# Measurement of the $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ cross section at the LEP energies 

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# Measurement of the $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ cross section at the LEP energies 

DELPHI Collaboration


#### Abstract

The total and the differential cross-sections for the reaction $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ have been measured with the DELPHI detector at LEP at centre-of-mass energies from 130 to 183 GeV for an integrated luminosity of $78.19 . \mathrm{pb}^{-1}$. The results agree with the QED predictions. The lower limits (obtained including previously published results at the $Z^{0}$ energies) on the QED cutoff parameters are $\Lambda_{+}>253 \mathrm{GeV}$ and $\Lambda_{-}>225 \mathrm{GeV}$ and the lower bound on the mass of an excited electron with an effective coupling constant $\lambda_{\gamma}=1$ is $231 \mathrm{GeV} / c^{2}$. All the limits are at the $95 \%$ confidence level.


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[^0]
## 1 Introduction

The reaction $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ provides a clean test of QED at LEP energies and is well suited to detect the presence of non-standard physics. Previous letters from the DELPHI collaboration [1,2] reported on a study of this reaction at the $Z^{0}$ energies based on $36.9 \mathrm{pb}^{-1}$. Similar results were published by other LEP collaborations [3]. In this letter a measurement of the $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ cross-section is reported using $78.2 \mathrm{pb}^{-1}$ of data collected by DELPHI during the 1995, 1996 and 1997 runs at 130, 136, 161, 172 and 183 GeV centre-of-mass energies. These results are combined with the previously published results at the $Z^{0}$ pole [2] and are used to obtain limits on deviations from QED and to search for compositeness.

## 2 Apparatus

A detailed description of the DELPHI detector can be found in Ref.[4,5]. The present analysis was mainly based on the measurement of the electromagnetic energy clusters [6] in the barrel electromagnetic calorimeter, the High density Projection Chamber (HPC), and in the Forward ElectroMagnetic Calorimeter (FEMC) as well as on the capability of vetoing charged particles using the tracking devices. In addition to the track reconstruction in the Time Projection Chamber (TPC), Inner Detector (ID) and Outer Detector (OD), a very efficient way of rejecting final states which include charged particles was to use hits reconstructed in the Vertex Detector (VD).

The Vertex Detector [2] was upgraded in 1994 by introducing a double coordinate measurement in the layer closest to $(6.5 \mathrm{~cm})$ and furthest from $(11 \mathrm{~cm})$ the interaction point [7]. In 1996 the detector was extended to cover the polar angle ( $\theta$ ) region ${ }^{1}$ between $25^{\circ}$ and $155^{\circ}$ and the double coordinate measurement was introduced in the central layer between $25^{\circ}$ and $45^{\circ}$ and between $135^{\circ}$ and $155^{\circ}$ [8]. Since 1994, a new electromagnetic calorimeter (STIC) was used to measure the luminosity.

The barrel and the forward electromagnetic energy trigger was based on data from the HPC and the FEMC, respectively. The HPC trigger consists of a 1st level trigger based on scintillator plates inserted into the calorimeter at the depth corresponding to the maximum development of electromagnetic showers. The barrel electromagnetic energy trigger then requires coincidence with a 2 nd level trigger based on the energy release on the calorimeter modules. The FEMC trigger simply rely on energy deposition on the lead-glass counters. A detailed description of the DELPHI trigger can be found in [5]. Because of the increased LEP luminosity and the correspondingly higher backgrounds, the trigger contained less redundancy than that used for the analysis on the $Z^{0}$ pole. The efficiency was therefore poorer and had to be measured as a function of the different running periods. The trigger efficiency for $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ was measured by noting how often the electromagnetic energy trigger was fired by $e^{+} e^{-}$final state events which had been triggered by an independent track trigger.

The results obtained are shown in Table 1. The low value measured in the 172 GeV run was due to a hardware failure in the second period of the 1996 data-taking. Compatible results were obtained from multi-photon final state events by looking at the correspondence between the trigger signal multiplicity and the number of detected photons.

[^1]| $\sqrt{s}$ <br> GeV | Barrel <br> Efficiency | Forward <br> Efficiency |
| :---: | :---: | :---: |
| 1995 data |  |  |
| 133.4 | $0.986_{-0.022}^{+0.011}$ | - |
| 1996 data |  |  |
| 161.5 | $0.956 \pm 0.013$ | $>0.995$ |
| 172.4 | $0.775 \pm 0.025$ | $>0.995$ |
| 1997 data |  |  |
| 182.7 | $0.990 \pm 0.005$ | $>0.995$ |

Table 1: Efficiency for the barrel and forward electromagnetic trigger as a function of the different running periods. The efficiency of two 1995 energy points is given at the mean centre-of-mass energy, weighted by the luminosity at each point.

## 3 Event selection and analysis

The data of 1995 were collected at two LEP centre-of-mass energies, 130.4 GeV and 136.3 GeV , the data of 1996 at 161.5 GeV and 172.4 GeV whereas the 1997 data-set was taken at the mean energy of 182.7 GeV . Requiring that the HPC, FEMC, TPC and VD were operational, the integrated luminosities at each energy point were $2.86 \mathrm{pb}^{-1}, 2.96$ $\mathrm{pb}^{-1} 9.58 \mathrm{pb}^{-1}, 9.80 \mathrm{pb}^{-1}$ and $52.99 \mathrm{pb}^{-1}$, respectively.

The analysis was similar to the one reported in [2]. Events with energetic clusters in the electromagnetic calorimeters were selected. Charged particle final states (mainly $e^{+} e^{-}$final state events) were rejected using a Vertex Detector track search which required that there were hits in at least two of the three VD layers, which were aligned with the mean beam crossing point. The use of the VD confined the analysis to the barrel region for the 1995 data, while the VD upgrade allowed the analysis to be extended into the forward region (corresponding to the FEMC acceptance) for data taken in 1996 and 1997. Although suppressing background, vetoing tracks using a VD track search also removed a small number of signal events where a photon converted into $e^{+} e^{-}$before or in the region of sensitivity of the Vertex Detector.

Charged particle final states were also rejected by looking for tracks (TK) in the other tracking devices. The redundancy of this search allowed the efficiency of the VD search to be measured, while also removing the small number of $e^{+} e^{-}$final state events with both VD tracks missing.

Events were selected as $\gamma \gamma(\gamma)$ candidates if they satisfied the following criteria : - at least two electromagnetic energy clusters with $0.219<E / \sqrt{s}<0.713 \mathrm{GeV}$;

- at least two electromagnetic energy clusters in the HPC, ( $42^{\circ}<\theta<88^{\circ}$ or $92^{\circ}<\theta<$ $\left.138^{\circ}\right)$ or in the FEMC ( $25^{\circ}<\theta<32.4^{\circ}$ or $147.6^{\circ}<\theta<155^{\circ}$ ) ;
- acollinearity between the two most energetic clusters smaller than $30^{\circ}$;
- no tracks reconstructed in the Vertex Detector associated to the HPC or FEMC clusters ( $\pm 2^{\circ}$ in the azimuthal angle $\phi$ );
- two hemispheres were defined by the direction of the most energetic cluster. In the barrel region, one hemisphere was required to have no TK with a momentum greater than $1 \mathrm{GeV} / \mathrm{c}$ which extrapolated to within 5 cm of the mean beam crossing point. In the forward region, the requirement was strengthened to suppress the larger $e^{+} e^{-}$ background further, by demanding that both hemispheres have no such TK.

The samples obtained after applying these requirements in the barrel (HPC) region are listed in Table 2 for the different years and LEP energies. Including the data reported in [2], a total of $803 \gamma \gamma(\gamma)$ events were obtained from the barrel region and 89 from the forward region. The ability of these selection criteria to separate $\gamma \gamma(\gamma)$ events from the $e^{+} e^{-}$background can be seen in Fig. 1 which shows the difference in azimuth ( $180^{\circ}-\Delta \phi$ ) between the two most energetic clusters ${ }^{2}$ for both types of events at 183 GeV centre-ofmass energy. The $\gamma \gamma(\gamma)$ events do not exhibit the effect of the magnetic field bending as $e^{+} e^{-}$final state events do.


Figure 1: Distribution of the difference $180^{\circ}-\Delta \phi$ between the two most energetic clusters for $e^{+} e^{-}$(white area) and $\gamma \gamma(\gamma)$ events (hatched area) at 183 GeV centre-of-mass energy. The difference in height between the two $e^{+} e^{-}$peaks reflects the physical for-ward-backward asymmetry of such events.

The energy sum of the two most energetic clusters, for the data taken at 183 GeV , is shown in Fig.2. It is compared with the same quantity obtained with a simulated sample of $\gamma \gamma(\gamma)$ events [9] processed through the DELPHI detector simulation [5] and the same analysis chain as the real data.

The cosine of the scattering angle is defined as $\cos \theta=\left|\frac{\cos \frac{1}{2}\left(\theta_{1}+\pi-\theta_{2}\right)}{\cos \frac{1}{2}\left(\theta_{1}-\pi+\theta_{2}\right)}\right|$ where $\theta_{1}$ and $\theta_{2}$ are the polar angles of the two most energetic photons. This definition has the advantage of not being sensitive to the collinear initial state radiation. The efficiency obtained with the selection criteria defined above was determined in different $\cos \theta$ intervals with the $\gamma \gamma(\gamma)$ Monte Carlo sample. The global efficiency for accepting $\gamma \gamma(\gamma)$ events, integrated over the whole barrel acceptance region, was $(89.4 \pm 2.5) \%$, where the error includes the Monte Carlo statistics, the error on the acceptance definition and the stability of the result with respect to variations on the energy and acceptance cuts. In $e^{+} e^{-}$final state events the efficiency of the calorimeter and VD selection can be measured directly on

[^2]

Figure 2: The energy sum of the two most energetic clusters for 183 GeV data (dots) and simulation (full line) events.
the data with an alternative selection based on TKs [5]. The efficiency was defined as the ratio between the number of the events selected with both the calorimetric and TK selection and the number of the events selected with the TK selection. This procedure can be repeated in simulated events and the efficiency obtained can be compared with the one obtained in the real data. The comparison allows the calorimeter and the VD response to be monitored since agreement is expected when both are working properly. For all the periods the agreement was good except for the 1997 run when the efficiency on the real data was lower by $(4.3 \pm 1.4) \%$. The difference was understood to be due to a loss caused by beam background tracks seen in VD and accidentally associated to the electromagnetic clusters. The correction was applied and its error included in the systematics. A similar procedure was applied to the forward region where the efficiency was calculated to be $(66.3 \pm 2.2) \%$.

The only expected background was the small fraction of $e^{+} e^{-}$final state events (or $\tau$ events with high electromagnetic energy) missing both sets of VD hits and at least one TK (or both TPC track elements in the forward region). It was evaluated by using events generated with the BABAMC Monte Carlo program[10] and was found to be negligible.

The total systematic error was obtained by summing in quadrature the uncertainties in the trigger (Table 1) and selection efficiency corrections, the $\pm 0.5 \%$ uncertainty in the luminosity measurement[11] and a $\pm 1 \%$ error assumed on the radiative corrections. It is shown in Table 2 for the different energy points. In all cases the statistical error dominates.

Table 2 summarises the integrated luminosities, the number of selected events and the corresponding cross-sections (in the angular range $42^{\circ}<\theta<138^{\circ}$ ) at each centre-of-mass energy. Table 3 summarises the number of events and the corresponding differential crosssection, corrected for the angular dependent detection and trigger efficiency, as a function

| $\sqrt{s}$ <br> $(\mathrm{GeV})$ | Int. L <br> $\left(\mathrm{pb}^{-1}\right)$ | $\mathrm{N} \gamma \gamma$ | $\sigma$ <br> $(\mathrm{pb})$ | $\sigma_{0}$ <br> $(\mathrm{pb})$ |
| :---: | ---: | ---: | :---: | :---: |
| 91.25 | 36.87 | 503 | $17.4 \pm 0.8 \pm 0.4$ | 18.3 |
| 130.4 | 2.86 | 23 | $10.5 \pm 2.2 \pm 0.4$ | 8.97 |
| 136.3 | 2.96 | 19 | $8.33 \pm 1.91 \pm 0.28$ | 8.21 |
| 161.5 | 9.58 | 44 | $5.76 \pm 0.87 \pm 0.20$ | 5.85 |
| 172.4 | 9.80 | 35 | $5.55 \pm 0.94 \pm 0.24$ | 5.13 |
| 182.7 | 52.99 | 179 | $4.27 \pm 0.35 \pm 0.14$ | 4.57 |

Table 2: The integrated luminosities, the number of detected events ( $\mathrm{N} \gamma \gamma$ ), the measured cross-sections ( $\sigma$ ) and the lowest order $e^{+} e^{-} \rightarrow \gamma \gamma$ QED predictions ( $\sigma_{0}$ ) at different cen-tre-of-mass energies. The first error is statistical, the second corresponds to the total systematic error. The cross-section of the previously published data [2] is given at the mean of the centre-of-mass energies weighted by the luminosity at each point. The cross-sections correspond to the angular range $42^{\circ}<\theta<138^{\circ}$; the measured cross-sections have been corrected for radiative effects.
of $\cos \theta$. The experimental efficiency was obtained for the $\gamma \gamma(\gamma)$ events which passed the acceptance and acollinearity cuts at the generator level. The measured cross-sections reported in both tables were obtained after subtracting the radiative corrections ${ }^{3}$ to the order $\alpha^{3}$ so that they should correspond to the lowest order QED values. The lowest order QED values are included for comparison. The systematics on the cross sections of Table 3 are assumed to contribute as overall normalization errors of $3.4 \%, 3.4 \%, 4.4 \%$ and $3.3 \%$ for the four data sets.

## 4 Test of QED

The measured total and differential cross-sections after subtracting radiative corrections are shown in figures 3 and 4 respectively, together with the lowest order QED predictions. Only statistical errors are shown.

Possible deviations from QED are usually parametrised by adding to the QED differential cross-section a term depending on the cutoff parameters $\Lambda_{+}$or $\Lambda_{-}[13,14]$ :

$$
\begin{equation*}
\frac{d \sigma}{d \Omega}=\frac{\alpha^{2}}{s} \frac{1+\cos ^{2} \theta}{1-\cos ^{2} \theta}\left(1 \pm \frac{s^{2}}{2 \Lambda_{ \pm}^{4}}\left(1-\cos ^{2} \theta\right)\right) \tag{1}
\end{equation*}
$$

A maximum likelihood fit of expression (1) to the measured differential cross-sections at all the energies gave, for the parameter $\eta=1 / \Lambda^{4}$, a central value $\eta=(-1.4 \pm 1.5) \times$ $10^{-10} \mathrm{GeV}^{-4}$. This corresponds to lower limits at the $95 \%$ confidence level of $\Lambda_{+}>253$ GeV and $\Lambda_{-}>225 \mathrm{GeV}$. These are represented as the dashed and dotted lines in figure 4. The overall normalisation errors were taken into account in the fitting procedure and their contribution to the total error on $\eta$ is $\pm 0.6 \times 10^{-10} \mathrm{GeV}^{-4}$. The published 1990-1992 DELPHI results [2] were also included in the fit. However, given the $s^{2}$ dependence of the non-QED term in eq.(1), the contribution of the $Z^{0}$ data was quite negligible; if these data are removed from the fit the limits are $\Lambda_{+}>250 \mathrm{GeV}$ and $\Lambda_{-}>225 \mathrm{GeV}$ and if

[^3]

Figure 3: Total cross-section (in pb ) for the process $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ in the region $42^{\circ}<\theta<138^{\circ}$, as a function of the mean centre-of-mass energy for 1990-1992 data (black dot), weighted by the luminosity at each point, and for the 1995-97 data (white dots). The solid line is the lowest order QED prediction.
the full statistical sample at the $Z^{0}$ would be included the expected improvement on the error on $\eta$ is smaller than $3.5 \%$.

For these and the following limits, the confidence level was obtained by normalising the probability to the integral over the region of definition of the parameters, as explained in Ref.[15]. The central values and their errors are quoted in order to allow them to be combined with the results of other experiments and to permit the evaluation of the confidence level by alternative methods[16]. The $\chi^{2}$ of the data points with respect to the pure QED predictions is $\chi^{2}=27.3$ with 31 degrees of freedom.

## 5 Search for compositeness

The exchange of a virtual excited electron would modify the differential QED crosssection [13]. A likelihood fit was performed to the following expression, as a function of the excited electron mass ( $M_{e^{*}}$ ) and the coupling constant $\left(\lambda_{\gamma}\right)$ :

$$
\begin{equation*}
\frac{d \sigma}{d \Omega}=\frac{\alpha^{2}}{s} \frac{1+\cos ^{2} \theta}{1-\cos ^{2} \theta}\left(1+\frac{s^{2} \lambda_{\gamma}^{2}}{2 M_{e^{*}}^{4}}\left(1-\cos ^{2} \theta\right) H\left(\cos ^{2} \theta\right)\right) \tag{2}
\end{equation*}
$$

where $H\left(\cos ^{2} \theta\right)=a \frac{a+\left(1-\cos ^{2} \theta\right) /\left(1+\cos ^{2} \theta\right)}{(1+a)^{2}-\cos ^{2} \theta}$ and $a=2 M_{e^{*}}^{2} / s$. The fit was done over all data samples. Fig. 5 shows the resulting $95 \%$ confidence level limit on the ( $M_{e^{*}}, \lambda_{\gamma} / M_{e^{*}}$ ) plane. In the mass region below $161 \mathrm{GeV} / \mathrm{c}^{2}$ a better limit was obtained from the DELPHI search for t-channel production of $e^{*} e[17]$. For $\lambda_{\gamma}=1$, the limit is $M_{e^{*}}>231 \mathrm{GeV} / c^{2}$ at the $95 \%$ confidence level, with a central value $1 / M_{e^{*}}^{4}=(-1.9 \pm 2.2) \times 10^{-10}\left(\mathrm{GeV} / \mathrm{c}^{2}\right)^{-4}$.

## 6 Conclusions

The measured $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ cross-sections show good agreement with the QED predictions. Lower bounds were obtained on the QED cutoff parameters, $\Lambda_{+}>253$ GeV and $\Lambda_{-}>225 \mathrm{GeV}$ as well as on the mass of an excited electron: $M_{e^{*}}>231$ $\mathrm{GeV} / c^{2}$ for $\lambda_{\gamma}=1$. All the limits are at the $95 \%$ confidence level and are higher than the existing published results at lower energies [3].

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| $\cos \theta$ | $\begin{array}{\|l\|} \hline d \sigma_{0} / d \Omega \\ (\mathrm{pb} / \mathrm{sr}) \end{array}$ | $\begin{aligned} & d \sigma / d \Omega \\ & (\mathrm{pb} / \mathrm{sr}) \end{aligned}$ | Number of events |
| :---: | :---: | :---: | :---: |
| 133 GeV |  |  |  |
| 0.035-0.136 | 1.18 | $2.05_{-0.74}^{+0.97}$ | 6 |
| 0.136-0.237 | 1.25 | $1.57_{-0.61}^{+0.83}$ | 5 |
| 0.237-0.338 | 1.38 | $0.911_{-0.44}^{+0.65}$ | 3 |
| 0.338-0.440 | 1.58 | $1.26_{-0.54}^{+0.75}$ | 4 |
| 0.440-0.541 | 1.90 | $1.79_{-0.64}^{+0.85}$ | 6 |
| 0.541-0.642 | 2.42 | $1.85_{-0.67}^{+0.88}$ | 6 |
| 0.642-0.743 | 3.31 | $3.88{ }_{-1.06}^{+1.30}$ | 11 |
| 161 GeV |  |  |  |
| 0.035-0.136 | 0.81 | $0.21_{-0.16}^{+0.32}$ | 1 |
| 0.136-0.237 | 0.85 | $0.800_{-0.34}^{+0.48}$ | 4 |
| 0.237-0.338 | 0.94 | $1.73_{-0.52}^{+0.65}$ | 9 |
| 0.338-0.440 | 1.08 | $0.99_{-0.38}^{+0.52}$ | 5 |
| 0.440-0.541 | 1.30 | $1.699_{-0.51}^{+0.64}$ | 9 |
| 0.541-0.642 | 1.65 | $1.16_{-0.42}^{+0.55}$ | 6 |
| 0.642-0.743 | 2.26 | $2.23_{-0.64}^{+0.79}$ | 10 |
| 0.844-0.906 | 6.00 | $8.93_{-1.90}^{+2.22}$ | 19 |
| 172 GeV |  |  |  |
| 0.035-0.136 | 0.71 | $0.52_{-0.29}^{+0.48}$ | 2 |
| 0.136-0.237 | 0.75 | $1.200_{-0.47}^{+0.63}$ | 5 |
| 0.237-0.338 | 0.82 | $0.93_{-0.40}^{+0.56}$ | 4 |
| 0.338-0.440 | 0.95 | $0.47_{-0.27}^{+0.44}$ | 2 |
| 0.440-0.541 | 1.14 | $1.36_{-0.49}^{+0.65}$ | 6 |
| 0.541-0.642 | 1.45 | $1.63_{-0.55}^{+0.70}$ | 7 |
| 0.642-0.743 | 1.98 | $2.42_{-0.73}^{+0.91}$ | 9 |
| 0.844-0.906 | 5.27 | $5.05_{-1.38}^{+1.70}$ | 11 |
| 183 GeV |  |  |  |
| 0.035-0.136 | 0.63 | $0.49_{-0.13}^{+0.15}$ | 13 |
| 0.136-0.237 | 0.67 | $0.84_{-0.16}^{+0.19}$ | 23 |
| 0.237-0.338 | 0.73 | $0.600_{-0.13}^{+0.15}$ | 18 |
| 0.338-0.440 | 0.84 | $0.500_{-0.13}^{+0.16}$ | 12 |
| 0.440-0.541 | 1.01 | $0.76_{-0.15}^{+0.17}$ | 23 |
| 0.541-0.642 | 1.29 | $1.25_{-0.20}^{+0.22}$ | 35 |
| 0.642-0.743 | 1.77 | $2.05_{-0.27}^{+0.29}$ | 53 |
| 0.844-0.906 | 4.69 | $5.144_{-0.64}^{+0.70}$ | 59 |

Table 3: The lowest order $e^{+} e^{-} \rightarrow \gamma \gamma$ QED predictions ( $d \sigma_{0} / d \Omega$ ), the measured differential cross-sections ( $d \sigma / d \Omega$ ) and the number of detected events for different $\cos \theta$ regions. The quoted errors are statistical only computed following the Bayesian approach (minimal interval) for small number of events [12]. The measured cross-sections were corrected for radiative effects. The systematics is assumed to contribute as an overall normalization error being $3.4 \%, 3.4 \%, 4.4 \%$ and $3.3 \%$ for the four data sets, respectively


Figure 4: Differential cross-section, $d \sigma / d \Omega$, for the process $e^{+} e^{-} \rightarrow \gamma \gamma(\gamma)$ at the cen-tre-of-mass energies of 133.3 GeV (mean of the 1995130.4 GeV and 136.3 GeV points), $161.5 \mathrm{GeV}, 172.4$ and 182.7 GeV . The solid curves show the lowest order QED prediction. The dashed (dotted) curves show the derived limit on the prediction parametrised by $\Lambda_{+}$ ( $\Lambda_{-}$).


Figure 5: Upper limit on the effective coupling constant $\lambda_{\gamma} / M_{e^{*}}$ versus $M_{e^{*}}$. For $M_{e^{*}}<161 \mathrm{GeV} / c^{2}$ a better limit was obtained by a direct search[17].


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[^1]:    ${ }^{1}$ The DELPHI coordinate system is Cartesian with the z axis along the electron direction, the x axis pointing towards the LEP centre and the $y$ axis pointing upwards. The polar angle $\theta=t g^{-1}\left(\sqrt{x^{2}+y^{2}} / z\right)$ and the azimuthal angle $\phi=t g^{-1}(y / x)$.

[^2]:    ${ }^{2}$ The quantity $180^{\circ}-\Delta \phi$ is defined as $\phi_{+}-\phi_{-}-180 \cdot \operatorname{sign}\left(\phi_{+}-\phi_{-}\right)$where $\phi_{+}\left(\phi_{-}\right)$refers to the azimuth of the cluster with the larger (smaller) z coordinate.

[^3]:    ${ }^{3}$ The radiative corrections are obtained as the difference between the cross-section of simulated $\gamma \gamma(\gamma)$ events [9] inside the acceptance and the lowest order QED prediction.

