# Measurement and interpretation of the W-pair cross-section in $e^{+} e^{-}$interactions at 161 GeV 

P. Abreu, W. Adam, T. Adye, P. Adzic, I. Ajinenko, G D. Alekseev, R.

Alemany, P P. Allport, S. Almehed, U. Amaldi, et al.

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## EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

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# Measurement and interpretation of the W-pair cross-section in $\mathrm{e}^{+} \mathrm{e}^{-}$interactions at $161 \mathbf{G e V}$ 

DELPHI Collaboration


#### Abstract

In 1996 LEP ran at a centre-of-mass energy of 161 GeV , just above the threshold of W-pair production. DELPHI accumulated data corresponding to an integrated luminosity of $9.93 \mathrm{pb}^{-1}$, and observed 29 events that are considered as candidates for W-pair production. From these, a cross-section for the doubly resonant $e^{+} e^{-} \rightarrow \mathrm{WW}$ process of $3.67{ }_{-0.85}^{+0.97} \pm 0.19 \mathrm{pb}$ has been measured. Within the Standard Model, this cross-section corresponds to a mass of the Wboson of $80.40 \pm 0.44$ (stat.) $\pm 0.09$ (syst.) $\pm 0.03$ (LEP) $\mathrm{GeV} / c^{2}$. Alternatively, if $m_{\mathrm{W}}$ is held fixed at its current value determined by other experiments, the observed cross-section is used to obtain limits on trilinear WWV (V $\equiv \gamma, \mathrm{Z})$ couplings.


P.Abreu ${ }^{21}$, W.Adam ${ }^{50}$, T.Adye $^{37}$, P.Adzic ${ }^{11}$, I.Ajinenko ${ }^{42}$, G.D.Alekseev ${ }^{16}$, R.Alemany ${ }^{49}$, P.P.Allport ${ }^{22}$, S.Almehed ${ }^{24}$, U.Amaldi ${ }^{9}$, S.Amato ${ }^{47}$, A.Andreazza ${ }^{28}$, M.L.Andrieux ${ }^{14}$, P.Antilogus ${ }^{9}$, W-D.Apel ${ }^{17}$, B.Åsman ${ }^{44}$, J-E.Augustin ${ }^{25}$, A.Augustinus ${ }^{31}$, P.Baillon ${ }^{9}$, P.Bambade ${ }^{19}$, F.Barao ${ }^{21}$, M.Barbi ${ }^{47}$, D.Y.Bardin ${ }^{16}$, G.Barker ${ }^{9}$, A.Baroncelli ${ }^{40}$, O.Barring ${ }^{24}$, J.A.Barrio ${ }^{26}$, W.Bartl ${ }^{50}$, M.J.Bates ${ }^{37}$, M.Battaglia ${ }^{15}$, M.Baubillier ${ }^{23}$, J.Baudot ${ }^{39}$, K-H.Becks ${ }^{52}$, M.Begalli ${ }^{6}$, P.Beilliere ${ }^{8}$, Yu.Belokopytov ${ }^{9,53}$, K.Belous ${ }^{42}$, A.C.Benvenuti ${ }^{5}$, M.Berggren ${ }^{47}$, D.Bertini ${ }^{25}$, D.Bertrand ${ }^{2}$, M.Besancon ${ }^{39}$, F.Bianchi ${ }^{45}$, M.Bigi ${ }^{45}$, M.S.Bilenky ${ }^{16}$, P.Billoir ${ }^{23}$, M-A.Bizouard ${ }^{19}$, D.Bloch ${ }^{10}$, M.Blume ${ }^{52}$, T.Bolognese ${ }^{39}$, M.Bonesini ${ }^{28}$, W.Bonivento ${ }^{28}$, P.S.L.Booth ${ }^{22}$, C.Bosio ${ }^{40}$, O.Botner ${ }^{48}$, E.Boudinov ${ }^{31}$, B.Bouquet ${ }^{19}$, C.Bourdarios ${ }^{19}$, T.J.V.Bowcock ${ }^{22}$, M.Bozzo ${ }^{13}$, P.Branchini ${ }^{40}$, K.D.Brand ${ }^{36}$, T.Brenke ${ }^{52}$, R.A.Brenner ${ }^{15}$, C.Bricman ${ }^{2}$, R.C.A.Brown ${ }^{9}$, P.Bruckman ${ }^{18}$, J-M.Brunet ${ }^{8}$, L.Bugge ${ }^{33}$, T.Buran ${ }^{33}$, T.Burgsmueller ${ }^{52}$, P.Buschmann ${ }^{52}$, S.Cabrera ${ }^{49}$, M.Caccia ${ }^{28}$, M.Calvi ${ }^{28}$, A.J.Camacho Rozas ${ }^{41}$, T.Camporesi ${ }^{9}$, V.Canale ${ }^{38}$, M.Canepa ${ }^{13}$, K.Cankocak ${ }^{44}$, F.Cao ${ }^{2}$, F.Carena ${ }^{9}$, L.Carroll ${ }^{22}$, C.Caso ${ }^{13}$, M.V.Castillo Gimenez ${ }^{49}$, A.Cattai ${ }^{9}$, F.R.Cavallo ${ }^{5}$, V.Chabaud ${ }^{9}$, Ph.Charpentier ${ }^{9}$, L.Chaussard ${ }^{25}$, P.Checchia ${ }^{36}$, G.A.Chelkov ${ }^{16}$, M.Chen ${ }^{2}$, R.Chierici ${ }^{45}$, P.Chliapnikov ${ }^{42}$, P.Chochula ${ }^{7}$, V.Chorowicz ${ }^{25}$, J.Chudoba ${ }^{30}$, V.Cindro ${ }^{43}$, P.Collins ${ }^{9}$, R.Contri ${ }^{13}$, E.Cortina ${ }^{49}$, G.Cosme ${ }^{19}$, F.Cossutti ${ }^{46}$, J-H.Cowell ${ }^{22}$, H.B.Crawley ${ }^{1}$, D.Crennell ${ }^{37}$, G.Crosetti ${ }^{13}$, J.Cuevas Maestro ${ }^{34}$, S.Czellar ${ }^{15}$, E.Dahl-Jensen ${ }^{29}$, J.Dahm ${ }^{52}$, B.Dalmagne ${ }^{19}$, M.Dam ${ }^{29}$, G.Damgaard ${ }^{29}$, P.D.Dauncey ${ }^{37}$, M.Davenport ${ }^{9}$, W.Da Silva ${ }^{23}$, C.Defoix ${ }^{8}$, A.Deghorain ${ }^{2}$, G.Della Ricca ${ }^{46}$, P.Delpierre ${ }^{27}$, N.Demaria ${ }^{35}$, A.De Angelis ${ }^{9}$, W.De Boer ${ }^{17}$, S.De Brabandere ${ }^{2}$, C.De Clercq ${ }^{2}$, C.De La Vaissiere ${ }^{23}$, B.De Lotto ${ }^{46}$, A.De Min ${ }^{36}$, L.De Paula ${ }^{47}$, C.De Saint-Jean ${ }^{39}$, H.Dijkstra ${ }^{9}$, L.Di Ciaccio ${ }^{38}$, A.Di Diodato ${ }^{38}$, A.Djannati ${ }^{8}$, J.Dolbeau ${ }^{8}$, K.Doroba ${ }^{51}$, M.Dracos ${ }^{10}$, J.Drees ${ }^{52}$, K.-A.Drees ${ }^{52}$, M.Dris ${ }^{32}$, J-D.Durand ${ }^{25,9}$, D.Edsall ${ }^{1}$, R.Ehret ${ }^{17}$, G.Eigen ${ }^{4}$, T.Ekelof ${ }^{48}$, G.Ekspong ${ }^{44}$, M.Elsing ${ }^{9}$, J-P.Engel ${ }^{10}$, B.Erzen ${ }^{43}$, E.Falk ${ }^{24}$, G.Fanourakis ${ }^{11}$, D.Fassouliotis ${ }^{46}$, M.Feindt ${ }^{9}$, P.Ferrari ${ }^{28}$, A.Ferrer ${ }^{49}$, S.Fichet ${ }^{23}$, T.A.Filippas ${ }^{32}$, A.Firestone ${ }^{1}$, P.-A.Fischer ${ }^{10}$, H.Foeth ${ }^{9}$, E.Fokitis ${ }^{32}$, F.Fontanelli ${ }^{13}$, F.Formenti ${ }^{9}$, B.Franek ${ }^{37}$, P.Frenkiel ${ }^{8}$, A.G.Frodesen ${ }^{4}$, R.Fruhwirth ${ }^{50}$, F.Fulda-Quenzer ${ }^{19}$, J.Fuster ${ }^{49}$, A.Galloni ${ }^{22}$, D.Gamba ${ }^{45}$, M.Gandelman ${ }^{47}$, C.Garcia ${ }^{49}$, J.Garcia ${ }^{41}$, C.Gaspar ${ }^{9}$, U.Gasparini ${ }^{36}$, Ph.Gavillet $^{9}$, E.N.Gazis ${ }^{32}$, D.Gele ${ }^{10}$, J-P.Gerber ${ }^{10}$, L.Gerdyukov ${ }^{42}$, R.Gokieli ${ }^{51}$, B.Golob ${ }^{43}$, P.Goncalves ${ }^{21}$, G.Gopal ${ }^{37}$, L.Gorn ${ }^{1}$, M.Gorski ${ }^{51}$, Yu.Gouz ${ }^{45,53}$, V.Gracco ${ }^{13}$, E.Graziani ${ }^{40}$, C.Green ${ }^{22}$, A.Grefrath ${ }^{52}$, P.Gris ${ }^{39}$, G.Grosdidier ${ }^{19}$, K.Grzelak ${ }^{51}$, S.Gumenyuk ${ }^{42}$, P.Gunnarsson ${ }^{44}$, M.Gunther ${ }^{48}$, J.Guy ${ }^{37}$, F.Hahn ${ }^{9}$, S.Hahn ${ }^{52}$, Z.Hajduk ${ }^{18}$, A.Hallgren ${ }^{48}$, K.Hamacher ${ }^{52}$, F.J.Harris ${ }^{35}$, V.Hedberg ${ }^{24}$, R.Henriques ${ }^{21}$, J.J.Hernandez ${ }^{49}$, P.Herquet ${ }^{2}$, H.Herr ${ }^{9}$, T.L.Hessing ${ }^{35}$, J.-M.Heuser ${ }^{52}$, E.Higon ${ }^{49}$, H.J.Hilke ${ }^{9}$, T.S.Hill ${ }^{1}$, S-O.Holmgren ${ }^{44}$, P.J.Holt ${ }^{35}$, D.Holthuizen ${ }^{31}$, S.Hoorelbeke ${ }^{2}$, M.Houlden ${ }^{22}$, J.Hrubec ${ }^{50}$, K.Huet ${ }^{2}$, K.Hultqvist ${ }^{44}$, J.N.Jackson ${ }^{22}$, R.Jacobsson ${ }^{44}$, P.Jalocha ${ }^{18}$, R.Janik ${ }^{7}$, Ch.Jarlskog ${ }^{24}$, G.Jarlskog ${ }^{24}$, P.Jarry ${ }^{39}$, B.Jean-Marie ${ }^{19}$, E.K.Johansson ${ }^{44}$, L.Jonsson ${ }^{24}$, P.Jonsson ${ }^{24}$, C.Joram ${ }^{9}$, P.Juillot ${ }^{10}$, M.Kaiser ${ }^{17}$, F.Kapusta ${ }^{23}$, K.Karafasoulis ${ }^{11}$, M.Karlsson ${ }^{44}$, S.Katsanevas ${ }^{25}$, E.C.Katsoufis ${ }^{32}$, R.Keranen ${ }^{4}$, Yu.Khokhlov ${ }^{42}$, B.A.Khomenko ${ }^{16}$, N.N.Khovanski ${ }^{16}$, B.King ${ }^{22}$, N.J.Kjaer ${ }^{31}$, O.Klapp ${ }^{52}$, H.Klein ${ }^{9}$, A.Klovning ${ }^{4}$, P.Kluit ${ }^{31}$, D.Knoblauch ${ }^{17}$, P.Kokkinias ${ }^{11}$, A.Konopliannikov ${ }^{42}$, M.Koratzinos ${ }^{9}$, K.Korcyl ${ }^{18}$, V.Kostioukhine ${ }^{42}$, C.Kourkoumelis ${ }^{3}$, O.Kouznetsov ${ }^{13,16}$, M.Krammer ${ }^{50}$, C.Kreuter $^{9}$, I.Kronkvist ${ }^{24}$, Z.Krumstein ${ }^{16}$, W.Krupinski ${ }^{18}$, P.Kubinec ${ }^{7}$, W.Kucewicz ${ }^{18}$, K.Kurvinen ${ }^{15}$, C.Lacasta ${ }^{49}$, I.Laktineh ${ }^{25}$, J.W.Lamsa ${ }^{1}$, L.Lanceri ${ }^{46}$, D.W.Lane ${ }^{1}$, P.Langefeld ${ }^{52}$, J-P.Laugier ${ }^{39}$, R.Lauhakangas ${ }^{15}$, G.Leder ${ }^{50}$, F.Ledroit ${ }^{14}$, V.Lefebure ${ }^{2}$, C.K.Legan ${ }^{1}$, A.Leisos ${ }^{11}$, R.Leitner ${ }^{30}$, J.Lemonne ${ }^{2}$, G.Lenzen ${ }^{52}$, V.Lepeltier ${ }^{19}$, T.Lesiak ${ }^{18}$, J.Libby ${ }^{35}$, D.Liko ${ }^{9}$, R.Lindner ${ }^{52}$, A.Lipniacka ${ }^{44}$, I.Lippi ${ }^{36}$, B.Loerstad ${ }^{24}$, J.G.Loken ${ }^{35}$, J.M.Lopez ${ }^{41}$, D.Loukas ${ }^{11}$, P.Lutz ${ }^{39}$, L.Lyons ${ }^{35}$, J.MacNaughton ${ }^{50}$, G.Maehlum ${ }^{17}$, J.R.Mahon ${ }^{6}$, A.Maio ${ }^{21}$, T.G.M.Malmgren ${ }^{44}$, V.Malycher ${ }^{16}$, J.Marco ${ }^{41}$, R.Marco ${ }^{41}$, B.Marechal ${ }^{47}$, M.Margoni ${ }^{36}$, J-C.Marin ${ }^{9}$, C.Mariotti ${ }^{9}$, A.Markou ${ 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V.Nikolaenko ${ }^{10}$, P.Niss ${ }^{44}$, A.Nomerotski ${ }^{36}$, A.Normand ${ }^{35}$, W.Oberschulte-Beckmann ${ }^{17}$, V.Obraztsov ${ }^{42}$, A.G.Olshevski ${ }^{16}$, A.Onofre ${ }^{21}$, R.Orava ${ }^{15}$, G.Orazi ${ }^{10}$, K.Osterberg ${ }^{15}$, A.Ouraou ${ }^{39}$, P.Paganini ${ }^{19}$, M.Paganoni ${ }^{9,28}$, P.Pages ${ }^{10}$, R.Pain ${ }^{23}$, H.Palka ${ }^{18}$, Th.D.Papadopoulou ${ }^{32}$, K.Papageorgiou ${ }^{11}$, L.Pape ${ }^{9}$, C.Parkes ${ }^{35}$, F.Parodi ${ }^{13}$, A.Passeri ${ }^{40}$, M.Pegoraro ${ }^{36}$, L.Peralta ${ }^{21}$, H.Pernegger ${ }^{50}$, M.Pernicka ${ }^{50}$, A.Perrotta ${ }^{5}$, C.Petridou ${ }^{46}$, A.Petrolini ${ }^{13}$, H.T.Phillips ${ }^{37}$, G.Piana ${ }^{13}$, F.Pierre ${ }^{39}$, M.Pimenta ${ }^{21}$, T.Podobnik ${ }^{43}$, O.Podobrin ${ }^{9}$, M.E.Pol ${ }^{6}$, G.Polok ${ }^{18}$, P.Poropat ${ }^{46}$, V.Pozdniakov ${ }^{16}$, P.Privitera $^{38}$, N.Pukhaeva ${ }^{16}$, A.Pullia ${ }^{28}$, D.Radojicic ${ }^{35}$, S.Ragazzi ${ }^{28}$, H.Rahmani ${ }^{32}$, J.Rames ${ }^{12}$, P.N.Ratoff ${ }^{20}$, A.L.Read ${ }^{33}$, M.Reale ${ }^{52}$, P.Rebecchi ${ }^{19}$, N.G.Redaelli ${ }^{28}$, M.Regler ${ }^{50}$, D.Reid ${ }^{9}$, R.Reinhardt ${ }^{52}$, P.B.Renton ${ }^{35}$, L.K.Resvanis ${ }^{3}$, F.Richard ${ }^{19}$, J.Richardson ${ }^{22}$, J.Ridky ${ }^{12}$, G.Rinaudo ${ }^{45}$, I.Ripp ${ }^{39}$, A.Romero ${ }^{45}$, I.Roncagliolo ${ }^{13}$, P.Ronchese ${ }^{36}$, L.Roos ${ }^{23}$, E.I.Rosenberg ${ }^{1}$, P.Roudeau ${ }^{19}$, T.Rovelli ${ }^{5}$, V.Ruhlmann-Kleider ${ }^{39}$, A.Ruiz ${ }^{41}$, K.Rybicki ${ }^{18}$, H.Saarikko ${ }^{15}$, Y.Sacquin ${ }^{39}$, A.Sadovsky ${ }^{16}$, O.Sahr ${ }^{14}$, G.Sajot ${ }^{14}$, J.Salt ${ }^{49}$, J.Sanchez ${ }^{26}$, M.Sannino ${ }^{13}$, H.Schneider ${ }^{17}$, U.Schwickerath ${ }^{17}$, M.A.E.Schyns ${ }^{52}$, G.Sciolla ${ }^{45}$, F.Scuri ${ }^{46}$, P.Seager ${ }^{20}$, Y.Sedykh ${ }^{16}$, A.M.Segar ${ }^{35}$, A.Seitz ${ }^{17}$, R.Sekulin ${ }^{37}$, L.Serbelloni ${ }^{38}$, R.C.Shellard ${ }^{6}$, P.Siegrist ${ }^{9,39}$, R.Silvestre ${ }^{39}$, S.Simonetti ${ }^{39}$, F.Simonetto ${ }^{36}$, A.N.Sisakian ${ }^{16}$, B.Sitar ${ }^{7}$, T.B.Skaali ${ }^{33}$, G.Smadja ${ }^{25}$, N.Smirnov ${ }^{42}$, O.Smirnova ${ }^{24}$, G.R.Smith ${ }^{37}$, A.Sokolov ${ }^{42}$, O.Solovianov ${ }^{42}$, R.Sosnowski ${ }^{51}$, D.Souza-Santos ${ }^{6}$, T.Spassov ${ }^{21}$, E.Spiriti ${ }^{40}$, P.Sponholz ${ }^{52}$, S.Squarcia ${ }^{13}$, D.Stampfer ${ }^{9}$, C.Stanescu ${ }^{40}$, S.Stanic ${ }^{43}$, S.Stapnes ${ }^{33}$, I.Stavitski ${ }^{36}$, K.Stevenson ${ }^{35}$, A.Stocchi ${ }^{19}$, J.Strauss ${ }^{50}$, R.Strub ${ }^{10}$, B.Stugu ${ }^{4}$, M.Szczekowski ${ }^{51}$, M.Szeptycka ${ }^{51}$, T.Tabarelli ${ }^{28}$,
J.P.Tavernet ${ }^{23}$, F.Terranova ${ }^{28}$, J.Thomas ${ }^{35}$, A.Tilquin ${ }^{27}$, J.Timmermans ${ }^{31}$, L.G.Tkatchev ${ }^{16}$, T.Todorov ${ }^{10}$, S.Todorova ${ }^{10}$, D.Z.Toet ${ }^{31}$, A.Tomaradze ${ }^{2}$, B.Tome ${ }^{21}$, A.Tonazzo ${ }^{28}$, L.Tortora ${ }^{40}$, G.Transtromer ${ }^{24}$, D.Treille ${ }^{9}$, G.Tristram ${ }^{8}$, A.Trombini ${ }^{19}$, C.Troncon ${ }^{28}$, A.Tsirou ${ }^{9}$, M-L.Turluer ${ }^{39}$, I.A.Tyapkin ${ }^{16}$, M.Tyndel ${ }^{37}$, S.Tzamarias ${ }^{11}$, B.Ueberschaer ${ }^{52}$, O.Ullaland ${ }^{9}$, V.Uvarov ${ }^{42}$, G.Valenti ${ }^{5}$, E.Vallazza ${ }^{9}$, C.Vander Velde ${ }^{2}$, G.W.Van Apeldoorn ${ }^{31}$, P.Van Dam ${ }^{31}$, W.K.Van Doninck ${ }^{2}$, J.Van Eldik ${ }^{31}$, A.Van Lysebetten ${ }^{2}$, N.Vassilopoulos ${ }^{35}$, G.Vegni ${ }^{28}$, L.Ventura ${ }^{36}$, W.Venus ${ }^{37}$, F.Verbeure ${ }^{2}$, M.Verlato ${ }^{36}$, L.S.Vertogradov ${ }^{16}$, D.Vilanova ${ }^{39}$, P.Vincent ${ }^{25}$, L.Vitale ${ }^{46}$, E.Vlasov ${ }^{42}$, A.S.Vodopyanov ${ }^{16}$, V.Vrba ${ }^{12}$, H.Wahlen ${ }^{52}$, C.Walck ${ }^{44}$, F.Waldner ${ }^{46}$, P.Weilhammer ${ }^{9}$, C.Weiser ${ }^{17}$, A.M.Wetherell ${ }^{9}$, D.Wicke ${ }^{52}$, J.H.Wickens ${ }^{2}$, M.Wielers ${ }^{17}$, G.R.Wilkinson ${ }^{9}$, W.S.C.Williams ${ }^{35}$, M.Winter ${ }^{10}$, M.Witek ${ }^{18}$, T.Wlodek ${ }^{19}$, K.Woschnagg ${ }^{48}$, K.Yip ${ }^{35}$, O.Yushchenko ${ }^{42}$, F.Zach ${ }^{25}$, A.Zaitsev ${ }^{42}$, A.Zalewska ${ }^{9}$, P.Zalewski ${ }^{51}$, D.Zavrtanik ${ }^{43}$, E.Zevgolatakos ${ }^{11}$, N.I.Zimin ${ }^{16}$, M.Zito ${ }^{39}$, D.Zontar ${ }^{43}$, G.C.Zucchelli ${ }^{44}$, G.Zumerle ${ }^{36}$

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## 1 Introduction

The W -boson mass, $m_{\mathrm{W}}$, is one of the key parameters of the electroweak theory. The combined measurements at $\mathrm{p} \overline{\mathrm{p}}$ colliders give a value $m_{\mathrm{W}}=80.35 \pm 0.13 \mathrm{GeV} / c^{2}[1-5]$. This is in agreement with the determination $m_{\mathrm{W}}=80.352 \pm 0.033 \mathrm{GeV} / c^{2}$ from a fit of all electroweak data to the Standard Model [6].

In 1996, LEP provided $\mathrm{e}^{+} \mathrm{e}^{-}$collisions at a centre-of-mass energy of 161.31 GeV with an integrated luminosity recorded by DELPHI of $9.93 \mathrm{pb}^{-1}$, from which a measurement of the W -pair cross-section has been obtained. The cross-section for W -pair production near threshold depends strongly on $m_{\mathrm{W}}$, which can therefore be determined from this measurement. It is also sensitive to the trilinear gauge coupling parameters (TGCs) at the WWV (i.e. WW $\gamma$ and WWZ) vertices, and can therefore be used to set limits on these parameters if another measurement of $m_{\mathrm{W}}$ is used. Limits on TGCs have previously been obtained in $\mathrm{p} \overline{\mathrm{p}}$ experiments [7].

The paper is organized as follows. In section 2, the DELPHI detector setup in 1996, the event trigger, and the luminosity measurement are briefly reviewed. The track selection and lepton identification are described in section 3. In section 4, the event selection and the computation of cross-sections are presented for the different decay channels, from which a total cross-section is obtained. In section 5 , a value for $m_{\mathrm{W}}$ is derived. Limits on TGCs are given in section 6 .

## 2 Apparatus, Trigger and Luminosity

Detailed descriptions of the DELPHI apparatus and its performance can be found in [8,9]. In 1996 the cylindrical 3-layer vertex detector was lengthened and extended with additional silicon detectors covering the endcap region.

The response of the detector to various physics processes was modelled using the full simulation program DELSIM [9,10], which incorporates the resolution, granularity, and efficiency of the detector components. The event generators chosen are described in the relevant sections below.

The event trigger is described in [8,9]. From trigger efficiencies measured for single charged particles with redundant trigger combinations, the efficiency for two charged particles (which is the worst case for all events of interest in the present analysis) was found to exceed $99 \%$.

The luminosity was measured using the Small Angle Tile Calorimeter (STIC). It consists of two lead/scintillator sampling calorimeters, located at $\pm 220 \mathrm{~cm}$ from the interaction point, providing full coverage of the region between 29 and 185 mrad with respect to the beam axis. A detailed description of this detector can be found in [11]. Events corresponding to Bhabha scattering were selected by requiring a coincidence of two coplanar electromagnetic showers, each with energy larger than $65 \%$ of the beam energy. In order to minimize the sensitivity to the position of the interaction point, asymmetric cuts were imposed on the reconstructed radii of the two showers.

The calculation of the accepted cross-section was based on the event generator BHLUMI 4.03 [12], which has a theoretical accuracy of $0.25 \%$ at LEP2 energies. The generated events were passed through a full simulation of the detector, and analysed in the same way as the real data. The total experimental systematic error on the luminosity amounts to $0.5 \%$, with the main contribution arising from the uncertainty in the radial cuts. For the data sample used, an integrated luminosity of $9.93 \pm 0.11$ (stat.) $\pm 0.06$ (syst.) $\mathrm{pb}^{-1}$ was determined.

## 3 Track Selection and Lepton Identification

## Charged particles were selected if they fulfilled the following criteria:

- polar angle with respect to the beam direction between $10^{\circ}$ and $170^{\circ}$;
- momentum greater than $0.4 \mathrm{GeV} / c$;
- good quality, assessed as follows:
- track length greater than 15 cm ;
- impact parameters with respect to the nominal interaction point less than 4 cm (transverse and longitudinal with respect to the beam direction);
- estimated relative error on momentum measurement less than $100 \%$.

For neutral particles the following selection criteria were applied :

- energy of the shower greater than 0.5 GeV ;
- additional requirements on shower quality, assessed as follows:
- showers in the STIC calorimeter with deposits in more than one cell;
- showers in the hadron calorimeter with energy uncertainties below $100 \%$.

Electron identification was performed in the polar angle range between $20^{\circ}$ and $160^{\circ}$ by looking for characteristic energy deposition in the central and forward/backward electromagnetic calorimeters and demanding an energy-to-momentum ratio consistent with unity. For this polar angle range the identification efficiency for high momentum electrons was determined from simulation to be $(77 \pm 2) \%$, in good agreement with efficiencies determined using Bhabha events measured in the detector.

Tracks were identified as due to muons if they had at least one associated hit in the muon chambers, or an energy deposition in the hadronic calorimeter consistent with a minimum ionizing particle. Muon identification was performed in the polar angle range between $10^{\circ}$ and $170^{\circ}$. Within this acceptance, the identification efficiency was determined from simulation to be $(92 \pm 1) \%$. Good agreement was found between data and simulation for high momentum muons in $\mathrm{Z} \rightarrow \mu^{+} \mu^{-}$decays, and for low momentum pairs produced in $\gamma \gamma$ reactions.

## 4 Event Selection and Cross-Sections

The cross-sections determined in this analysis are defined to correspond to W pair production through the three doubly resonant tree-level diagrams ("CC03 diagrams" [13]) involving $s$-channel $\gamma$ and $Z$ exchange and $t$-channel $\nu$ exchange. The selection efficiencies given in this section are also defined with respect to these diagrams only. Depending on the decay mode of each W, final states which are fully hadronic, mixed hadronicleptonic ("semileptonic"), or fully leptonic are obtained with branching ratios derived from the Standard Model of $45.9 \%, 43.7 \%$ and $10.4 \%$ respectively. In addition to their production via the CC03 diagrams, the four-fermion final states corresponding to these decay modes may be produced via other electroweak diagrams involving either zero, one, or two massive vector bosons. The effects of the interference between the CC03 diagrams and the additional diagrams have been treated as correction factors, which were applied such that the cross-sections given below can be compared to theoretical estimates of the CC03 cross-sections. The correction factors $C_{\mathrm{CC} 03}$ were determined for the individual decay modes using the 4 -fermion generator EXCALIBUR [14], which is interfaced to the DELPHI simulation package [10], and are given in table 1. The uncertainties are
estimated to be about $1.5 \%$ and are taken into account in the systematic uncertainties on the cross-sections given below.

| WW decay mode | $C_{\mathrm{CCO3}}$ |
| :--- | :--- |
| $\mathrm{q} \overline{\mathrm{q} q \overline{\mathrm{q}}}$ | 0.996 |
| $\mathrm{e} \nu \mathrm{q} \overline{\mathrm{q}}$ | 1.087 |
| $\mu(\tau) \nu \mathrm{q} \overline{\mathrm{q}}$ | 1.006 |
| $\ell \nu \ell \nu$ | 1.045 |

Table 1: Correction factors $C_{\mathrm{CC} 03}$ for the decay modes of WW pairs. For $\ell \nu \ell \nu$ the correction factor given is the average of all lepton combinations.

### 4.1 Fully Hadronic Final State

The event selection criteria were optimised in order to ensure that the final state was purely hadronic and in order to reduce the residual background. The background is dominated by electron-positron annihilation into $q \bar{q}(\gamma)$, with a cross-section about two orders of magnitude larger than that for the signal.

For each event, all particles were clustered into jets using the LUCLUS algorithm [15] with $d_{\text {join }}=6.5 \mathrm{GeV} / c$. At least 4 jets were required, with at least four particles in each jet. Figure 1a shows the distributions of the differential 3 -jet rate as a function of $d_{\text {join }}$ for data and for simulated WW and background events.

Events coming from the radiative return to the Z peak were rejected by requiring the effective centre-of-mass energy of the $\mathrm{e}^{+} \mathrm{e}^{-}$annihilation to be larger than 115 GeV . The effective energy was estimated from the momentum of the radiated photon. If an isolated photon was recorded in the detector, its measured momentum was used; otherwise its direction was assumed to be parallel to the beam axis, and its momentum was calculated by forcing a 2 -jet interpretation of the event and then using only the angular information of the jets [16]. Figure 1 b shows the distributions of the effective energy for events with at least 4 jets.

Events were then forced into a 4-jet configuration, and a kinematically constrained fit performed, imposing energy and momentum conservation. The final cut to separate WW from $\mathrm{q} \overline{\mathrm{q}}(\gamma)$ events was made on the variable

$$
D=\frac{E_{\min }}{E_{\max }} \cdot \frac{\theta_{\min }}{\left(E_{\max }-E_{\min }\right)},
$$

where $E_{\min }, E_{\max }$ are the energies of the jets with least and greatest energy, and $\theta_{\min }$ is the smallest interjet angle, after the constrained fit.

The $D$ variable discriminates well between the signal and the $q \bar{q}(\gamma)$ background, for the following reason. The signal, with both W's on or near mass-shell, consists of events with two pairs of (nearly) back-to-back di-jets, the two di-jets being able to have any orientation with respect to each other and each jet having an energy in the range of about $30-50 \mathrm{GeV}$. In contrast, in q $\bar{q} g g$ background events the quarks tend to have higher energy than the radiated gluons, and the gluons tend to follow the quark directions. $D$ was required to exceed $0.013 \mathrm{GeV}^{-1}$. Figure 1 c shows the distributions of this quantity after the other two cuts described above.

The selection efficiency was computed from a sample of WW events generated with the generator PYTHIA 5.7 [17] (with $m_{W}=80.23 \mathrm{GeV} / c^{2}$ ), with the fragmentation tuned


Figure 1: Fully hadronic final state: comparison of data (points with error bars) with simulated $\mathrm{q} \overline{\mathrm{q}}(\gamma)$ background (cross-hatched areas) and WW signal (white areas) normalised to the fitted cross-section. (a) Differential 3-jet rate (number of events changing from 4 to 3 jets) as function of $d_{\text {join }}$; (b) effective centre-of-mass energy for events with at least 4 jets; (c) $D$ variable (as defined in the text) for 4-jet events with effective centre-of-mass energy greater than 115 GeV .
to the DELPHI data measured at LEP1 [18], and was found to be $(61.3 \pm 2.0) \%$. The error includes the systematic uncertainty, which was estimated by varying all selection criteria by at least the value of their experimental resolutions and taking the quadratic sum of all contributions.

A residual background cross-section of $0.61 \pm 0.07 \mathrm{pb}$ was estimated, with the dominant contribution coming from $\mathrm{e}^{+} \mathrm{e}^{-}$annihilation into $\mathrm{q} \overline{\mathrm{q}}(\gamma)$ events, $0.4 \%$ of which survived the WW selection procedure, corresponding to a residual cross-section of 0.58 pb . The other contributions come from the channels $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{ZZ}(0.02 \mathrm{pb})$ and $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{Ze}^{+} \mathrm{e}^{-}(0.01 \mathrm{pb})$. The systematic uncertainty on the background was estimated from the variation of the selection efficiency for the $q \bar{q}(\gamma)$ background using different generators. Furthermore the accuracy of the simulation was checked on multihadronic events collected at the Z pole and at collision energies between 130 and 140 GeV . These data were selected with the 161 GeV criteria downscaled in proportion to the collision energy, and good agreement was found for the expected numbers of selected events.

From the full data sample, 15 events were selected. An unbinned maximum likelihood fit to the distribution of the variable $D$, taking into account the expected background, leads to a cross-section for fully hadronic events

$$
\sigma_{\mathrm{WW}}^{4 j e t}=\sigma_{\mathrm{WW}}^{t o t} \times \mathrm{BR}(\mathrm{WW} \rightarrow 4 \text { jets })=1.56_{-0.55}^{+0.67} \pm 0.13 \mathrm{pb},
$$

where $\mathrm{BR}(W W \rightarrow 4$ jets $)$ is the probability for the WW pair to give a purely hadronic final state, and the first errors are statistical and the last is systematic. The effects of colour reconnection are estimated to be negligible [19].

### 4.2 Semileptonic Final States

Events in which one W decays into $\ell \nu$ and the other one into quarks are characterized by two hadronic jets, one energetic and isolated charged lepton, and missing momentum
resulting from the neutrino. The major backgrounds to these events come from radiative $q \bar{q}$ production and four-fermion final states containing two quarks and two charged leptons of the same flavour. Photon conversions in the detector lead to an increase of background events in the electron channel.

Events were selected by requiring 6 or more charged particles and a missing momentum of more than $10 \mathrm{GeV} / \mathrm{c}$. Electron and muon tagging were applied to the events. In $q \bar{q}(\gamma)$ events, the selected lepton candidates are either leptons produced in heavy quark decays, misidentified hadrons, or electrons from a materialized photon. These particles generally have low momenta and small angles with respect to their quark jets. Therefore the momentum of the selected muon or the energy deposited in the electromagnetic calorimeters by the selected electron was required to be greater than 10 GeV , and the angle $\theta_{\text {iso }}$ between the lepton and the nearest charged particle with a momentum greater than $1 \mathrm{GeV} / c$ was required to be larger than $10^{\circ}$. For leptons with momenta less than $20 \mathrm{GeV} / c, \theta_{\text {iso }}$ was required to be larger than $30^{\circ}$. Figures 2 a and 2 b show the distributions of the isolation angle of the lepton and of its momentum. If more than one identified lepton passed these selections, the one of highest momentum was considered as the lepton candidate from the $W$ decay. The angle between the lepton and the missing momentum vector was required to exceed $90^{\circ}$ for electrons and $60^{\circ}$ for muons. All other particles were forced into two jets using the LUCLUS algorithm [15]. Both jets had to contain at least one charged particle, and the event was rejected if the invariant mass of the jets was smaller than $30 \mathrm{GeV} / c^{2}$, or if the angle between the jets was smaller than $80^{\circ}$.


Figure 2: Semileptonic final state: (a) isolation angle of the lepton; (b) momentum of the lepton; (c) polar angle of the missing momentum. The full lines are the expectations for the fitted signal (white areas) plus the calculated background (cross-hatched areas); data points are shown with statistical error bars. Distribution (a) contains all events with at least 6 charged tracks and a lepton with momentum above $10 \mathrm{GeV} / c$; for (b) and (c), all selection criteria are applied except the one on the variable described by each plot.

The radiative $q \bar{q}(\gamma)$ background was suppressed further by looking for evidence of an initial state radiation (ISR) photon. Events were removed if there was an energy deposition cluster of above 20 GeV in the electromagnetic calorimeters, unassociated with a charged particle. Events with undetected ISR photons close to the beam direction were suppressed by requiring the polar angle of the missing momentum vector to exceed $20^{\circ}$ for lepton momenta above $20 \mathrm{GeV} / c$, or else to exceed $32^{\circ}$. Figure 2c shows the polar angle distributions of the missing momentum. In addition, for $\mathrm{e} \nu \mathrm{q} \overline{\mathrm{q}}$ events the component
of the missing momentum transverse to the beam axis, $p_{\text {miss }}^{T}$, had to exceed $10 \mathrm{GeV} / c$, and the angles between the missing momentum vector and the directions of both jets had to exceed $10^{\circ}$ for electrons in the polar angle range between $40^{\circ}$ and $140^{\circ}$ and to exceed $20^{\circ}$ outside this range.

Four-fermion neutral current backgrounds ( $q \bar{q} \ell \ell$ ) were reduced by applying an additional cut to events in which a second lepton of the same flavour and with charge opposite to that of the first was selected: the energy in a $10^{\circ}$ cone around the second lepton direction was required to exceed 5 GeV .

If no identified lepton was found, the most energetic particle which formed an angle greater than $25^{\circ}$ with all other charged particles was considered as the lepton candidate; this recovered unidentified leptons and some additional $\mathrm{W} \rightarrow \tau \nu_{\tau}$ decays. In this case a momentum greater than $20 \mathrm{GeV} / c$ was required, and tighter cuts were also applied to the magnitude of the missing momentum (required to be above $20 \mathrm{GeV} / \mathrm{c}$ ), to its polar angle (above $32^{\circ}$ ), and to its angles to both jets (above $20^{\circ}$ ).

To improve the selection of $\mathrm{W} \rightarrow \tau \nu_{\tau}$ decays, events with at least 6 charged particles were selected if they showed a 3 -jet topology for $d_{\text {join }}>4.0 \mathrm{GeV} / \mathrm{c}$. A missing momentum above $10 \mathrm{GeV} / c$ with polar angle above $20^{\circ}$ was required, and the missing energy had to exceed 45 GeV . One jet had to be $\tau$-like, i.e. to have:

- charged multiplicity between 1 and 3 ;
- total multiplicity less than 5;
- total energy above 8 GeV ;
- fraction of charged energy above 0.1;
- fraction of the jet energy in a cone of $5^{\circ}$ around the jet axis above 0.7.

The angle between this jet and the missing momentum vector had to exceed $90^{\circ}$. In order to reduce the background from $\mathrm{q} \overline{\mathrm{q}}(\gamma)$ events further, additional cuts on the invariant mass of the two other jets ( $m_{j j}>40 \mathrm{GeV} / \mathrm{c}^{2}$ ), on the angle between them $\left(\cos \theta_{j j}<-0.8\right)$, and on their angle with the missing momentum vector (above $20^{\circ}$ ) were imposed. In addition, events were rejected if the effective centre-of-mass energy of the $\mathrm{e}^{+} \mathrm{e}^{-}$annihilation (see section 4.1) was above 150 GeV or in the range of the Z resonance ( $80-100 \mathrm{GeV}$ ).

The efficiency for selecting the signal (WW $\rightarrow \ell \nu \mathrm{jj}$ ) was calculated using events simulated with PYTHIA 5.7 to be $(60.9 \pm 3.0) \%$. The cross-section for background events which pass all selection criteria was evaluated using different generators to be $0.193 \pm$ 0.024 pb , with the main contributions coming from the channels $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{q} \overline{\mathrm{q}}(\gamma)(0.127 \mathrm{pb})$ and $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{Ze}^{+} \mathrm{e}^{-}(0.041 \mathrm{pb})$. The errors on signal efficiency and background include all systematic uncertainties, where the error on the background is dominated by hadron misidentification and photon conversions.

From a data sample corresponding to an integrated luminosity of $9.69 \mathrm{pb}^{-1}, 12$ events were selected. From this the WW cross-section for semileptonic decays was derived to be

$$
\sigma_{\mathrm{WW}}^{\ell \nu j j}=\sigma_{\mathrm{WW}}^{t o t} \times \mathrm{BR}(\mathrm{WW} \rightarrow \ell \nu \mathrm{j} \mathrm{j})=1.77_{-0.55}^{+0.67} \pm 0.10 \mathrm{pb}
$$

where the first errors are statistical and the last is systematic.

### 4.3 Fully Leptonic Final States

Events in which both W -bosons decay into $\ell \nu$ are characterized by two energetic, acollinear and acoplanar leptons of opposite charge, and by large missing energy and momentum. In $W \rightarrow \mu \nu$ and $W \rightarrow e \nu$ decays, the energy of the lepton ranges typically between 20 and $60 \mathrm{GeV} ; \mathrm{W} \rightarrow \tau \nu$ decays produce either a single charged particle with
a lower momentum, or a narrow jet. The relevant backgrounds are dilepton events from $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{Z}(\gamma)$, Bhabha scattering, and two-photon collisions.

In order to select a sample of purely leptonic events, a charged particle multiplicity between 2 and 6 was required, with the total energy of these particles greater than 40 GeV . All particles in the event were then clustered into jets using the LUCLUS algorithm [15] with $d_{\text {join }}=5.0 \mathrm{GeV} / c$. The following selection was then applied to the jet variables, thus including hadronic tau decays in the sample: a) only events with two reconstructed jets were retained, $b$ ) the momentum of the leading jet was required to be between 20 and $60 \mathrm{GeV} / c$ and that of the other jet between 12 and $50 \mathrm{GeV} / c$. Events with detected hard photons, such as those from radiative Z production with the ISR photon entering the detector acceptance, were explicitly rejected by requiring there to be no electromagnetic calorimeter cluster with energy above 30 GeV and unassociated with a charged particle.

An acollinearity $\theta_{\text {acol }}>10^{\circ}$ and acoplanarity $\theta_{\text {apl }}>10^{\circ}$ were required; the former suppresses non-radiative di-lepton production, the latter is also effective against radiative background events. Cuts on the minimum polar angle of the two jets ( $\theta$ between $20^{\circ}$ and $160^{\circ}$ ) and on the direction of the missing momentum ( $\left|\cos \theta_{\text {miss }}\right|<0.94$ ) further reduced the backgrounds due to two-photon collisions and Bhabha scattering, which are concentrated at low polar angles. Figure 3 shows the distribution of the momentum spectrum of the leading jet and of the acoplanarity.


Figure 3: Fully leptonic final states: (a) momentum of the leading jet; (b) acoplanarity. The full lines are the expectations for the fitted signal (white areas) plus the calculated background (cross-hatched areas), the data points are shown with statistical error bars. All cuts are applied except the one on the variable described by each plot.

The global efficiency of these selection criteria was computed to be $(47.7 \pm 3.0) \%$; it is considerably higher for events in which neither of the W-bosons decays to a tau lepton. The total cross-section for background events which pass all the selection cuts was computed from simulated events to be $0.06 \pm 0.04 \mathrm{pb}$. The errors contain the estimated systematic uncertainties.

With the criteria described above, 2 events were selected in the full data sample. The cross-section for purely leptonic final states was determined to be

$$
\sigma_{\mathrm{WW}}^{\ell \nu \ell \nu}=\sigma_{\mathrm{WW}}^{\text {tot }} \times \mathrm{BR}(\mathrm{WW} \rightarrow \ell \nu \ell \nu)=0.31_{-0.24}^{+0.39} \pm 0.09 \mathrm{pb},
$$

where the first errors are statistical and the last is systematic.

### 4.4 Total Cross-section

The total cross-section for WW production was obtained from a likelihood fit based on the product of the probabilities of finding the observed number of events in each final state, using the branching fractions for each of them derived from the Standard Model, giving:

$$
\sigma_{\mathrm{WW}}^{t o t}=3.67_{-0.85}^{+0.97} \pm 0.19 \mathrm{pb}
$$

where the first errors are statistical and the last is systematic. Similar results were obtained by the other LEP experiments [21].

## 5 Determination of the Mass of the W-boson

As mentioned in Section 1, the cross-section for $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{W}^{+} \mathrm{W}^{-}$near threshold is very sensitive to the value of $m_{\mathrm{W}}$, and its measured value can therefore be used to estimate $m_{\mathrm{W}}$. Such an estimate is, of course, strictly valid only within the Standard Model.

In the previous section the total cross-section for $\sigma\left(\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{W}^{+} \mathrm{W}^{-}\right)$has been determined. As mentioned in section 4, the approach adopted here has been to correct the data to correspond to a CC03 cross-section. This procedure involves several theoretical uncertainties arising from the treatment of the finite W -boson width, the uncertainty in the Coulomb term (this term, representing the Coulomb force between the W pair, is important near threshold), and from uncertainties in other radiative corrections. These effects have been considered in detail in [13], where it is concluded that the present theoretical uncertainty on the CC03 cross-section computation is about $\pm 2 \%$. This corresponds to an uncertainty on $m_{\mathrm{W}}$ of $\pm 0.04 \mathrm{GeV} / c^{2}$. In this paper the program used for the CC03 computation was that taken from reference [20]. As a cross-check, the result was compared to that obtained using reference [22] and the calculations with the default settings in the programs were found to agree at the level of $1 \%$.

In addition, it was verified that the selection efficiency does not depend strongly on the precise value of $m_{\mathrm{W}}$. This study was performed at generator level, using the EXCALIBUR generator, with cuts applied which emulated those applied to the data. Both for the CC03 subset of diagrams, and for all diagrams, the efficiency was found to be independent of $m_{\mathrm{W}}$ within the range 80.1 to $80.6 \mathrm{GeV} / c^{2}$ to within the statistical accuracy of the generated samples (about $1.5 \%$ ).

The mean LEP beam energy was determined using a model based on the field readings of nuclear magnetic resonance probes installed in the dipole magnets. The probes were calibrated with resonant depolarisation measurements at $\sqrt{ } s \approx m_{Z}{ }^{\dagger}$. A cross-check of the energy scale was made using flux-loop measurements. The effect of the RF system at the DELPHI interaction point was modelled, and a mean correction of 9 MeV was applied to the centre-of-mass energy. From these studies the LEP luminosity-weighted average centre-of-mass energy at DELPHI, $E_{C M}$, was determined to be [23]

$$
E_{C M}=161.31 \pm 0.05 \mathrm{GeV}
$$

[^1]where the error accounts for the calibration of the nuclear magnetic resonance probes at high energy, the understanding of the RF system, and additional smaller effects.

From the value of the cross-section given in section 4.4, $\sigma_{W W}^{t o t}=3.67_{-0.85}^{+0.97} \pm 0.19 \mathrm{pb}$, the value of the W -boson mass was then determined to be

$$
m_{\mathrm{W}}=80.40 \pm 0.44 \text { (stat.) } \pm 0.09 \text { (syst.) } \pm 0.03 \text { (LEP) } \mathrm{GeV} / c^{2}
$$

where the first error is from the statistical uncertainty on the cross-section, the systematic error includes both the experimental systematic errors and the theory error discussed above, and the LEP error comes from the uncertainty on the centre-of-mass energy. Figure 4 shows the dependence of the WW cross-section at 161.31 GeV on $m_{\mathrm{W}}$ together with the DELPHI result.

A further check of the method was made by evaluating $m_{W}$ in a pure four-fermion analysis, using EXCALIBUR to calculate cross-sections and to generate events which were passed through the DELPHI simulation program for efficiency determinations. Consistent results were obtained.


Figure 4: Cross-section for $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow \mathrm{W}^{+} \mathrm{W}^{-}$at 161.31 GeV versus $m_{\mathrm{W}}$ with the DELPHI result. The shaded band corresponds to a $1 \mathrm{~s} . d$. variation of the measured cross-section.

## 6 Determination of Limits on Trilinear Gauge Couplings

If $m_{\mathrm{W}}$ is taken to have the value of $80.35 \pm 0.13 \mathrm{GeV} / c^{2}$ [5] determined in $\mathrm{p} \overline{\mathrm{p}}$ experiments, the WW threshold cross-section can be used to provide limits on possible non-standard couplings at the WWV vertices. Here we interpret our measurement in terms of two such couplings.

The first is $\alpha_{W \phi}$, the contribution from one of the three $C P$-conserving components of dimension 6 in the Lagrangian $\mathcal{L}_{W W V}$ which satisfy $S U(2) \times U(1)$ invariance and are not excluded by previous measurements. According to the relations given in [24], a non-zero value of $\alpha_{W_{\phi}}$ would imply non-standard values of the dipole couplings $\kappa_{\gamma}$ and $\kappa_{Z}$ and of the $W W Z$ coupling $g_{Z}$.

The second is $\tilde{\alpha}_{W}$, a possible $C P$-violating quadrupole contribution defined in [25]. The relation between this TGC and the $C P$-violating couplings in other commonly used schemes can be found in $[25,26]$. In particular, a non-zero value of $\tilde{\alpha}_{W}$ would imply non-zero values of the couplings $f_{6}^{\gamma, Z}$ which, as pointed out in [27], are not subject to the same kinematic suppression at the WW threshold as all the other couplings (both $C P$-conserving and $C P$-violating). It is therefore of considerable interest to use these data to impose limits on a possible contribution from this source.

The amplitudes contributing to the WW production process depend linearly on the TGCs $\alpha_{i}\left(\equiv \alpha_{W \phi}, \tilde{\alpha}_{W}\right)$; the cross-section therefore has a quadratic dependence on any one TGC, which may be used in comparison with the observed production rate to derive limits on any non-standard contribution. The dependences of the cross-section on the $\alpha_{i}$ considered here are such that their minima occur close to the Standard Model value, $\alpha_{i}=0$.

The number of events in each of the three channels considered in section 4 (hadronic, semileptonic and fully leptonic) is given as a function of $\alpha_{i}$ by:

$$
\begin{equation*}
N_{j}\left(\alpha_{i}\right)=\mathcal{L} \cdot\left\{\epsilon_{j}^{s}\left(\alpha_{i}\right) \sigma_{j}^{s}\left(\alpha_{i}\right)+\epsilon_{j}^{b} \sigma_{j}^{b}\right\}, \tag{1}
\end{equation*}
$$

where $\mathcal{L}$ represents the integrated luminosity, and the $\epsilon_{j}$ represent the experimental efficiencies in channel $j$ determined in the four-fermion analysis mentioned in the previous section, the superscripts $s$ and $b$ denoting signal and background respectively. The predicted variation with the $\alpha_{i}$ of the $N_{j}\left(\alpha_{i}\right)$ was evaluated using the four-fermion generators ERATO [28] and EXCALIBUR [14], to take the interference terms between doubly resonant and other diagrams discussed in the previous section correctly into account. Separate calculations using these two generators yielded compatible predictions for the cross-sections. The probabilities of seeing 15, 12 and 2 events in the hadronic, semileptonic and fully leptonic channels, respectively, when $N_{j}\left(\alpha_{i}\right)$ are expected were evaluated and then combined in maximum likelihood fits of the $\alpha_{i}$, giving limits at $95 \%$ confidence level of

$$
\begin{aligned}
& -1.9<\alpha_{W \phi}<+2.0 \\
& -1.1<\tilde{\alpha}_{W}<+1.3
\end{aligned}
$$

The effects of systematic errors were studied by convoluting the probability function described above with Gaussian distributions of the relevant parameters and repeating the fits. They have been included in the results given. The dominant systematic effect comes from the uncertainty in $m_{\mathrm{W}}$; this leads to a broadening of the regions accepted in $\alpha_{W \phi}$ and in $\tilde{\alpha}_{W}$ by $\leq 0.04$ at each end. Smaller systematic errors come from uncertainties
in estimates of selection efficiencies and from the statistical errors in the calculation of background cross-sections, and from the uncertainty in the LEP energy.

## $7 \quad$ Summary

From an integrated luminosity of $9.93 \mathrm{pb}^{-1}$ accumulated by DELPHI at an energy of 161.31 GeV , the W-pair cross-section has been determined in its various decay modes, giving a total cross-section

$$
\sigma_{\mathrm{WW}}^{t o t}=3.67_{-0.85}^{+0.97} \text { (stat.) } \pm 0.19 \text { (syst.) pb. }
$$

From these measurements, assuming Standard Model couplings, the value of the W mass has been determined to be

$$
m_{\mathrm{W}}=80.40 \pm 0.44 \text { (stat.) } \pm 0.09 \text { (syst.) } \pm 0.03 \text { (LEP) } \mathrm{GeV} / c^{2}
$$

in agreement with previous measurements [1-5] and with a fit of electroweak data to the Standard Model [6].

Alternatively, by assuming $m_{\mathrm{W}}$ to be fixed at its current experimentally determined value, we have derived $95 \%$ confidence limits on TGCs of

$$
\begin{aligned}
& -1.9<\alpha_{W \phi}<+2.0 \\
& -1.1<\tilde{\alpha}_{W}<+1.3 .
\end{aligned}
$$

where each limit is derived assuming that the other TGCs are fixed at their Standard Model values, and the limits include estimates of the effects of systematic errors.

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[^0]:    ${ }^{1}$ Department of Physics and Astronomy, Iowa State University, Ames IA 50011-3160, USA
    ${ }^{2}$ Physics Department, Univ. Instelling Antwerpen, Universiteitsplein 1, B-2610 Wilrijk, Belgium and IIHE, ULB-VUB, Pleinlaan 2, B-1050 Brussels, Belgium
    and Faculté des Sciences, Univ. de l'Etat Mons, Av. Maistriau 19, B-7000 Mons, Belgium
    ${ }^{3}$ Physics Laboratory, University of Athens, Solonos Str. 104, GR-10680 Athens, Greece
    ${ }^{4}$ Department of Physics, University of Bergen, Allégaten 55, N-5007 Bergen, Norway
    ${ }^{5}$ Dipartimento di Fisica, Università di Bologna and INFN, Via Irnerio 46, I-40126 Bologna, Italy
    ${ }^{6}$ Centro Brasileiro de Pesquisas Físicas, rua Xavier Sigaud 150, RJ-22290 Rio de Janeiro, Brazil and Depto. de Física, Pont. Univ. Católica, C.P. 38071 RJ- 22453 Rio de Janeiro, Brazil
    and Inst. de Física, Univ. Estadual do Rio de Janeiro, rua São Francisco Xavier 524, Rio de Janeiro, Brazil
    ${ }^{7}$ Comenius University, Faculty of Mathematics and Physics, Mlynska Dolina, SK- 84215 Bratislava, Slovakia
    ${ }^{8}$ Collège de France, Lab. de Physique Corpusculaire, IN2P3-CNRS, F-75231 Paris Cedex 05, France
    ${ }^{9}$ CERN, CH-1211 Geneva 23, Switzerland
    ${ }^{10}$ Centre de Recherche Nucléaire, IN2P3 - CNRS/ULP - BP20, F-67037 Strasbourg Cedex, France
    ${ }^{11}$ Institute of Nuclear Physics, N.C.S.R. Demokritos, P.O. Box 60228, GR-15310 Athens, Greece
    ${ }^{12}$ FZU, Inst. of Physics of the C.A.S. High Energy Physics Division, Na Slovance 2, 180 40, Praha 8, Czech Republic
    ${ }^{13}$ Dipartimento di Fisica, Università di Genova and INFN, Via Dodecaneso 33, I-16146 Genova, Italy
    ${ }^{14}$ Institut des Sciences Nucléaires, IN2P3-CNRS, Université de Grenoble 1, F-38026 Grenoble Cedex, France
    ${ }^{15}$ Helsinki Institute of Physics, HIP, P.O. Box 9, FIN-00014 Helsinki, Finland
    ${ }^{16}$ Joint Institute for Nuclear Research, Dubna, Head Post Office, P.O. Box 79, 101000 Moscow, Russian Federation
    ${ }^{17}$ Institut für Experimentelle Kernphysik, Universität Karlsruhe, Postfach 6980, D-76128 Karlsruhe, Germany
    ${ }^{18}$ Institute of Nuclear Physics and University of Mining and Metalurgy, Ul. Kawiory 26a, PL-30055 Krakow, Poland
    ${ }^{19}$ Université de Paris-Sud, Lab. de l'Accélérateur Linéaire, IN2P3-CNRS, Bât. 200, F-91405 Orsay Cedex, France
    ${ }^{20}$ School of Physics and Chemistry, University of Lancaster, Lancaster LA1 4YB, UK
    ${ }^{21}$ LIP, IST, FCUL - Av. Elias Garcia, 14-1 ${ }^{\circ}$, P-1000 Lisboa Codex, Portugal
    ${ }^{22}$ Department of Physics, University of Liverpool, P.O. Box 147, Liverpool L69 3BX, UK
    ${ }^{23}$ LPNHE, IN2P3-CNRS, Universités Paris VI et VII, Tour 33 (RdC), 4 place Jussieu, F- 75252 Paris Cedex 05, France
    ${ }^{24}$ Department of Physics, University of Lund, Sölvegatan 14, S-22363 Lund, Sweden
    ${ }^{25}$ Université Claude Bernard de Lyon, IPNL, IN2P3-CNRS, F-69622 Villeurbanne Cedex, France
    ${ }^{26}$ Universidad Complutense, Avda. Complutense s/n, E-28040 Madrid, Spain
    ${ }^{27}$ Univ. d'Aix - Marseille II - CPP, IN2P3-CNRS, F-13288 Marseille Cedex 09, France
    ${ }^{28}$ Dipartimento di Fisica, Università di Milano and INFN, Via Celoria 16, I-20133 Milan, Italy
    ${ }^{29}$ Niels Bohr Institute, Blegdamsvej 17, DK-2100 Copenhagen 0, Denmark
    ${ }^{30}$ NC, Nuclear Centre of MFF, Charles University, Areal MFF, V Holesovickach 2, 18000 , Praha 8, Czech Republic
    ${ }^{31}$ NIKHEF, Postbus 41882, NL-1009 DB Amsterdam, The Netherlands
    ${ }^{32}$ National Technical University, Physics Department, Zografou Campus, GR-15773 Athens, Greece
    ${ }^{33}$ Physics Department, University of Oslo, Blindern, N-1000 Oslo 3, Norway
    ${ }^{34}$ Dpto. Fisica, Univ. Oviedo, Avda. Calvo Sotelo, S/N-33007 Oviedo, Spain, (CICYT-AEN96-1681)
    ${ }^{35}$ Department of Physics, University of Oxford, Keble Road, Oxford OX1 3RH, UK
    ${ }^{36}$ Dipartimento di Fisica, Università di Padova and INFN, Via Marzolo 8, I-35131 Padua, Italy
    ${ }^{37}$ Rutherford Appleton Laboratory, Chilton, Didcot OX11 OQX, UK
    ${ }^{38}$ Dipartimento di Fisica, Università di Roma II and INFN, Tor Vergata, I-00173 Rome, Italy
    ${ }^{39}$ CEA, DAPNIA/Service de Physique des Particules, CE-Saclay, F-91191 Gif-sur-Yvette Cedex, France
    ${ }^{40}$ Istituto Superiore di Sanità, Ist. Naz. di Fisica Nucl. (INFN), Viale Regina Elena 299, I-00161 Rome, Italy
    ${ }^{41}$ Instituto de Fisica de Cantabria (CSIC-UC), Avda. los Castros, S/N-39006 Santander, Spain, (CICYT-AEN96-1681)
    ${ }^{42}$ Inst. for High Energy Physics, Serpukov P.O. Box 35, Protvino, (Moscow Region), Russian Federation
    ${ }^{43}$ J. Stefan Institute, Jamova 39, SI-1000 Ljubljana, Slovenia and Department of Astroparticle Physics, School of Environmental Sciences, Kostanjeviska 16a, Nova Gorica, SI-5000 Slovenia, and Department of Physics, University of Ljubljana, SI-1000 Ljubljana, Slovenia
    ${ }^{44}$ Fysikum, Stockholm University, Box 6730, S-113 85 Stockholm, Sweden
    ${ }^{45}$ Dipartimento di Fisica Sperimentale, Università di Torino and INFN, Via P. Giuria 1, I-10125 Turin, Italy
    ${ }^{46}$ Dipartimento di Fisica, Università di Trieste and INFN, Via A. Valerio 2, I-34127 Trieste, Italy and Istituto di Fisica, Università di Udine, I-33100 Udine, Italy
    ${ }^{47}$ Univ. Federal do Rio de Janeiro, C.P. 68528 Cidade Univ., Ilha do Fundão BR-21945-970 Rio de Janeiro, Brazil
    ${ }^{48}$ Department of Radiation Sciences, University of Uppsala, P.O. Box 535, S-751 21 Uppsala, Sweden
    ${ }^{49}$ IFIC, Valencia-CSIC, and D.F.A.M.N., U. de Valencia, Avda. Dr. Moliner 50, E-46100 Burjassot (Valencia), Spain
    ${ }^{50}$ Institut für Hochenergiephysik, Österr. Akad. d. Wissensch., Nikolsdorfergasse 18, A-1050 Vienna, Austria
    ${ }^{51}$ Inst. Nuclear Studies and University of Warsaw, Ul. Hoza 69, PL-00681 Warsaw, Poland
    ${ }^{52}$ Fachbereich Physik, University of Wuppertal, Postfach 100 127, D-42097 Wuppertal, Germany
    ${ }^{53} \mathrm{On}$ leave of absence from IHEP Serpukhov

[^1]:    ${ }^{\dagger}$ The presence of machine imperfections inhibits the build up of transverse polarization at energies significantly higher than 50 GeV , so the resonant depolarisation technique cannot be used at the WW threshold.

