrinsic interest of such investigations to nuclear physics, this will allow obtaining a more complete and \( Z \)-dependent picture of the underlying ionization mechanisms.

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TABLE II: Main ionization routes leading to Cl$^{n+}$ formation (in %). $nl^{-1}$ refers to primary SO hole creation in the $nl$-subshell of Cl while $m \times e_A$ means emission of $m$ Auger electrons. The asterisk indicates multiple Auger emission.

<table>
<thead>
<tr>
<th>Cl$^+$</th>
<th>Cl$^{2+}$</th>
<th>Cl$^{3+}$</th>
<th>Cl$^{4+}$</th>
<th>Cl$^{5+}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>3p$^{-1}$: 79.83</td>
<td>2p$^{-1} + 1e_A$: 49.71</td>
<td>2s$^{-1} + 2e_A$: 52.21</td>
<td>2s$^{-1}$3p$^{-1} + 2e_A$: 36.95</td>
<td>1s$^{-1} + 4e_A$: 35.56</td>
</tr>
<tr>
<td>3s$^{-1}$: 20.16</td>
<td>3p$^{-2}$: 29.32</td>
<td>2p$^{-1}$3p$^{-1} + 1e_A$: 29.36</td>
<td>1s$^{-1} + 3e_A$: 31.02</td>
<td>1s$^{-1}$3p$^{-1} + 3e_A$: 19.69</td>
</tr>
<tr>
<td>3s$^{-1}$3p$^{-1}$: 18.51</td>
<td>3s$^{-1}3p^{-2}$: 4.37</td>
<td>2p$^{-1}$3p$^{-2} + 1e_A$: 8.28</td>
<td>2s$^{-1}$3p$^{-2} + 2e_A$: 9.26</td>
<td>2s$^{-1}3s^{-1}3p^{-1} + 2e_A$: 5.84</td>
</tr>
<tr>
<td>3s$^{-2}$: 1.17</td>
<td>3p$^{-3}$: 3.46</td>
<td>2p$^{-2} + 2e_A$: 5.86</td>
<td>2s$^{-1}3s^{-1}3p^{-1} + 2e_A$: 5.84</td>
<td>2s$^{-2}3p^{-1} + 2e_A$: 3.66</td>
</tr>
<tr>
<td>1s$^{-1} + 2e_A$: 1.56</td>
<td>2p$^{-1}$3s$^{-1}$3p$^{-1} + 1e_A$: 5.23</td>
<td>1s$^{-1}$3s$^{-1} + 3e_A$: 4.90</td>
<td>2p$^{-2}3p^{-1} + 2e_A$: 3.66</td>
<td>2p$^{-1}3s^{-1}3p^{-2} + 1e_A$: 1.31</td>
</tr>
</tbody>
</table>

[29] It is quite common to employ the Roothan-Hartree-Fock (RHF) orbitals of Clementi and Roetti [30] to compute the ionization probabilities $p_i$. Even though we employ a different (and larger) underlying basis to construct the Ar$^+$ and Cl orbitals, we have verified that the $p_i$ values obtained with the orbitals of Clementi and Roetti differ by less than 1% from our ROHF and UHF values.