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A measurement of the W boson mass using large rapidity electrons

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Abstract

We present a measurement of the W boson mass using data collected by the DØ experiment at the Fermilab Tevatron during 1994–1995. We identify W bosons by their decays to $e\nu$ final states where the electron is detected in a forward calorimeter. We extract the W boson mass, M_W , by fitting

the transverse mass and transverse electron and neutrino momentum spectra from a sample of 11,089 $W \rightarrow e\nu$ decay candidates. We use a sample of 1,687 dielectron events, mostly due to $Z \rightarrow ee$ decays, to constrain our model of the detector response. Using the forward calorimeter data, we measure $M_W = 80.691 \pm 0.227$ GeV. Combining the forward calorimeter measurements with our previously published central calorimeter results, we obtain $M_W = 80.482 \pm 0.091$ GeV.

I. INTRODUCTION

In this article we describe the first measurement [1] of the mass of the W boson using electrons detected at large rapidities. We use data collected in 1994–1995 with the DØ detector [2] at the Fermilab Tevatron $p\bar{p}$ collider. This measurement performed with the DØ forward calorimeters [3] complements our previous measurements with central electrons [4,5] and the more complete combined rapidity coverage gives useful constraints on model parameters that permit reduction of the systematic error, in addition to increasing the statistical precision.

The study of the properties of the W boson began in 1983 with its discovery by the UA1 [6] and UA2 [7] collaborations at the CERN $p\bar{p}$ collider. Together with the discovery of the Z boson in the same year [8,9], it provided a direct confirmation of the unified description of the weak and electromagnetic interactions [10], which — together with the theory of the strong interaction, quantum chromodynamics (QCD) — now constitutes the standard model.

Since the W and Z bosons are carriers of the weak force, their properties are intimately coupled to the structure of the model. The properties of the Z boson have been studied in great detail in e^+e^- collisions [11]. The study of the W boson has proven to be significantly more difficult, since it is charged and so cannot be resonantly produced in e^+e^- collisions. Until recently its direct study has therefore been the realm of experiments at $p\bar{p}$ colliders [4,5,12,13]. Direct measurements of the W boson mass have also been carried out at LEP2 [14–17] using nonresonant W pair production. A summary of these measurements can be found in Table XI at the end of this article.

The standard model links the W boson mass to other parameters,

$$M_W = \left(\frac{\pi\alpha}{\sqrt{2}G_F} \right)^{\frac{1}{2}} \frac{1}{\sin\theta_W\sqrt{1-\Delta r}} \quad . \quad (1.1)$$

In the “on shell” scheme [18]

$$\cos\theta_W = \frac{M_W}{M_Z}, \quad (1.2)$$

where θ_W is the weak mixing angle. Aside from the radiative corrections Δr , the W boson mass is thus determined by three precisely measured quantities, the mass of the Z boson M_Z [11], the Fermi constant G_F [19], and the electromagnetic coupling constant α evaluated at $Q^2 = M_Z^2$ [19]:

$$M_Z = 91.1867 \pm 0.0021 \text{ GeV}, \quad (1.3)$$

$$G_F = (1.16639 \pm 0.00001) \times 10^{-5} \text{ GeV}^{-2} \quad , \quad (1.4)$$

$$\alpha = (128.88 \pm 0.09)^{-1} \quad . \quad (1.5)$$

From the measured W boson mass, we can derive the size of the radiative corrections Δr . Within the framework of the standard model, these corrections are dominated by loops involving the top quark and the Higgs boson (see Fig. 1). The correction from the $t\bar{t}$ loop is substantial because of the large mass difference between the two quarks. It is proportional

to m_t^2 for large values of the top quark mass m_t . Since m_t has been measured [20,21], this contribution can be calculated within the standard model. For a large Higgs boson mass, m_H , the correction from the Higgs loop is proportional to $\ln(m_H)$. In extensions to the standard model, new particles may give rise to additional corrections to the value of M_W . In the minimal supersymmetric extension of the standard model (MSSM), for example, additional corrections can increase the predicted W mass by up to 250 MeV [22].

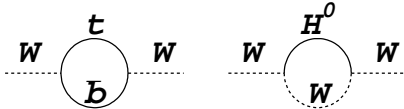


FIG. 1. Loop diagrams contributing to the W boson mass.

A measurement of the W boson mass therefore constitutes a test of the standard model. In conjunction with a measurement of the top quark mass, the standard model predicts M_W up to a 200 MeV uncertainty due to the unknown Higgs boson mass. By comparing the standard model calculation to the measured value of the W boson mass, we can constrain the mass of the Higgs boson, the agent of the electroweak symmetry breaking in the standard model that has up to now eluded experimental detection. A discrepancy with the range allowed by the standard model could indicate new physics. The experimental challenge is thus to measure the W boson mass to sufficient precision, about 0.1%, to be sensitive to these corrections.

II. OVERVIEW

A. Conventions

We use a Cartesian coordinate system with the z -axis defined by the direction of the proton beam, the x -axis pointing radially out of the Tevatron ring, and the y -axis pointing up. A vector \vec{p} is then defined in terms of its projections on these three axes, p_x , p_y , p_z . Since protons and antiprotons in the Tevatron are unpolarized, all physical processes are invariant with respect to rotations around the beam direction. It is therefore convenient to use a cylindrical coordinate system, in which the same vector is given by the magnitude of its component transverse to the beam direction, p_T , its azimuth ϕ , and p_z . In $p\bar{p}$ collisions, the center-of-mass frame of the parton-parton collisions is approximately at rest in the plane transverse to the beam direction but has an undetermined motion along the beam direction. Therefore the plane transverse to the beam direction is of special importance, and sometimes we work with two-dimensional vectors defined in the x - y plane. They are written with a subscript T , e.g. \vec{p}_T . We also use spherical coordinates by replacing p_z with the colatitude θ or the pseudorapidity $\eta = -\ln \tan(\theta/2)$. The origin of the coordinate system is in general the reconstructed position of the $p\bar{p}$ interaction when describing the interaction, and the geometrical center of the detector when describing the detector. For convenience, we use units in which $c = \hbar = 1$.

B. W and Z Boson Production and Decay

In $p\bar{p}$ collisions at $\sqrt{s} = 1.8$ TeV, W and Z bosons are produced predominantly through quark-antiquark annihilation. Figure 2 shows the lowest-order diagrams. The quarks in the initial state may radiate gluons which are usually very soft but may sometimes be energetic enough to give rise to hadron jets in the detector. In the reaction, the initial proton and antiproton break up and the fragments hadronize. We refer to everything except the vector boson and its decay products collectively as the underlying event. Since the initial proton and antiproton momentum vectors add to zero, the same must be true for the vector sum of all final state momenta and therefore the vector boson recoils against all particles in the underlying event. The sum of the transverse momenta of the recoiling particles must balance the transverse momentum of the boson, which is typically small compared to its mass but has a long tail to large values.

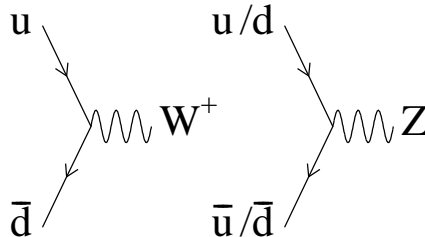


FIG. 2. Lowest order diagrams for W and Z boson production.

We identify W and Z bosons by their leptonic decays. The DØ detector (Sec. III) is best suited for a precision measurement of electrons and positrons¹, and we therefore use the decay channel $W \rightarrow e\nu$ to measure the W boson mass. $Z \rightarrow ee$ decays serve as an important calibration sample. About 11% of the W bosons decay to $e\nu$ and about 3.3% of the Z bosons decay to ee . The leptons typically have transverse momenta of about half the mass of the decaying boson and are well isolated from other large energy deposits in the calorimeter. Gauge vector boson decays are the dominant source of isolated high- p_T leptons at the Tevatron, and therefore these decays allow us to select clean samples of W and Z boson decays.

C. Event Characteristics

In events due to the process $p\bar{p} \rightarrow (W \rightarrow e\nu) + X$, where X stands for the underlying event, we detect the electron and all particles recoiling against the W boson with pseudorapidity $-4 < \eta < 4$. The neutrino escapes undetected. In the calorimeter we cannot resolve individual recoil particles, but we measure their energies summed over detector segments. Recoil particles with $|\eta| > 4$ escape unmeasured through the beampipe, possibly carrying

¹In the following we use “electron” generically for both electrons and positrons.

away substantial momentum along the beam direction. This means that we cannot measure the sum of the z -components of the recoil momenta, u_z , precisely. Since these particles escape at a very small angle with respect to the beam, their transverse momenta are typically small and can be neglected in the sum of the transverse recoil momenta, \vec{u}_T . We measure \vec{u}_T by summing the observed energy flow vectorially over all detector segments. Thus, we reduce the reconstruction of every candidate event to a measurement of the electron momentum $\vec{p}(e)$ and \vec{u}_T .

Since the neutrino escapes undetected, the sum of all measured final state transverse momenta does not add to zero. The missing transverse momentum \vec{p}_T , required to balance the transverse momentum sum, is a measure of the transverse momentum of the neutrino. The neutrino momentum component along the beam direction cannot be determined, because u_z is not measured well. The signature of a $W \rightarrow e\nu$ decay is therefore an isolated high- p_T electron and large missing transverse momentum.

In the case of $Z \rightarrow ee$ decays, the signature consists of two isolated high- p_T electrons and we measure the momenta of both leptons, $\vec{p}(e_1)$ and $\vec{p}(e_2)$, and \vec{u}_T in the detector.

D. Mass Measurement Strategy

Since $p_z(\nu)$ is unknown, we cannot reconstruct the $e\nu$ invariant mass for $W \rightarrow e\nu$ candidate events and therefore must resort to other kinematic variables for the mass measurement.

For recent measurements [12,13,5,4] the transverse mass,

$$m_T = \sqrt{2p_T(e)p_T(\nu)(1 - \cos(\phi(e) - \phi(\nu)))} \quad , \quad (2.1)$$

was used. This variable has the advantage that its spectrum is relatively insensitive to the production dynamics of the W boson. Corrections to m_T due to the motion of the W are of order $(q_T/M_W)^2$, where q_T is the transverse momentum of the W boson. It is also insensitive to selection biases that prefer certain event topologies (Sec. VID). However, it makes use of the inferred neutrino p_T and is therefore sensitive to the response of the detector to the recoil particles.

The electron p_T spectrum provides an alternative measurement of the W mass. It is measured with better resolution than the neutrino p_T and is insensitive to the recoil momentum measurement. However, its shape is sensitive to the motion of the W boson and receives corrections of order q_T/M_W . It thus requires a better understanding of the W boson production dynamics than the m_T spectrum does.

These effects are illustrated in Figs. 3 and 4, which show the effect of the motion of the W bosons and the detector resolutions on the shapes of the m_T and $p_T(e)$ spectra. The solid line shows the shape of the distribution before the detector simulation and with $q_T=0$. The points show the shape after q_T is added to the system, and the shaded histogram also includes the detector simulation. We observe that the shape of the m_T spectrum is dominated by detector resolutions and the shape of the $p_T(e)$ spectrum by the motion of the W boson.

The shape of the neutrino p_T spectrum is sensitive to both the W boson production dynamics and the recoil momentum measurement. By performing the measurement using all three spectra, we provide a powerful cross check with complementary systematics.

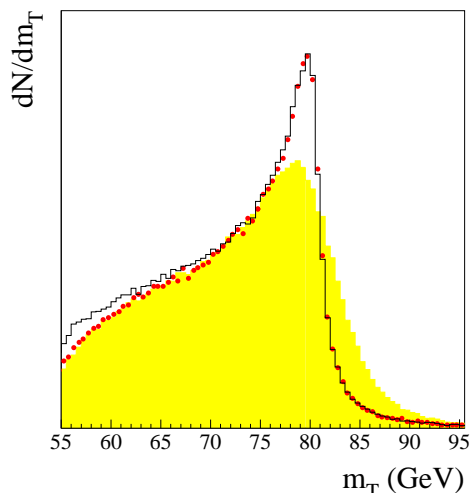


FIG. 3. The m_T spectrum for W bosons with $q_T = 0$ (—), with the correct q_T distribution (\bullet), and with detector resolutions (shaded).

All three spectra are equally sensitive to the electron energy response of the detector. We calibrate this response by forcing the observed dielectron mass peak in the $Z \rightarrow ee$ sample to agree with the known Z mass [11] (Sec. VI). This means that we effectively measure the ratio of W and Z masses, which is equivalent to a measurement of the W mass because the Z mass is known precisely.

To carry out these measurements, we perform a maximum likelihood fit to the spectra. Since the shape of the spectra, including all the experimental effects, cannot be computed analytically, we need a Monte Carlo simulation program that can predict the shape of the spectra as a function of the W mass. To measure the W mass to a precision of order 100 MeV, we have to estimate individual systematic effects to 5 MeV. This requires a Monte Carlo sample of 10 million accepted W bosons for each such effect. The program therefore must be capable of generating large event samples in a reasonable time. We achieve the required performance by employing a parameterized model of the detector response.

We next summarize the aspects of the accelerator and detector that are important for our measurement (Sec. III). Then we describe the data selection (Sec. IV) and the fast Monte Carlo model (Sec. V). Most parameters in the model are determined from our data. We describe the determination of the various components of the Monte Carlo model in Secs. VI–IX. After tuning the model, we fit the kinematic spectra (Sec. X), perform some consistency checks (Sec. XI), and discuss the systematic uncertainties (Sec. XII). We summarize the results and present the conclusions in Sec. XIV.

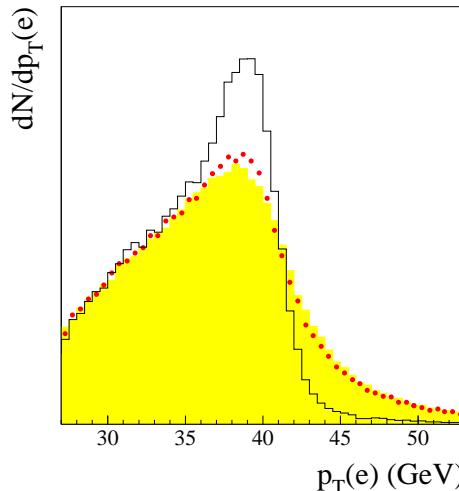


FIG. 4. The $p_T(e)$ spectrum for W bosons with $q_T = 0$ (—), with the correct q_T distribution (\bullet), and with detector resolutions (shaded).

III. EXPERIMENTAL METHOD

A. Accelerator

During the data run, the Fermilab Tevatron [23] collided proton and antiproton beams at a center-of-mass energy of $\sqrt{s} = 1.8$ TeV. Six bunches each of protons and antiprotons circulated around the ring in opposite directions. Bunches crossed at the intersection regions every $3.5 \mu\text{s}$. During the 1994–1995 running period, the accelerator reached a peak luminosity of $2.5 \times 10^{31} \text{cm}^{-2}\text{s}^{-1}$ and delivered an integrated luminosity of about 100pb^{-1} .

The Tevatron tunnel also housed a 150 GeV proton synchrotron, called the Main Ring, used as an injector for the Tevatron and accelerated protons for antiproton production during collider operation. Since the Main Ring beam pipe passed through the outer section of the DØ calorimeter, passing proton bunches gave rise to backgrounds in the detector. We eliminated this background using timing cuts based on the accelerator clock signal.

B. Detector

1. Overview

The DØ detector consists of three major subsystems: an inner tracking detector, a calorimeter, and a muon spectrometer. It is described in detail in Ref. [2]. We describe only the features that are most important for this measurement.

2. Inner Tracking Detector

The inner tracking detector is designed to measure the trajectories of charged particles. It consists of a vertex drift chamber, a transition radiation detector, a central drift chamber (CDC), and two forward drift chambers (FDC). There is no central magnetic field. The CDC covers the region $|\eta| < 1.0$. The FDC covers the region $1.4 < |\eta| < 3.0$. Each FDC consists of three separate chambers: a Φ module, with radial wires which measures the ϕ coordinate, sandwiched between a pair of Θ modules which measure (approximately) the radial coordinate. Figure 5 shows one of the two FDC detectors.

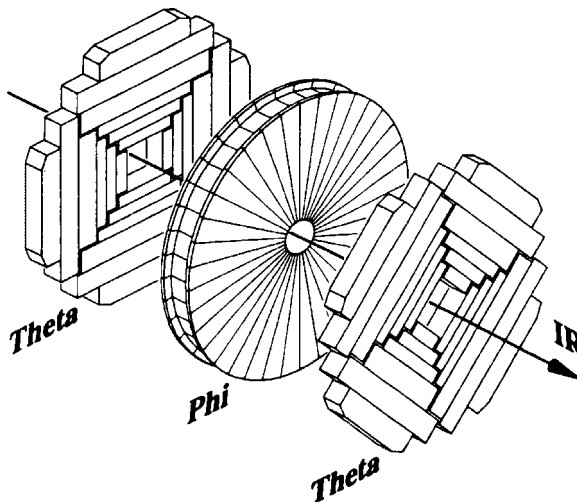


FIG. 5. An exploded view of a DØ forward drift chamber (FDC).

3. Calorimeter

The uranium/liquid-argon sampling calorimeter (Fig. 6) is the most important part of the detector for this measurement. There are three calorimeters: a central calorimeter (CC) and two end calorimeters (EC), each housed in its own cryostat. Each is segmented into an electromagnetic (EM) section, a fine hadronic (FH) section, and a coarse hadronic (CH) section, with increasingly coarser sampling.

The ECEM section (Fig. 7) has a monolithic construction of alternating uranium plates, liquid-argon gaps, and multilayer printed-circuit readout boards. Each end calorimeter is divided into about 1000 pseudo-projective towers, each covering 0.1×0.1 in $\eta \times \phi$. The EM section is segmented into four layers, 0.3, 2.6, 7.9, and 9.3 radiation lengths thick. The third layer, in which electromagnetic showers typically reach their maximum, is transversely segmented into cells covering 0.05×0.05 in $\eta \times \phi$. The EC hadronic section is segmented into five layers. The entire calorimeter is 7–9 nuclear interaction lengths thick. There are no projective cracks in the calorimeter and it provides hermetic and almost uniform coverage for particles with $|\eta| < 4$.

DØ LIQUID ARGON CALORIMETER

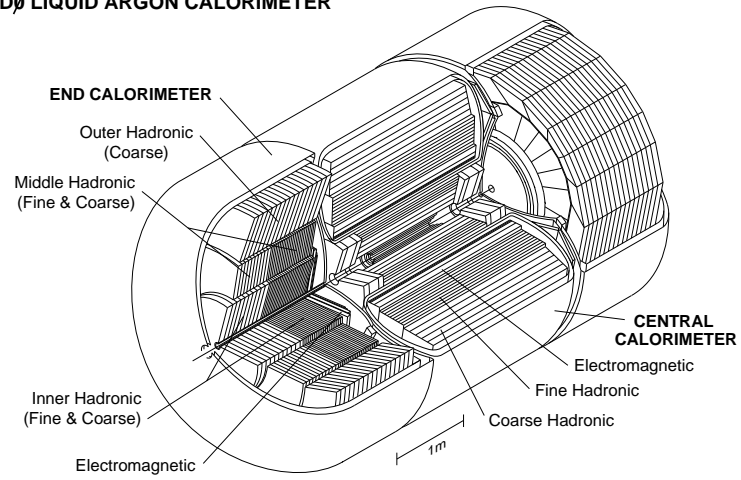


FIG. 6. A cutaway view of the DØ calorimeter and tracking system.

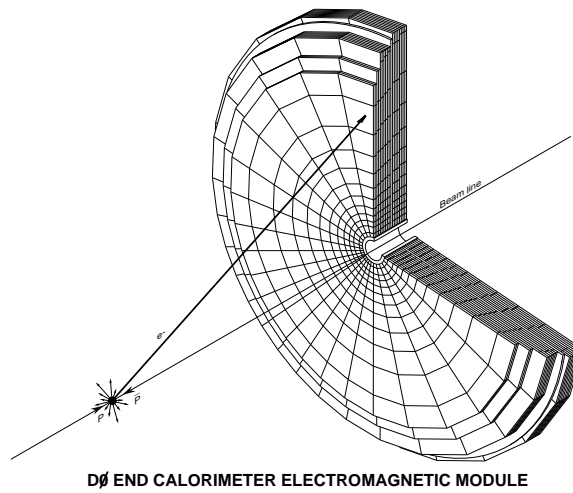


FIG. 7. The ECEM section of an end calorimeter.

The signals from arrays of 2×2 calorimeter towers covering 0.2×0.2 in $\eta \times \phi$ are added together electronically for the EM section alone and for the EM and hadronic sections together, and shaped with a fast rise time for use in the Level 1 trigger. We refer to these arrays of 2×2 calorimeter towers as “trigger towers.”

The liquid argon has unit gain and the end calorimeter response was extremely stable during the entire run. The liquid-argon response was monitored with radioactive sources of α and β particles throughout the run, as were the gains and pedestals of all readout channels. Details can be found in Ref. [24].

The ECEM calorimeter provides a measurement of energy and position of the electrons from the W and Z boson decays. Due to the fine segmentation of the third layer, we can measure the position of the shower centroid with a precision of about 1 mm in the azimuthal and radial directions.

We have studied the response of the ECEM calorimeter to electrons in beam tests [3,25]. To reconstruct the electron energy we add the signals a_i observed in each EM layer ($i = 1, \dots, 4$) and the first FH layer ($i = 5$) of an array of 5×5 calorimeter towers, centered on the most energetic tower, weighted by a layer-dependent sampling weight s_i ,

$$E = A \sum_{i=1}^5 s_i a_i - \delta_{\text{EC}} \quad . \quad (3.1)$$

To determine the sampling weights we minimize

$$\chi^2 = \sum \frac{(p_{\text{beam}} - E)^2}{\sigma_{\text{EM}}^2} \quad , \quad (3.2)$$

where the sum runs over all events and σ_{EM} is the resolution given in Eq. 3.3. We obtain $A = 3.74$ MeV/ADC count, $\delta_{\text{EC}} = -300$ MeV, $s_1 = 1.47$, $s_2 = 1.00$, $s_4 = 1.10$, and $s_5 = 1.67$. We arbitrarily fix $s_3 = 1$. The value of δ_{EC} depends on the amount of uninstrumented material in front of the calorimeter. The parameters s_1 to s_4 weight the four EM layers and s_5 the first FH layer. Figure 8 shows the fractional deviation of E as a function of the beam momentum p_{beam} . Above 20 GeV the non-linearity is less than 0.1%.

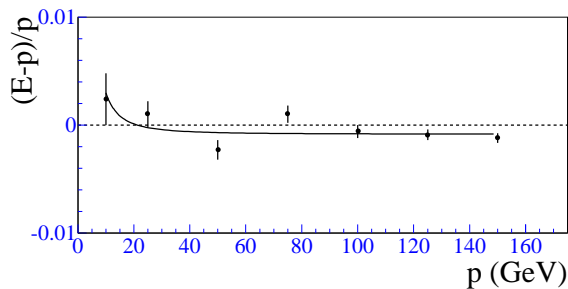


FIG. 8. The fractional deviation of the reconstructed electron energy from the beam momentum from beam tests of an ECEM module.

The fractional energy resolution can be parameterized as a function of electron energy using constant, sampling, and noise terms as

$$\left(\frac{\sigma_{\text{EM}}}{E}\right)^2 = c_{\text{EM}}^2 + \left(\frac{s_{\text{EM}}}{\sqrt{E}}\right)^2 + \left(\frac{n_{\text{EM}}}{E}\right)^2, \quad (3.3)$$

with $c_{\text{EM}} = 0.003$, $s_{\text{EM}} = 0.157 \text{ GeV}^{1/2}$ and $n_{\text{EM}} = 0.29 \text{ GeV}$ in the end calorimeters, as measured in beam tests [3,25].

4. Muon Spectrometer

The DØ muon spectrometer consists of five separate solid-iron toroidal magnets, together with sets of proportional drift tube chambers to measure the track coordinates. The central toroid covers the region $|\eta| \leq 1$, two end toroids cover $1 < |\eta| \leq 2.5$, and the small-angle muon system covers $2.5 < |\eta| \leq 3.6$. There is one layer of chambers inside the toroids and two layers outside for detecting and reconstructing the trajectory and the momentum of muons.

5. Luminosity Monitor

Two arrays of scintillator hodoscopes, mounted in front of the EC cryostats, register hits with a 220 ps time resolution. They serve to detect the occurrence of an inelastic $p\bar{p}$ interaction. The particles from the breakup of the proton give rise to hits in the hodoscopes on one side of the detector that are tightly clustered in time. For events with a single interaction, the location of the interaction vertex can be determined with a resolution of 3 cm from the time difference between the hits on the two sides of the detector for use in the Level 2 trigger. This array is also called the Level 0 trigger because the detection of an inelastic $p\bar{p}$ interaction is required for most triggers.

6. Trigger

Readout of the detector is controlled by a two-level trigger system. Level 1 consists of an and-or network that can be programmed to trigger on a $p\bar{p}$ crossing if a number of preselected conditions are satisfied. The Level 1 trigger decision is taken within the 3.5 μs time interval between crossings. As an extension to Level 1, a trigger processor (Level 1.5) may be invoked to execute simple algorithms on the limited information available at the time of a Level 1 accept. For electrons, the processor uses the energy deposits in each trigger tower as inputs. The detector cannot accept any triggers until the Level 1.5 processor completes execution and accepts or rejects the event.

Level 2 of the trigger consists of a farm of 48 VAXstation 4000's. At this level, the complete event is available. More sophisticated algorithms refine the trigger decisions and events are accepted based on preprogrammed conditions. Events accepted by Level 2 are written to magnetic tape for offline reconstruction.

IV. DATA SELECTION

A. Trigger

The conditions required at trigger Level 1 for W and Z boson candidates are:

- $p\bar{p}$ interaction: Level 0 hodoscopes register hits consistent with a $p\bar{p}$ interaction. This condition accepts 98.6% of all W and Z bosons produced.
- Main Ring Veto: No Main Ring proton bunch passes through the detector within 800 ns of the $p\bar{p}$ crossing and no protons were injected into the Main Ring less than 400 ms before the $p\bar{p}$ crossing.
- EM trigger towers: There are one or more EM trigger towers with $E \sin \theta > T$, where E is the energy measured in the tower, θ is the polar angle of the tower with the beam measured from the center of the detector, and T is a programmable threshold. This requirement is fully efficient for electrons with $p_T > 2T$.

The Level 1.5 processor recomputes the transverse electron energy by adding the adjacent EM trigger tower with the largest signal to the EM trigger tower that exceeded the Level 1 threshold. In addition, the signal in the EM trigger tower that exceeded the Level 1 threshold must constitute at least 85% of the signal registered in this tower if the hadronic layers are also included. This EM fraction requirement is fully efficient for electron candidates that pass our offline selection (Sec. IV D).

Level 2 uses the EM trigger tower that exceeded the Level 1 threshold as a starting point. The Level 2 algorithm finds the most energetic of the four calorimeter towers that make up the trigger tower, and sums the energy in the EM sections of a 3×3 array of calorimeter towers around it. It checks the longitudinal shower shape by applying cuts on the fraction of the energy in the different EM layers. The transverse shower shape is characterized by the energy deposition pattern in the third EM layer. The difference between the energies in concentric regions covering 0.25×0.25 and 0.15×0.15 in $\eta \times \phi$ must be consistent with an electron. Level 2 also imposes an isolation condition requiring

$$\frac{\sum_i E_i \sin \theta_i - p_T}{p_T} < 0.15 \quad , \quad (4.1)$$

where E_i and θ_i are the energy and polar angle of cell i , the sum runs over all cells within a cone of radius $R = \sqrt{\Delta\phi^2 + \Delta\eta^2} = 0.4$ around the electron direction and p_T is the transverse momentum of the electron [26].

The p_T of the electron computed at Level 2 is based on its energy and the z -position of the interaction vertex measured by the Level 0 hodoscopes. Level 2 accepts events that have a minimum number of EM clusters that satisfy the shape cuts and have p_T above a preprogrammed threshold. Figure 9 shows the measured relative efficiency of the Level 2 electron filter for forward electrons versus electron p_T for a Level 2 p_T threshold of 20 GeV. We determine this efficiency using Z boson data taken with a lower threshold value (16 GeV) for one electron. The efficiency is the fraction of electrons above a Level 2 p_T threshold of 20 GeV. The curve is the parameterization used in the fast Monte Carlo (see Sec. V).

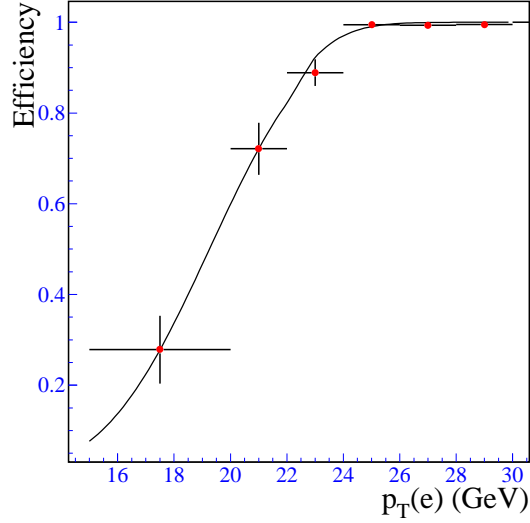


FIG. 9. The relative efficiency of the Level 2 electron filter for a threshold of 20 GeV for EC electrons, as a function of the $p_T(e)$ computed offline for the W boson mass analysis.

Level 2 also computes the missing transverse momentum based on the energy registered in each calorimeter cell and the vertex z -position as measured by the Level 0 hodoscopes. The level 2 W boson trigger requires minimum \cancel{p}_T of 15 GeV. We determine the efficiency curve for a 15 GeV Level 2 \cancel{p}_T requirement from data taken without the Level 2 \cancel{p}_T condition. Figure 10 shows the measured efficiency versus $p_T(\nu)$ as computed for the W mass analysis, when the electron is detected in the end calorimeters. The curve is the parameterization used in the fast Monte Carlo.

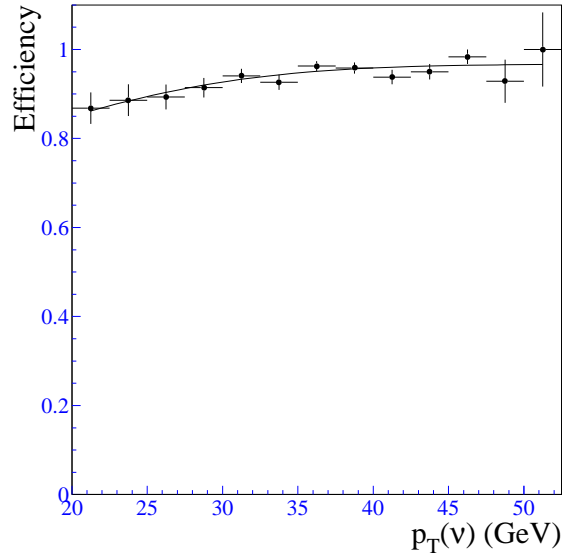


FIG. 10. The efficiency of a 15 GeV Level 2 \cancel{p}_T requirement for EC electrons, as a function of the $p_T(\nu)$ computed for the W boson mass analysis.

B. Reconstruction

1. Electron

We identify electrons as clusters of adjacent calorimeter cells with significant energy deposits. Only clusters with at least 90% of their energy in the EM section and at least 60% of their energy in the most energetic calorimeter tower are considered as electron candidates. For most electrons we also reconstruct a track in the CDC or FDC that points towards the centroid of the cluster.

We compute the forward electron energy $E(e)$ from the signals in all cells of the EM layers and the first FH layer whose centers lie within a projective cone of radius 20 cm and centered at the cluster centroid. In the computation we use the sampling weights and calibration constants determined using the test-beam data (Sec. III B 3), except for the overall energy scale A and the offset δ_{EC} , which we take from an *in situ* calibration (Sec. VI E).

The calorimeter shower centroid position $(x_{\text{cal}}, y_{\text{cal}}, z_{\text{cal}})$, the center of gravity of the track $(x_{\text{trk}}, y_{\text{trk}}, z_{\text{trk}})$, and the proton beam trajectory define the electron angle. We determine the position of the electron shower centroid $\vec{x}_{\text{cal}} = (x_{\text{cal}}, y_{\text{cal}}, z_{\text{cal}})$ in the calorimeter from the energy depositions in the third EM layer by computing the weighted mean of the positions \vec{x}_i of the cell centers,

$$\vec{x}_{\text{cal}} = \frac{\sum_i w_i \vec{x}_i}{\sum_i w_i} \quad . \quad (4.2)$$

The weights are given by

$$w_i = \max \left(0, w_0 + \log \left(\frac{E_i}{E(e)} \right) \right) \quad , \quad (4.3)$$

where E_i is the energy in cell i , w_0 is a parameter which depends upon $\eta(e)$, and $E(e)$ is the energy of the electron. The FDC track coordinates are reported at a fixed z position using a straight line fit to all the drift chamber hits on the track. The calibration of the measured r -coordinates contributes a systematic uncertainty to the W boson mass measurement. Using tracks from many events reconstructed in the vertex drift chamber, we measure the beam trajectory for every run. The closest approach to the beam trajectory of the line through the shower centroid and the track center of gravity defines the z -position of the interaction vertex (z_{vtx}). The beam trajectory provides $(x_{\text{vtx}}, y_{\text{vtx}})$. In $Z \rightarrow ee$ events, we may have two electron candidates with tracks. In this case we take the point determined from the more central electron as the interaction vertex, because this gives better resolution. Using only the electron track to determine the position of the interaction vertex, rather than all tracks in the event, makes the resolution of this measurement less sensitive to the luminosity and avoids confusion between vertices in events with more than one $p\bar{p}$ interaction.

We then define the azimuth $\phi(e)$ and the colatitude $\theta(e)$ of the electron using the vertex and the shower centroid positions

$$\tan \phi(e) = \frac{y_{\text{cal}} - y_{\text{vtx}}}{x_{\text{cal}} - x_{\text{vtx}}} \quad , \quad (4.4)$$

$$\tan \theta(e) = \frac{\sqrt{x_{\text{cal}}^2 + y_{\text{cal}}^2} - \sqrt{x_{\text{vtx}}^2 + y_{\text{vtx}}^2}}{z_{\text{cal}} - z_{\text{vtx}}} \quad . \quad (4.5)$$

Neglecting the electron mass, the momentum of the electron is given by

$$\vec{p}(e) = E(e) \begin{pmatrix} \sin \theta(e) \cos \phi(e) \\ \sin \theta(e) \sin \phi(e) \\ \cos \theta(e) \end{pmatrix} . \quad (4.6)$$

2. Recoil

We reconstruct the transverse momentum of all particles recoiling against the W or Z boson by taking the vector sum

$$\vec{u}_T = \sum_i E_i \sin \theta_i \begin{pmatrix} \cos \phi_i \\ \sin \phi_i \end{pmatrix} , \quad (4.7)$$

where the sum runs over all calorimeter cells that were read out, except those that belong to electron cones. E_i are the cell energies, and ϕ_i and θ_i are the azimuth and colatitude of the center of cell i with respect to the interaction vertex.

3. Derived Quantities

In the case of $Z \rightarrow ee$ decays, we define the dielectron momentum

$$\vec{p}(ee) = \vec{p}(e_1) + \vec{p}(e_2) \quad (4.8)$$

and the dielectron invariant mass

$$m(ee) = \sqrt{2E(e_1)E(e_2)(1 - \cos \omega)} \quad , \quad (4.9)$$

where ω is the opening angle between the two electrons. It is useful to define a coordinate system in the plane transverse to the beam that depends only on the electron directions. We follow the conventions first introduced by UA2 [12] and call the axis along the inner bisector of the two electrons the η -axis and the axis perpendicular to that the ξ -axis. Projections on these axes are denoted with subscripts η or ξ . Figure 11 illustrates these definitions.

In the case of $W \rightarrow e\nu$ decays, we define the transverse neutrino momentum

$$\vec{p}_T(\nu) = -\vec{p}_T(e) - \vec{u}_T \quad (4.10)$$

and the transverse mass (Eq. 2.1). Useful quantities are the projection of the transverse recoil momentum on the electron direction,

$$u_{\parallel} = \vec{u}_T \cdot \hat{p}_T(e) \quad , \quad (4.11)$$

and the projection on the direction perpendicular to the electron direction,

$$u_{\perp} = \vec{u}_T \cdot (\hat{p}_T(e) \times \hat{z}) \quad . \quad (4.12)$$

Figure 12 illustrates these definitions.

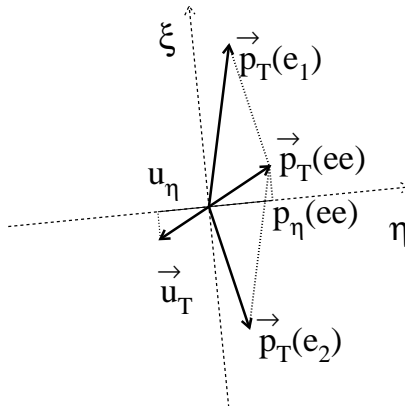


FIG. 11. Illustration of momentum vectors in the transverse plane for $Z \rightarrow ee$ candidates. The vectors drawn as thick lines are directly measured.

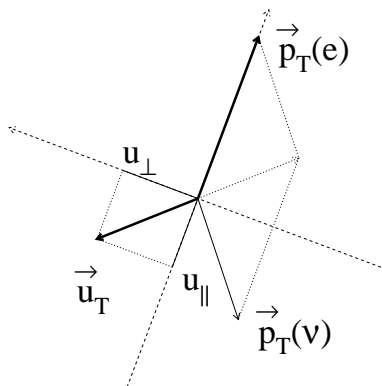


FIG. 12. Illustration of momentum vectors in the transverse plane for $W \rightarrow e\nu$ candidates. The vectors drawn as thick lines are directly measured.

C. Electron Identification

1. Fiducial Cuts

Electrons in the ECEM are defined by the pseudorapidity η of the cluster centroid position with respect to the center of the detector. We define forward electrons by $1.5 \leq |\eta_{\text{det}}(e)| \leq 2.5$.

2. Quality Variables

We test how well the shape of a cluster agrees with that expected for an electromagnetic shower by computing a quality variable (χ^2) for all cell energies using a 41-dimensional covariance matrix. The covariance matrix was determined from GEANT-based [27] simulations [28] that were tuned to agree with extensive test beam measurements.

To determine how well a track matches a cluster, we extrapolate the track to the third EM layer in the end calorimeter and compute the distance between the extrapolated track and the cluster centroid in the azimuthal direction, Δs , and in the r -direction, $\Delta \rho$. The variable

$$\sigma_{\text{trk}}^2 = \left(\frac{\Delta s}{\delta s}\right)^2 + \left(\frac{\Delta \rho}{\delta \rho}\right)^2, \quad (4.13)$$

quantifies the quality of the match. The parameters $\delta s = 0.25$ cm and $\delta \rho = 1.0$ cm are the resolutions with which Δs and $\Delta \rho$ are measured, as determined using the end calorimeter electrons from $W \rightarrow e\nu$ decays.

In the EC, electrons must have a matched track in the forward drift chamber to suppress background due to misidentification. In the CC, we define “tight” and “loose” criteria. The tight criteria require a matched track in the CDC, defined as the track with the smallest σ_{trk} . The loose criteria do not require a matched track and help increase the electron finding efficiency for $Z \rightarrow ee$ decays with at least one central electron.

The isolation fraction is defined as

$$f_{\text{iso}} = \frac{E_{\text{cone}} - E_{\text{core}}}{E_{\text{core}}}, \quad (4.14)$$

where E_{cone} is the energy in a cone of radius $R = 0.4$ around the direction of the electron, summed over the entire depth of the calorimeter, and E_{core} is the energy in a cone of $R = 0.2$, summed over the EM calorimeter only.

We use the dE/dx information provided by the FDC on the tracks associated with the EM calorimeter cluster. The dE/dx information helps to distinguish between singly-ionizing electron tracks and doubly-ionizing tracks from photon conversions.

We identify electron candidates in the forward detectors by making loose cuts on the shower shape χ^2 , the track-cluster match quality, and the shower electromagnetic energy fraction. We then use a cut on a 4-variable likelihood ratio λ_4 which combines the information in these variables and the track dE/dx into a single variable. The final cut on the likelihood ratio λ_4 gives the maximum discrimination between electrons and jet background, i.e. gives the maximum background rejection for any given electron selection efficiency.

Figure 13 shows the distributions of the quality variables for electrons in the EC; the arrows indicate the cut values. Table I summarizes the electron selection criteria.

D. Data Samples

The data were collected during the 1994–1995 Tevatron run. After the removal of runs in which parts of the detector were not operating adequately, the data correspond to an integrated luminosity of 82 pb^{-1} . We select W boson decay candidates by requiring:

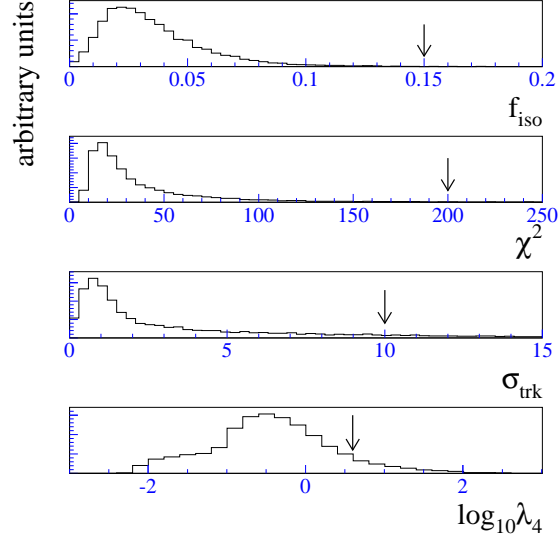


FIG. 13. Distributions of the EC electron identification variables for $W \rightarrow e\nu$ candidates. The arrows indicate the cut values.

- Level 1: $p\bar{p}$ interaction
Main Ring Veto
EM trigger tower above 10 GeV
- Level 1.5: ≥ 1 EM cluster above 15 GeV
- Level 2: electron candidate with $p_T > 20$ GeV
momentum imbalance $\cancel{p}_T > 15$ GeV
- offline: ≥ 1 tight electron candidate in EC
 $p_T(e) > 30$ GeV
 $p_T(\nu) > 30$ GeV
 $u_T < 15$ GeV

This selection gives us 11,089 W boson candidates. We select Z boson decay candidates by requiring:

- Level 1: $p\bar{p}$ interaction
 ≥ 2 EM trigger towers above 7 GeV
- Level 1.5: ≥ 1 EM cluster above 10 GeV
- Level 2: ≥ 2 electron candidates with $p_T > 20$ GeV
- offline: ≥ 2 electron candidates
 $p_T(e) > 30$ GeV (EC)
or $p_T(e) > 25$ GeV (CC)

We accept $Z \rightarrow ee$ decays with at least one electron candidate in the EC and the other in the CC or the EC. EC candidates must pass the tight electron selection criteria. A CC candidate may pass only the loose criteria. We use the 1,687 events with at least one electron in the EC (CC/EC + EC/EC Z samples) to calibrate the calorimeter response to electrons (Sec. VI). These events need not pass the Main Ring Veto cut because Main Ring background does not affect the EM calorimeter. The events for which both electrons are in the EC (EC/EC Z sample) and which pass the Main Ring Veto serve to check the calibration of the recoil

TABLE I. Electron selection criteria. $\Delta\phi_{\text{cal}}$ is the difference in azimuthal angle between the cluster centroid and the CC module edge.

variable	CC (loose)	CC (tight)	EC (tight)
fiducial cuts	$ \Delta\phi_{\text{cal}} > 0.02$ $ z_{\text{cal}} < 108 \text{ cm}$ —	$ \Delta\phi_{\text{cal}} > 0.02$ $ z_{\text{cal}} < 108 \text{ cm}$ $ z_{\text{trk}} < 80 \text{ cm}$	— $1.5 \leq \eta \leq 2.5$ —
shower shape	$\chi^2 < 100$	$\chi^2 < 100$	$\chi^2 < 200$
isolation	$f_{\text{iso}} < 0.15$	$f_{\text{iso}} < 0.15$	$f_{\text{iso}} < 0.15$
track match	—	$\sigma_{\text{trk}} < 5$	$\sigma_{\text{trk}} < 10$
4-variable likelihood ratio	—	—	$\lambda_4 < 4$

momentum response (Sec. VII). Table II summarizes the data samples.

TABLE II. Number of W and Z boson candidate events.

channel	$Z \rightarrow ee$		$W \rightarrow e\nu$
fiducial region of electrons	CC/EC	EC/EC	EC
	1265	422	11089

Figure 14 shows the luminosity of the colliding beams during the W and Z boson data collection.

On several occasions we use a sample of 295,000 random $p\bar{p}$ interaction events for calibration purposes. We collected these data concurrently with the W and Z signal data, requiring only a $p\bar{p}$ interaction at Level 1. We refer to these data as “minimum bias events.”

V. FAST MONTE CARLO MODEL

A. Overview

The fast Monte Carlo model consists of three parts. First we simulate the production of the W or Z boson by generating the boson four-momentum and other characteristics of the event such as the z -position of the interaction vertex and the luminosity. The event luminosity is required for luminosity-dependent parametrizations in the detector simulation. Then we simulate the decay of the boson. At this point we know the true p_T of the boson and the momenta of its decay products. We next apply a parameterized detector model to these momenta to simulate the observed transverse recoil momentum and the observed electron momenta.

Our fast Monte Carlo program is very similar to the one used in our published CC analysis [4], with some modifications in the simulation of forward electron events.

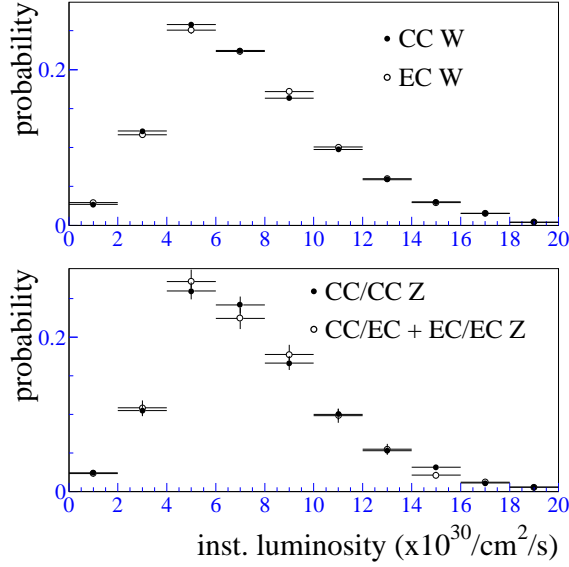


FIG. 14. The instantaneous luminosity distribution of the W (top) and the Z (bottom) boson samples.

B. Vector Boson Production

To specify the production dynamics of vector bosons in $p\bar{p}$ collisions completely, we need to know the differential production cross section in mass Q , rapidity y , and transverse momentum q_T of the produced W bosons. To speed up the event generation, we factorize this into

$$\frac{d^3\sigma}{dq_T^2 dy dQ} \approx \left. \frac{d^2\sigma}{dq_T^2 dy} \right|_{Q^2=M_W^2} \times \frac{d\sigma}{dQ} \quad (5.1)$$

to generate q_T , y , and Q of the bosons.

For $p\bar{p}$ collisions, the vector boson production cross section is given by the parton cross section $\tilde{\sigma}_{i,j}$ convoluted with the parton distribution functions $f(x, Q^2)$ and summed over parton flavors i, j :

$$\frac{d^2\sigma}{dq_T^2 dy} = \sum_{i,j} \int dx_1 \int dx_2 f_i(x_1, Q^2) f_j(x_2, Q^2) \delta(sx_1x_2 - Q^2) \frac{d^2\tilde{\sigma}_{i,j}}{dq_T^2 dy} \quad (5.2)$$

The cross section $d^2\sigma/dq_T^2 dy|_{Q^2=M_W^2}$ has been computed by several authors [29,30] using a perturbative calculation [31] for the high- q_T regime and the Collins-Soper resummation formalism [32,33] for the low- q_T regime. We use the code provided by the authors of Ref. [29] and the MRST parton distribution functions [34] to compute the cross section.

We use a Breit-Wigner curve with a mass-dependent width for the line shape of the W boson. The intrinsic width of the W is $\Gamma_W = 2.062 \pm 0.059$ GeV [35]. The line shape is

skewed due to the momentum distribution of the quarks inside the proton and antiproton. The mass spectrum is given by

$$\frac{d\sigma}{dQ} = \mathcal{L}_{q\bar{q}}(Q) \frac{Q^2}{(Q^2 - M_W^2)^2 + \frac{Q^4 \Gamma_W^2}{M_W^2}} \quad (5.3)$$

We call

$$\mathcal{L}_{q\bar{q}}(Q) = \frac{2Q}{s} \sum_{i,j} \int_{Q^2/s}^1 \frac{dx}{x} f_i(x, Q^2) f_j(Q^2/s, Q^2) \quad (5.4)$$

the parton luminosity. To evaluate it, we generate $W \rightarrow e\nu$ events using the HERWIG Monte Carlo event generator [36], interfaced with PDFLIB [37], and select the events subject to the same fiducial cuts as for the W and Z boson samples with at least one electron in EC. We plot the mass spectrum divided by the intrinsic line shape of the W boson. The result is proportional to the parton luminosity, and we parameterize the shape of the spectrum with the function [5]

$$\mathcal{L}_{q\bar{q}}(Q) = \frac{e^{-\beta Q}}{Q} \quad (5.5)$$

Table III shows the parton luminosity slope β for W and Z events for the different topologies. The value of β depends on the rapidity distribution of the W and Z bosons, which is restricted by the fiducial cuts that we impose on the decay leptons. The values of β given in Table III are for the rapidity distributions of W and Z bosons that satisfy the fiducial cuts given in Sec. IV. The uncertainty in β is about 0.001 GeV^{-1} , due to Monte Carlo statistics and uncertainties in the acceptance.

TABLE III. Parton luminosity slope β in the W and Z boson production model. The β value is given for $W \rightarrow e\nu$ decays with the electron in the EC and for $Z \rightarrow ee$ decays with at least one electron in the EC.

	Z production $\beta \text{ (GeV}^{-1}\text{)}$	W production $\beta \text{ (GeV}^{-1}\text{)}$
CC/EC	9.9×10^{-3}	—
EC/EC	19.9×10^{-3}	—
EC	—	16.9×10^{-3}

Bosons can be produced by the annihilation of two valence quarks, two sea quarks, or one valence quark and one sea quark. Using the HERWIG events, we evaluate the fraction f_{ss} of bosons produced by the annihilation of two sea quarks. We find $f_{ss} = 0.207$, independent of the boson topology.

To generate the boson four-momenta, we treat $d\sigma/dQ$ and $d^2\sigma/dq_T^2 dy$ as probability density functions and pick Q from the former and a pair of y and q_T values from the latter.

For a fraction f_{ss} the boson helicity is $+1$ or -1 with equal probability. The remaining W bosons always have helicity -1 . Finally, we pick the z -position of the interaction vertex from a Gaussian distribution centered at $z = 0$ with a standard deviation of 27 cm and a luminosity for each event from the histogram in Fig. 14.

C. Vector Boson Decay

At lowest order, the W^\pm boson is fully polarized along the beam direction due to the $V \mp A$ coupling of the charged current. The resulting angular distribution of the charged lepton in the W boson rest frame is given by

$$\frac{d\sigma}{d\cos\theta^*} \propto (1 - \lambda q \cos\theta^*)^2, \quad (5.6)$$

where λ is the helicity of the W boson with respect to the proton direction, q is the charge of the lepton, and θ^* is the angle between the charged lepton and proton beam directions in the W rest frame. The spin of the W boson points along the direction of the incoming antiquark. Most of the time, the quark comes from the proton and the antiquark from the antiproton, so that $\lambda = -1$. Only if both quark and antiquark come from the sea of the proton and antiproton, is there a 50% chance that the quark comes from the antiproton and the antiquark from the proton and in that case $\lambda = 1$ (see Fig. 15).

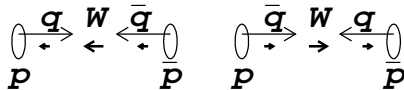


FIG. 15. Polarization of the W boson produced in $p\bar{p}$ collisions if the quark comes from the proton (left) and if the antiquark comes from the proton (right). The short thick arrows indicate the orientations of the particle spins.

When $\mathcal{O}(\alpha_s)$ processes are included, the boson acquires finite transverse momentum and Eq. 5.6 becomes [38]

$$\frac{d\sigma}{d\cos\theta_{CS}} \propto \left(1 - \lambda q \alpha_1(q_T) \cos\theta_{CS} + \alpha_2(q_T) \cos^2\theta_{CS}\right) \quad (5.7)$$

for W bosons after integration over ϕ . The angle θ_{CS} in Eq. 5.7 is now defined in the Collins-Soper frame [39]. The values of α_1 and α_2 as a function of transverse boson momentum have been calculated at $\mathcal{O}(\alpha_s^2)$ [38]. We have implemented the angular distribution given in Eq. 5.7 in the fast Monte Carlo. The angular distribution of the leptons from $Z \rightarrow ee$ decays is also generated according to Eq. 5.7, but with α_1 and α_2 computed for $Z \rightarrow ee$ decays [38].

Radiation from the decay electron or the W boson biases the mass measurement. If the decay electron radiates a photon and the photon is sufficiently separated from the electron so that its energy is not included in the electron energy, or if an on-shell W boson radiates a photon and therefore is off-shell when it decays, the measured mass is biased low. We use the calculation of Ref. [40] to generate $W \rightarrow e\nu\gamma$ and $Z \rightarrow ee\gamma$ decays. The calculation gives the fraction of events in which a photon with energy $E(\gamma) > E_0$ is radiated, and the

angular distribution and energy spectrum of the photons. Only radiation from the decay electron and the W boson, if the final state W is off-shell, is included to order α . Radiation by the initial quarks or the W boson, if the final W is on-shell, does not affect the mass of the $e\nu$ pair from the W decay. We use a minimum photon energy $E_0 = 50$ MeV, and calculate that in 30.6% of all W decays a photon with $E(\gamma) > 50$ MeV is radiated. Most of these photons are emitted close to the electron direction and cannot be separated from the electron in the calorimeter. For $Z \rightarrow ee$ decays, there is a 66% probability for either of the electrons to radiate a photon with $E(\gamma) > 50$ MeV.

If the photon and electron are close together, they cannot be separated in the calorimeter. The momentum of a photon with $\Delta R(e\gamma) < R_0$ is therefore added to the electron momentum, while for $\Delta R(e\gamma) \geq R_0$, a photon is considered separated from the electron and its momentum is added to the recoil momentum. We use $R_0 = 20$ cm, which is the size of the cone in which the electron energy is measured.

W boson decays through the channel $W \rightarrow \tau\nu \rightarrow e\nu\bar{\nu}\nu$ are topologically indistinguishable from $W \rightarrow e\nu$ decays. We therefore include these decays in the W decay model, properly accounting for the polarization of the tau leptons in the decay angular distributions. The fraction of W boson decays to electrons that proceed via tau decay is $B(\tau \rightarrow e\nu\bar{\nu}) / (1 + B(\tau \rightarrow e\nu\bar{\nu})) = 0.151$.

D. Detector Model

The detector simulation uses a parameterized model for detector response and resolution to obtain a prediction for the distributions of the observed electron and recoil momenta.

When simulating the detector response to an electron of energy E_0 , we compute the observed electron energy as

$$E(e) = \alpha_{\text{EC}} E_0 + \Delta E(\mathcal{L}, \eta, u_{\parallel}) + \sigma_{\text{EM}} X \quad , \quad (5.8)$$

where α_{EC} is the response of the end electromagnetic calorimeter, ΔE is the energy due to particles from the underlying event within the electron cone (parameterized as a function of luminosity \mathcal{L} , η and u_{\parallel}), σ_{EM} is the energy resolution of the electromagnetic calorimeter, and X is a random variable from a normal parent distribution with zero mean and unit width.

The transverse energy measurement depends on the measurement of the electron direction as well. We determine the shower centroid position by intersecting the line defined by the event vertex and the electron direction with a plane perpendicular to the beam and located at $z = \pm 179$ cm (the longitudinal center of the ECEM3 layer). We then smear the azimuthal and r -coordinates of the intersection point by their resolutions. We determine the r -coordinate of the center of gravity of the FDC track by intersecting the same line with a plane at $z = \pm 105$ cm, the defined z position of the FDC track centroid, and smearing by the resolution. The measured angles are then obtained from the smeared points as described in Section IV B 1.

The model for the particles recoiling against the W boson has two components: a “hard” component that models the p_T of the W boson, and a “soft” component that models detector noise and pile-up. Pile-up refers to the effects of additional $p\bar{p}$ interactions in the same or

previous beam crossings. For the soft component we use the transverse momentum balance \vec{p}_T measured in minimum bias events recorded in the detector. The minimum bias events are weighted so that their luminosity distribution is the same as that of the W sample. The observed recoil p_T is then given by

$$\begin{aligned}\vec{u}_T = & -(\text{R}_{\text{rec}}q_T + \sigma_{\text{rec}}X)\hat{q}_T \\ & -\Delta u_{\parallel}(\mathcal{L}, \eta, u_{\parallel})\hat{p}_T(e) \\ & +\alpha_{\text{mb}}\vec{p}_T \quad ,\end{aligned}\tag{5.9}$$

where q_T is the generated value of the boson transverse momentum, R_{rec} is the (in general momentum-dependent) response, σ_{rec} is the resolution of the calorimeter (parameterized as $\sigma_{\text{rec}} = s_{\text{rec}}\sqrt{u_T}$), Δu_{\parallel} is the transverse energy flow into the electron window (parameterized as a function of \mathcal{L} , η and u_{\parallel}), and α_{mb} is a correction factor that allows us to adjust the resolution to the data, accounting for the difference between the data minimum bias events and the underlying spectator collisions in W events. The quantity Δu_{\parallel} is different from the transverse energy added to the electron, ΔE_T , because of the difference in the algorithms used to compute the electron E_T and the recoil p_T .

We simulate selection biases due to the trigger requirements and the electron isolation by accepting events with the estimated efficiencies. Finally, we compute all the derived quantities from these observables and apply fiducial and kinematic cuts.

VI. ELECTRON MEASUREMENT

A. Angular Calibrations

The FDC detectors have been studied and calibrated extensively in a test beam [41]. We use collider data muons which traverse the forward muon detectors and the FDC to provide a cross-check of the test beam calibration of the r -measurement of the track in the FDC. We predict the trajectory of the muon through the FDC by connecting the hits in the innermost muon chambers with the reconstructed event vertex by a straight line. The center of gravity of the FDC track can then be compared relative to this line. Figure 16 shows the difference between the predicted and the actual r -positions of the track center of gravity. These data are fit to a straight line constrained to pass through the origin. We find the track position is consistent with the predicted position.

We calibrate the shower centroid algorithm using Monte Carlo electrons simulated using GEANT and electrons from the $Z \rightarrow ee$ data. We apply a polynomial correction as a function of r_{cal} and the distance from the cell edges based on the Monte Carlo electrons. We refine the calibration with the $Z \rightarrow ee$ data by exploiting the fact that both electrons originate from the same vertex. Using the algorithm described in Sec. IV B 1, we determine a vertex for each electron from the shower centroid and the track center of gravity. We minimize the difference between the two vertex positions as a function of an r_{cal} scale factor β_{EC} (see Fig. 17). The correction factor is $\beta_{\text{EC}} = 0.9997 \pm 0.00044$ for EC North, and $\beta_{\text{EC}} = 1.00225 \pm 0.00044$ for EC South. We find no systematic radial dependence of these correction factors.

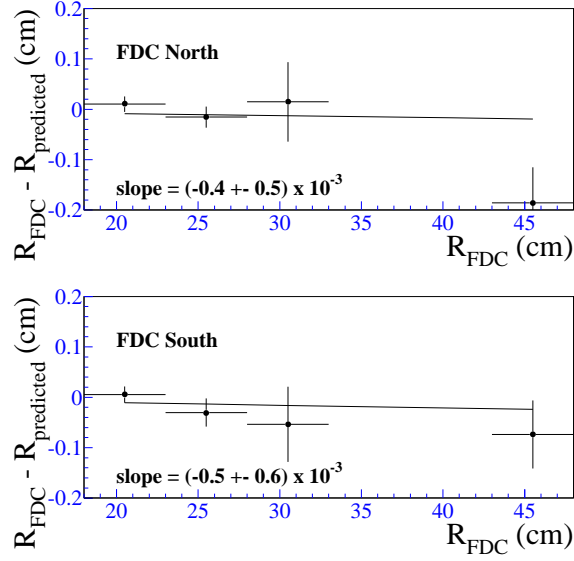


FIG. 16. Residue of the radial position of the FDC track centroid from the predicted radial position of forward muon tracks at the FDC, as a function of the track radial position. The solid line is a fitted straight line constrained to pass through the origin.

We quantify the FDC and EC radial calibration uncertainty in terms of scale factor uncertainties $\delta\beta_{\text{FDC}} = \pm 0.00054$ and $\delta\beta_{\text{EC}} = \pm 0.0003$ for the r -coordinate. The uncertainties in these scale factors lead to a 20 MeV uncertainty in the EC W boson mass measurement.

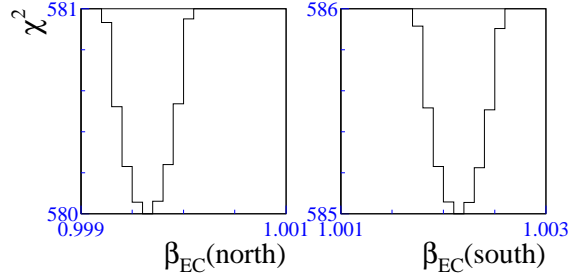


FIG. 17. The χ^2 versus β_{EC} value.

B. Angular Resolutions

The resolution for the r -coordinate of the track center of gravity, r_{trk} , is determined from the $Z \rightarrow ee$ sample. Both electrons originate from the same interaction vertex and therefore the difference between the interaction vertices reconstructed from the two electrons separately, $z_{\text{vtx}}(e_1) - z_{\text{vtx}}(e_2)$, is a measure of the resolution with which the electrons point back to the vertex. The points in Fig. 18 show the distribution of $z_{\text{vtx}}(e_1) - z_{\text{vtx}}(e_2)$ observed in the CC/EC and EC/EC Z samples with matching tracks required for both electrons.

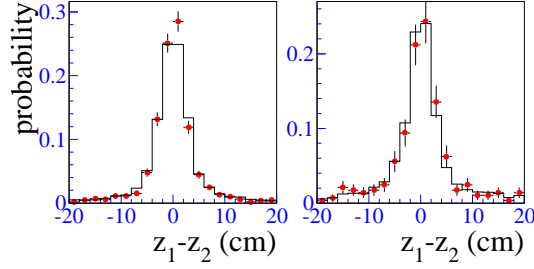


FIG. 18. The distribution of $z_{\text{vtx}}(e_1) - z_{\text{vtx}}(e_2)$ for the CC/EC (left) and EC/EC (right) $Z \rightarrow ee$ samples (\bullet) and the fast Monte Carlo simulation (—).

A Monte Carlo study based on single electrons generated with a GEANT simulation shows that the resolution of the shower centroid algorithm is 0.1 cm in the EC, consistent with EC electron beam tests. We then tune the resolution function for r_{trk} in the fast Monte Carlo so that it reproduces the shape of the $z_{\text{vtx}}(e_1) - z_{\text{vtx}}(e_2)$ distribution observed in the data. We find that a resolution function consisting of two Gaussians 0.2 cm and 1.7 cm wide, with 20% of the area under the wider Gaussian, fits the data well. The histogram in Fig. 18 shows the Monte Carlo prediction for the best fit, normalized to the same number of events as the data.

C. Underlying Event Energy

The energy in a projective cone of radius 20 cm in the four ECEM layers and the first EC-FH layer around the electron cluster centroid is assigned to the electron. This cone contains the entire energy deposited by the electron shower plus some energy from other particles. The energy in the window is excluded from the computation of \vec{u}_T . This causes a bias in u_{\parallel} , the component of \vec{u}_T along the direction of the electron. We call this bias Δu_{\parallel} . It is equal to the momentum flow observed in the EM and first FH sections of a projective cone of radius 20 cm at ECEM3.

We use the W data sample to measure Δu_{\parallel} . For every electron in the W sample, we compute the energy flow into an azimuthally rotated position, keeping the cone radius and the radial position the same. For the rotated position we compute the measured transverse energy. Since the $\eta\phi$ area of the cone increases as the electron η increases, it is convenient to parameterize the transverse energy density, $\Delta u_{\parallel}/\delta\eta\delta\phi$.

At higher luminosity the average number of interactions per event increases and therefore $\Delta u_{\parallel}/\delta\eta\delta\phi$ increases (Fig. 19). The mean value of $\Delta u_{\parallel}/\delta\eta\delta\phi$ increases by 40 MeV per $10^{30}\text{cm}^{-2}\text{s}^{-1}$. The underlying event energy flow into the electron cone depends on the electron η , as shown in Fig. 20, corrected back to zero luminosity. The underlying event energy flow into the electron cone also depends on u_{\parallel} . Figure 21 shows $\langle\Delta u_{\parallel}/\delta\eta\delta\phi(\mathcal{L} = 0, |\eta| = 2.0)\rangle$, the mean value for $\Delta u_{\parallel}/\delta\eta\delta\phi$ corrected to zero luminosity and $|\eta| = 2.0$, as a function of u_{\parallel} . In the fast Monte Carlo model, a value $\Delta u_{\parallel}/\delta\eta\delta\phi$ is picked from the distribution shown in Fig. 22 for every event, corrected for u_{\parallel} , η , and luminosity dependences, and then scaled by the $\delta\eta\delta\phi$ area of a 20 cm cone at the electron η .

The measured electron transverse energy is biased upwards by the additional energy ΔE_T

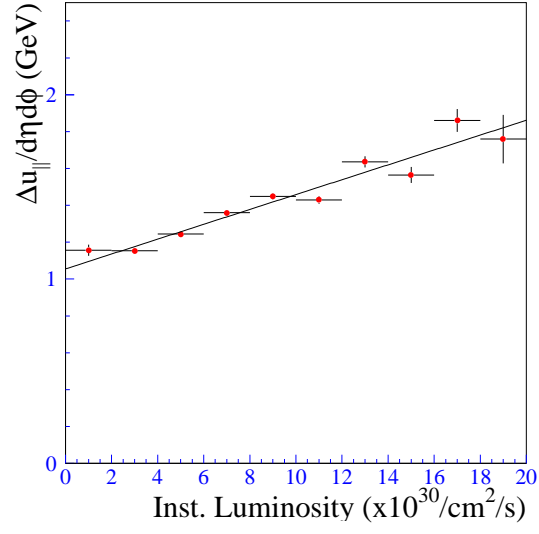


FIG. 19. The instantaneous luminosity dependence of $\langle \Delta u_{\parallel} / \delta \eta \delta \phi \rangle$.

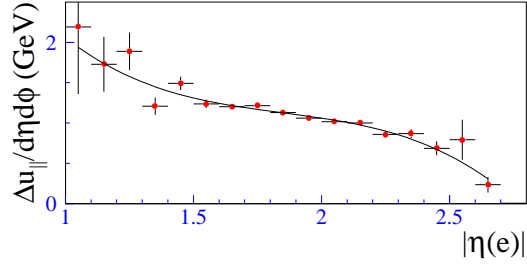


FIG. 20. The variation of $\langle \Delta u_{\parallel} / \delta \eta \delta \phi \rangle$ as a function of electron η .

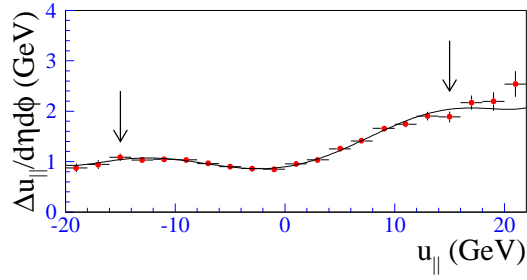


FIG. 21. The variation of $\langle \Delta u_{\parallel} / \delta \eta \delta \phi \rangle$ as a function of u_{\parallel} . The region between the arrows is populated by the W boson sample.

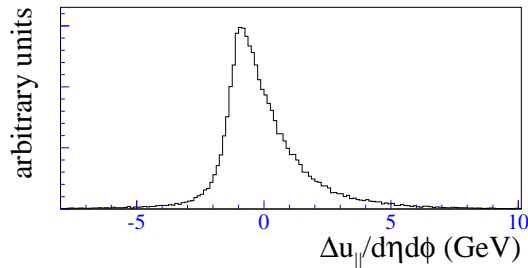


FIG. 22. The distribution of $\Delta u_{||}/\delta\eta\delta\phi$ in the W signal sample, corrected to $\mathcal{L}=0$, $|\eta|=2$, $u_{||}=0$.

in the window from the underlying event. ΔE_T is not equal to $\Delta u_{||}$ because the electron E_T is calculated by scaling the sum of the cell energies by the electron angle, whereas u_T is obtained by summing the E_T of each cell. The ratio of the two corrections as a function of electron η is shown in Fig. 23.

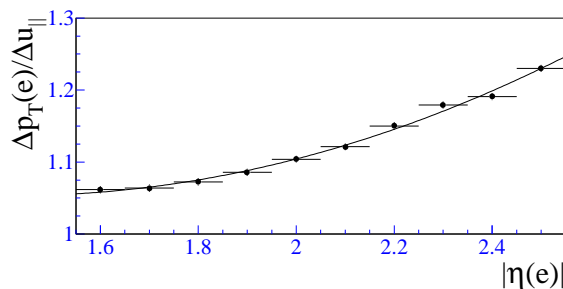


FIG. 23. The ratio of the $\langle\Delta u_{||}/\delta\eta\delta\phi\rangle$ corrections to the electron and the recoil as a function of electron η .

The uncertainty in the underlying event transverse energy density has a statistical component and a systematic component. The systematic component is derived from the difference between the measurement close to the electron (where it is biased by the isolation requirement) and far from the electron (where it is not biased). The total uncertainty in the underlying event transverse energy density is 28 MeV.

D. $u_{||}$ Efficiency

The efficiency for electron identification depends on the electron environment. Well-isolated electrons are identified correctly more often than electrons near other particles. Therefore W decays in which the electron is emitted in the same direction as the particles recoiling against the W boson are selected less often than W decays in which the electron is emitted in the direction opposite the recoiling particles. This causes a bias in the lepton p_T distributions, shifting $p_T(e)$ to larger values and $p_T(\nu)$ to lower values, whereas the m_T distribution is only slightly affected.

We measure the electron finding efficiency as a function of $u_{||}$ using $Z \rightarrow ee$ events. The Z event is tagged with one electron, and the other electron provides an unbiased measurement

of the efficiency. Following background subtraction, the measured efficiency is shown in Fig. 24. The line is a fit to a function of the form

$$\varepsilon(u_{\parallel}) = \varepsilon_0 \begin{cases} 1 & \text{for } u_{\parallel} < u_0 \\ 1 - s(u_{\parallel} - u_0) & \text{otherwise.} \end{cases} \quad (6.1)$$

The parameter ε_0 is an overall efficiency which is inconsequential for the W mass measurement, u_0 is the value of u_{\parallel} at which the efficiency starts to decrease as a function of u_{\parallel} , and s is the rate of decrease. We obtain the best fit for $u_0 = -2.4$ GeV and $s = 0.0029$ GeV $^{-1}$. These two values are strongly anti-correlated. The error on the slope $\delta s = \pm 0.0012$ GeV $^{-1}$ accounts for the statistics of the Z sample.

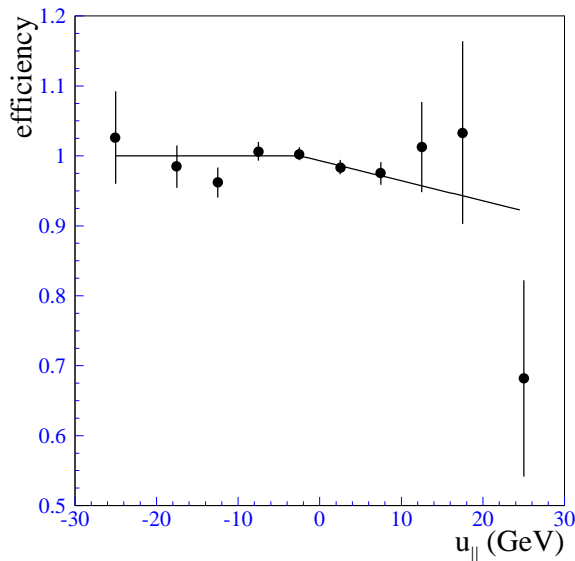


FIG. 24. The EC electron selection efficiency as a function of u_{\parallel} .

E. Electron Energy Response

Equation 3.1 relates the reconstructed electron energy to the recorded end calorimeter signals. Since the values for the constants were determined in the test beam, we determine the offset δ_{EC} and a scale α_{EC} , which essentially modifies A , *in situ* with collider $Z \rightarrow ee$ data.

The electrons from Z decays are not monoenergetic and therefore we can make use of their energy spread to constrain δ_{EC} . When both electrons are in the EC, we can write

$$m(ee) = \alpha_{\text{EC}} M_Z + f_Z \delta_{\text{EC}} \quad (6.2)$$

for $\delta_{\text{EC}} \ll E(e_1) + E(e_2)$. f_Z is a kinematic function related to the boost of the Z boson, and is given by $f_Z = [E(e_1) + E(e_2)](1 - \cos \omega)/m(ee)$, where ω is the opening angle between the two electrons. When one electron is in the CC and one is in the EC, we can write

$$m(ee) = \sqrt{\alpha_{CC}\alpha_{EC}}M_Z + f_Z\delta_{EC}, \quad (6.3)$$

where $f_Z = E(e_2)(1 - \cos\omega)/m(ee)$ and e_2 is the CC electron. When we apply this formula, we have already corrected the CC electron for the corresponding CCEM offset, $\delta_{CC} = -0.16$ GeV, which was measured for our CC W mass analysis [4].

We plot $m(ee)$ versus f_Z and extract δ_{EC} as the slope of the fitted straight line. We use the fast Monte Carlo to correct for residual biases introduced by the kinematic cuts. The δ_{EC} measurements from the CC/EC and EC/EC Z samples are shown in Fig. 25. We obtain the average $\delta_{EC} = -0.1 \pm 0.7$ GeV. The uncertainty in this measurement of δ_{EC} is dominated by the statistical uncertainty due to the finite size of the Z sample. As Fig. 25 shows, the offsets measured in the north and south end calorimeters separately are completely consistent.

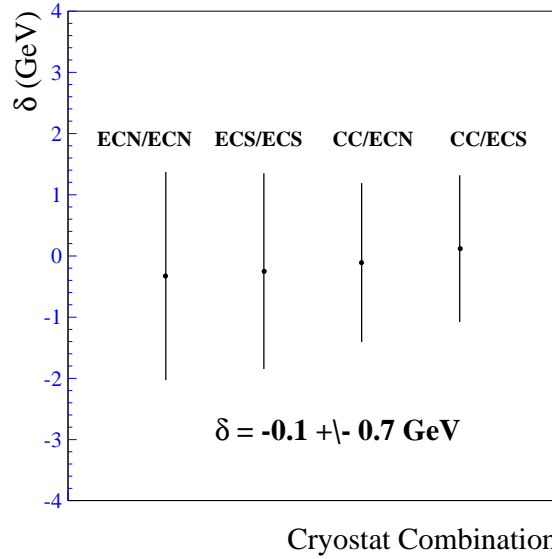


FIG. 25. The ECEM offset measurements using the CC/EC and EC/EC Z samples.

After correcting the data with this value of δ_{EC} we determine α_{EC} so that the position of the Z peak predicted by the fast Monte Carlo agrees with the data. To determine the scale factor that best fits the data, we perform a maximum likelihood fit to the $m(ee)$ spectrum between 70 GeV and 110 GeV. In the resolution function we allow for background shapes determined from samples of events with two EM clusters that fail the electron quality cuts (Fig. 26). The background normalization is obtained from the sidebands of the Z peak.

Figure 27 shows the $m(ee)$ spectrum for the CC/EC Z sample and the Monte Carlo spectrum that best fits the data for $\delta_{EC} = -0.1$ GeV. The χ^2 for the best fit to the CC/EC $m(ee)$ spectrum is 14 for 19 degrees of freedom. For $\alpha_{EC} = 0.95143 \pm 0.00259$, the Z peak position of the CC/EC sample is consistent with the known Z boson mass. The error reflects the statistical uncertainty. The background has no measurable effect on the result.

Figure 28 shows the $m(ee)$ spectrum for the EC/EC Z sample and the Monte Carlo spectrum that best fits the data for $\delta_{EC} = -0.1$ GeV. The χ^2 for the best fit to the EC/EC $m(ee)$ spectrum is 12 for 17 degrees of freedom. For $\alpha_{EC} = 0.95230 \pm 0.00231$, the Z peak position of the EC/EC sample is consistent with the known Z boson mass. The error reflects the statistical uncertainty and the uncertainty in the background.

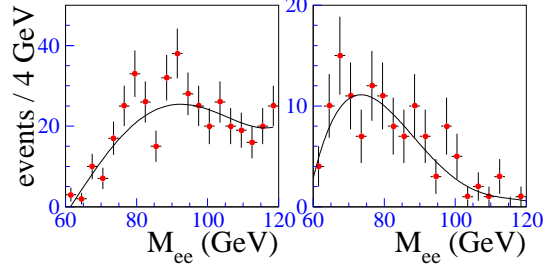


FIG. 26. The dielectron mass spectrum from the CC/EC (left) and EC/EC (right) samples of events with two EM clusters that fail the electron quality cuts. The superimposed curves shows the fitted functions used to model the shape of the background in the Z samples.

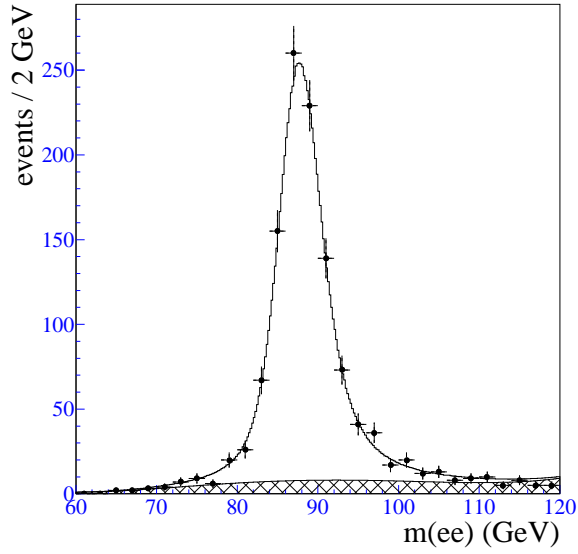


FIG. 27. The dielectron mass spectrum from the CC/EC Z sample. The superimposed curve shows the maximum likelihood fit and the shaded region the fitted background.

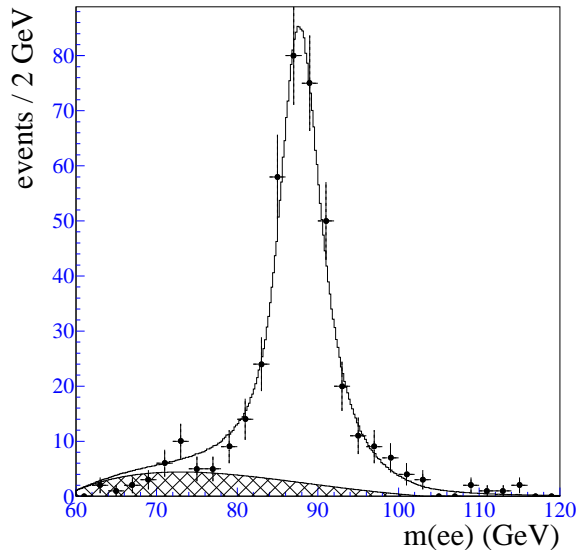


FIG. 28. The dielectron mass spectrum from the EC/EC Z sample. The superimposed curve shows the maximum likelihood fit and the shaded region the fitted background.

Combining the α_{EC} measurements from the CC/EC and the EC/EC Z samples, we obtain the ECEM energy scale

$$\alpha_{\text{EC}} = 0.95179 \pm 0.00187 \quad . \quad (6.4)$$

The difference between the ECEM scales measured separately in the north and south calorimeters is 0.0040 ± 0.0037 , consistent with the calorimeters having the same EM response.

F. Electron Energy Resolution

Equation 3.3 gives the functional form of the electron energy resolution. We take the intrinsic resolution of the end calorimeter, which is given by the sampling term s_{EM} , from the test beam measurements. The noise term n_{EM} is represented by the width of the electron underlying event energy distribution (Fig. 22). We measure the constant term c_{EM} from the Z line shape of the data. We fit a Breit-Wigner convoluted with a Gaussian, whose width characterizes the dielectron mass resolution, to the Z peaks for the CC/EC and EC/EC samples separately. Figure 29 shows the width $\sigma_{m(ee)}$ of the Gaussian fitted to the Z peak predicted by the fast Monte Carlo as a function of c_{EM} . The horizontal lines indicate the width of the Gaussian fitted to the Z samples and its uncertainties. For the data measurements of

$$\begin{aligned} \sigma_m &= 2.47 \pm 0.05 \text{ GeV (CC/EC)} \\ \sigma_m &= 2.72 \pm 0.11 \text{ GeV (EC/EC)} \end{aligned} \quad (6.5)$$

we extract from the CC/EC Z boson events $c_{\text{EC}} = 1.6^{+0.8\%}_{-1.6\%}$ and from the EC/EC Z events we extract $c_{\text{EC}} = 0.0^{+1.0\%}_{-0.0\%}$. We take the combined measurement to be

$$c_{\text{EC}} = 1.0^{+0.6}_{-1.0} \%. \quad (6.6)$$

The measured Z boson mass does not depend on c_{EC} .

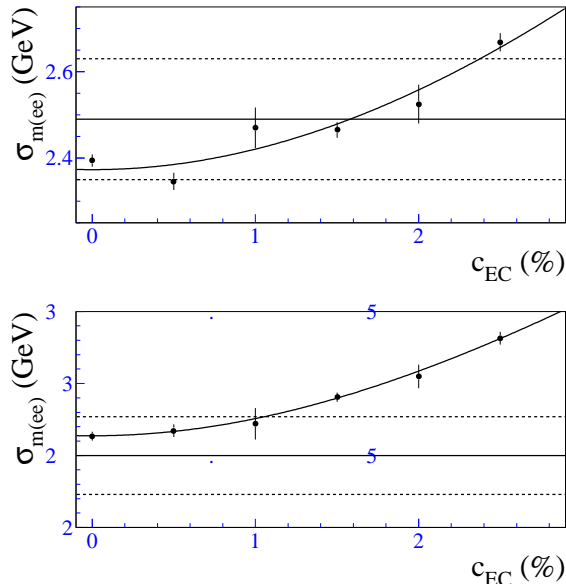


FIG. 29. The dielectron mass resolution versus the constant term c_{EM} . The top plot is for the CC/EC Z events and the bottom plot is for the EC/EC Z events.

VII. RECOIL MEASUREMENT

A. Recoil Momentum Response

The detector response and resolution for particles recoiling against a W boson should be the same as for particles recoiling against a Z boson. For $Z \rightarrow ee$ events, we can measure the transverse momentum of the Z boson from the e^+e^- pair, $p_T(ee)$, into which it decays, and from the recoil momentum u_T in the same way as for $W \rightarrow e\nu$ events. By comparing $p_T(ee)$ and u_T , we calibrate the recoil response relative to the electron response.

The recoil momentum is carried by many particles, mostly hadrons, with a wide momentum spectrum. Since the response of the calorimeter to hadrons is slightly nonlinear at low energies, and the recoil particles see a reduced response at module boundaries, we expect a momentum-dependent response function with values below unity. To fix the functional form of the recoil momentum response, we studied [4] the response predicted by a Monte Carlo $Z \rightarrow ee$ sample obtained using the HERWIG program and a GEANT-based detector simulation. We projected the reconstructed transverse recoil momentum onto the direction of motion of the Z boson and define the response as

$$R_{\text{rec}} = \frac{|\vec{u}_T \cdot \hat{q}_T|}{|q_T|}, \quad (7.1)$$

where q_T is the generated transverse momentum of the Z boson. A response function of the form

$$R_{\text{rec}} = \alpha_{\text{rec}} + \beta_{\text{rec}} \ln(q_T/\text{GeV}) \quad (7.2)$$

fits the response predicted by GEANT with $\alpha_{\text{rec}} = 0.713 \pm 0.006$ and $\beta_{\text{rec}} = 0.046 \pm 0.002$. This functional form also describes the jet energy response [42] of the DØ calorimeter.

The recoil response for data was calibrated against the electron response by requiring p_T balance in $Z \rightarrow ee$ decays for our published CC analysis [4]. The Z boson p_T measured with the electrons and the recoil are projected on the η axis, defined as the bisector of the two electron directions in the transverse plane. From the CC/CC + CC/EC Z boson events, we measured $\alpha_{\text{rec}} = 0.693 \pm 0.060$ and $\beta_{\text{rec}} = 0.040 \pm 0.021$, in good agreement with the Monte Carlo prediction. To compare the recoil response measured with Z events of different topologies, we scale the recoil measurement with the inverse of the response parametrization

$$R_{\text{rec}} = 0.693 + 0.04 \cdot \ln(p_T(ee)/\text{GeV}) \quad (7.3)$$

and plot the sum of the projections versus $p_\eta(ee)$, as shown in Fig. 30. We see no $p_\eta(ee)$ dependence to the p_η balance measured using the Z boson events with at least one central electron, since this sample was used to derive the values of these parameters. The EC/EC Z boson events give a recoil response measurement statistically consistent with the above. Hence we use the same recoil response for the EC and the CC W boson events [4].

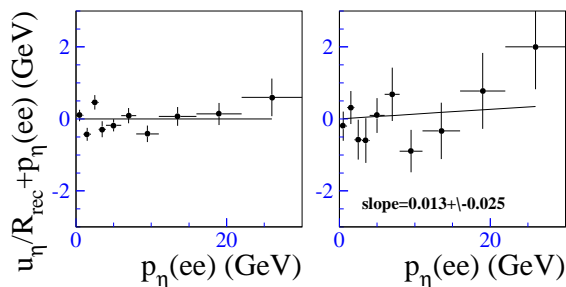


FIG. 30. The recoil momentum response in the CC/CC + CC/EC (left) and the EC/EC (right) Z samples as a function of $p_\eta(ee)$.

B. Recoil Momentum Resolution

The widths of the p_η balance and the p_ξ balance (where the ξ axis is perpendicular to the η axis) are sensitive to the recoil resolution. Figures 31–32 show the comparison between the data and Monte Carlo for the recoil resolution determined in our CC W mass analysis [4]. The p_η balance width is in good agreement between data and Monte Carlo for all Z boson topologies. Hence we use the same recoil resolution for EC W boson events as for the CC W boson events [4].

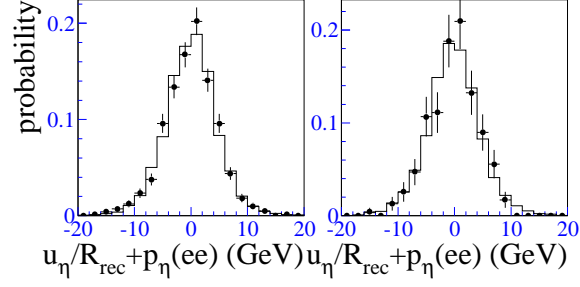


FIG. 31. The η -balance distribution for the Z boson data (\bullet) and the fast Monte Carlo simulation ($—$). The plot on the left is for the CC/CC + CC/EC Z events and the plot on the right is for the EC/EC Z events.

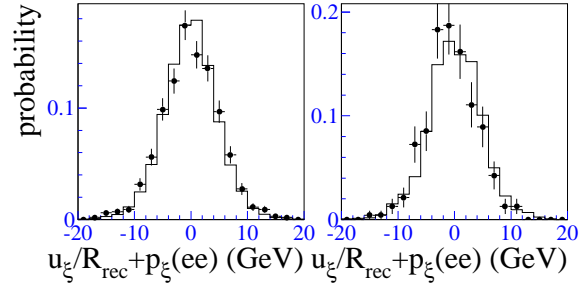


FIG. 32. The ξ -balance distribution for the Z boson data (\bullet) and the fast Monte Carlo simulation ($—$). The plot on the left is for the CC/CC + CC/EC Z events and the plot on the right is for the EC/EC Z events.

C. Comparison with W Boson Data

We compare the recoil momentum distributions in the W boson data to the predictions of the fast Monte Carlo, which includes the parameters described in this section and Sec. VI. Figure 33 shows the u_{\parallel} spectra from Monte Carlo and W data. The agreement means that the recoil momentum response and resolution and the u_{\parallel} efficiency parameterization describe the data well. Figures 34–36 show u_{\perp} , u_T , and the azimuthal difference between electron and recoil directions from Monte Carlo and W boson data. The figures also show the mean and r.m.s. of the data and Monte Carlo distributions and the χ^2 .

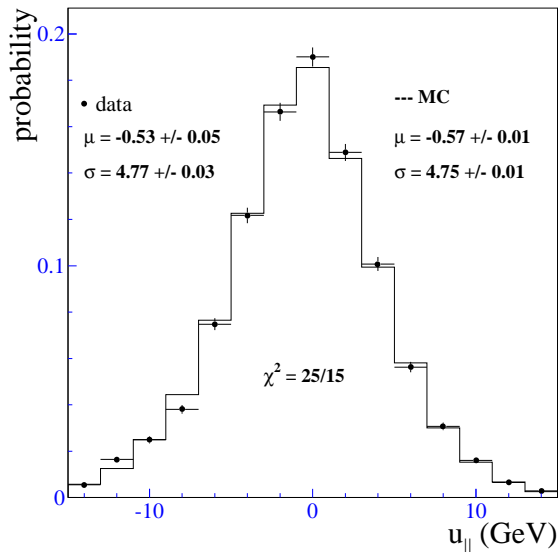


FIG. 33. The u_{\parallel} spectrum for the W data (\bullet) and the Monte Carlo simulation (—). The mean (μ) and r.m.s. (σ) of the distributions and the χ^2 is also shown.

VIII. CONSTRAINTS ON THE W BOSON RAPIDITY SPECTRUM

In principle, if the acceptance for the $W \rightarrow e\nu$ decays were complete, the transverse mass distribution or the lepton p_T distributions would be independent of the W rapidity. However, cuts on the electron angle in the laboratory frame cause the observed distributions of the transverse momenta to depend on the W rapidity. Hence a constraint on the W rapidity distribution is useful in constraining the production model uncertainty on the W mass.

The pseudorapidity distribution of the electron from $W \rightarrow e\nu$ decays is correlated with the rapidity distribution of the W boson. Therefore we can compare the electron η distribution between data and Monte Carlo.

To compare the data with the Monte Carlo, we need to correct for the jet background in the data and the electron identification efficiency as a function of η . We obtain the jet background fraction as a function of η by counting the number of W events that fail electron cuts (see Sec. IX B) in bins of η , subtracting the small contamination due to true electrons,

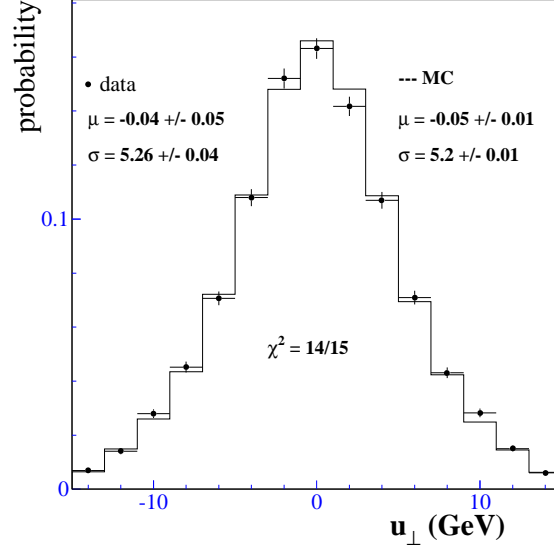


FIG. 34. The u_{\perp} spectrum for the W data (\bullet) and the Monte Carlo simulation ($—$). The mean (μ) and r.m.s. (σ) of the distributions and the χ^2 is also shown.

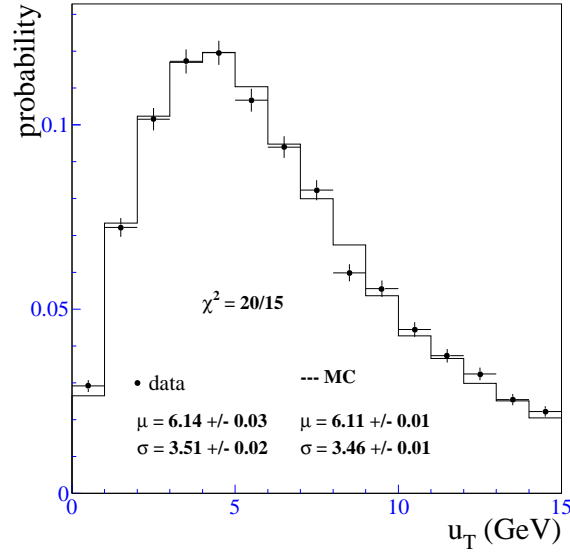


FIG. 35. The recoil momentum (u_T) spectrum for the W data (\bullet) and the Monte Carlo simulation ($—$). The mean (μ) and r.m.s. (σ) of the distributions and the χ^2 is also shown.

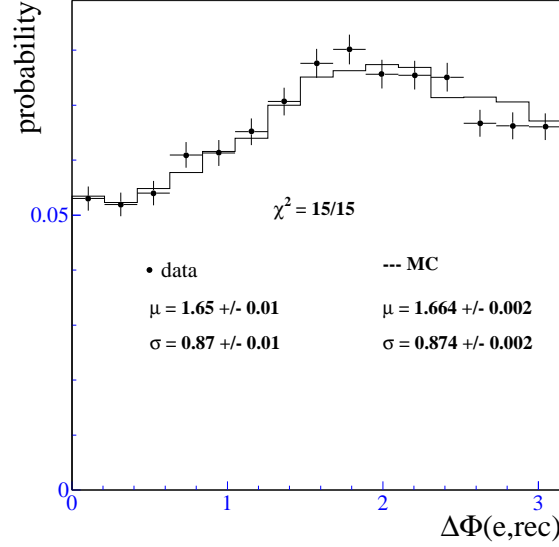


FIG. 36. The azimuthal difference between electron and recoil directions for the W data (\bullet) and the Monte Carlo simulation (—). The mean (μ) and r.m.s. (σ) of the distributions and the χ^2 is also shown.

and normalizing the entire distribution to the total background fraction (separately in the CC and EC). The normalized background η distribution is subtracted from the η distribution of the data.

The electron identification efficiency (after fiducial and kinematic cuts) is measured using the CC/CC and CC/EC $Z \rightarrow ee$ events. All the electron identification cuts are used to identify one electron to tag the event. Candidates are selected in the mass range $81 < m_{ee} < 101$ GeV. Sidebands in the mass range $60 < m_{ee} < 70$ GeV and $110 < m_{ee} < 120$ GeV are used for background subtraction. The number of events in which the second electron also satisfies all the electron identification cuts is used to calculate the efficiency. The efficiency measured in bins of the η of the second electron is shown in Fig. 37.

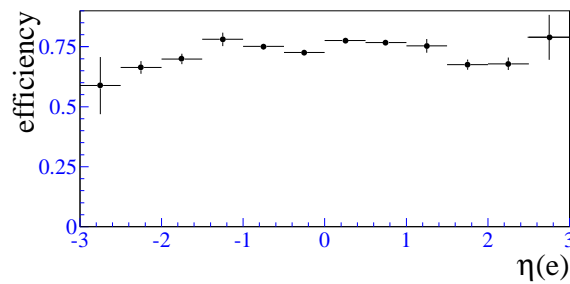


FIG. 37. Dependence of electron identification efficiency on electron pseudorapidity. Statistical errors are shown.

We scale the electron η distribution predicted by the Monte Carlo by the η -dependent efficiency, and compare to the background-subtracted data in Fig. 38. The errors on the Monte Carlo points include the statistical errors on the Monte Carlo sample and the statistical errors on the efficiency measurements. The errors on the data points include the statisti-

cal errors on the number of candidate events and the statistical errors on the background estimate which has been subtracted. Figure 39 shows the ratio between the background-subtracted data and the efficiency-corrected Monte Carlo, with the uncertainties mentioned above added in quadrature. The Monte Carlo has been normalized to the data. The χ^2 shown is with respect to unity. There is good agreement between the data and the Monte Carlo.

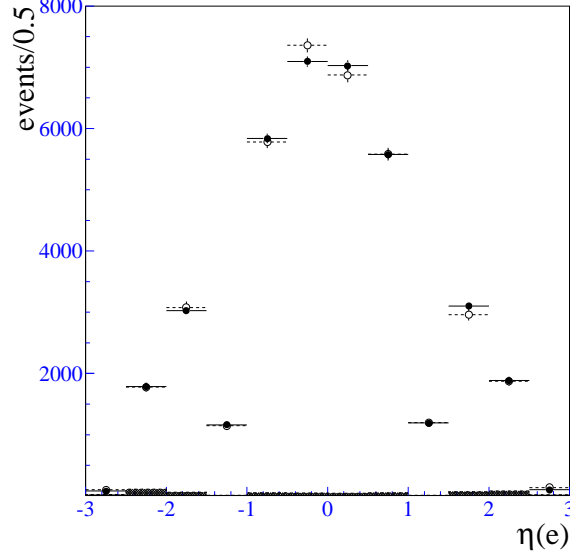


FIG. 38. η distribution of the electron from $W \rightarrow e\nu$ decays from background-subtracted data (\bullet), efficiency-corrected Monte Carlo (\circ) and the jet background (shaded histogram). The distributions drop near $|\eta| = 1.2$ because there is no EM calorimetry in the range $1.1 < |\eta_{\text{det}}| < 1.4$.

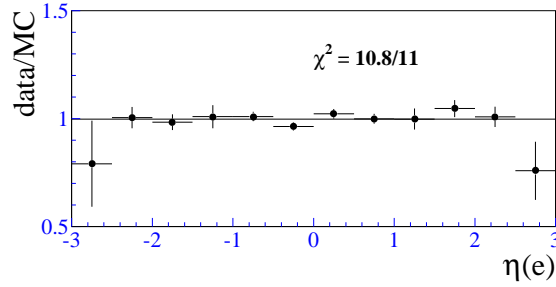


FIG. 39. The ratio of the background-subtracted data and efficiency-corrected Monte Carlo. The Monte Carlo has been normalized to the data. The χ^2 is with respect to unity.

To extract a constraint on the y distribution of the W boson, we introduce in the Monte Carlo a scale factor as follows:

$$y_W \rightarrow k_\eta \cdot y_W \quad (8.1)$$

i.e. the rapidity of the W is scaled by the factor k_η . We then compute the χ^2 between the data and Monte Carlo $\eta(e)$ distributions for different k_η . The result is shown in Fig. 40 for

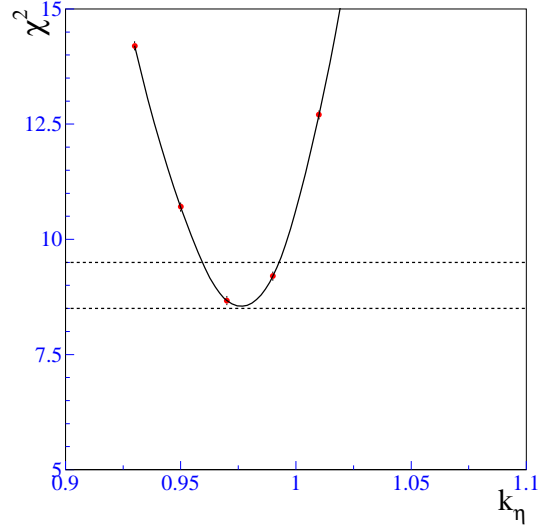


FIG. 40. χ^2 of the electron η distribution ratio between data and Monte Carlo from unity, as a function of the W rapidity scale factor k_η . There are 11 degrees of freedom. The Monte Carlo uses the MRS(A') parton distribution functions. The horizontal lines indicate χ^2_{\min} and $\chi^2_{\min} + 1$.

the MRS(A') [43] parton distribution functions. Table IV shows the values of k_η at which the χ^2 is minimized for the different pdf's.

The uncertainty in k_η is 1.6%, which is the change in k_η that causes the χ^2 to rise by one unit above the minimum. We generate Monte Carlo events with different values of k_η and fit them with templates generated with k_η set to unity. For a k_η variation of 1.6%, the variation of the fitted W mass in the EC is shown in Table V.

TABLE IV. Value of k_η giving the minimum χ^2 for different pdf's.

MRS(A') [43]	CTEQ3M [44]	CTEQ2M [45]	MRSD-' [46]
0.975	0.98	0.985	0.99

TABLE V. Variation in fitted EC W mass due to a 1.6% variation in k_η .

	m_T fit	$p_T(e)$ fit	$p_T(\nu)$ fit
δM_W (MeV)	34	48	25

The comparison of the electron η distribution between the data and the Monte Carlo provides a consistency check of the predicted W rapidity distribution, and hence of the pdf's.

The measured k_η being consistent with unity² sets an upper bound on the pdf uncertainty. While this constraint can potentially be much more powerful with higher statistics obtained in future data-taking, it is presently weaker than the uncertainty in the modern pdf's. Therefore we do not use this constraint to set our final W mass uncertainty due to pdf's. However, since our data used for this constraint are independent of the world data used to derive the pdf's, we have additional evidence that the uncertainty on the W mass due to the pdf's is not being underestimated.

IX. BACKGROUNDS

A. $W \rightarrow \tau\nu \rightarrow e\nu\bar{\nu}\nu$

The decay $W \rightarrow \tau\nu \rightarrow e\nu\bar{\nu}\nu$ is topologically indistinguishable from $W \rightarrow e\nu$. It is included in the fast Monte Carlo simulation (Sec. V). This decay is suppressed by the branching fraction for $\tau \rightarrow e\nu\bar{\nu}$ ($17.83 \pm 0.08\%$) [19], and by the lepton p_T cuts. It accounts for 1% of the events in the W sample.

B. Hadronic Background

QCD processes can fake the signature of a $W \rightarrow e\nu$ decay if a hadronic jet fakes the electron signature and the transverse momentum balance is mismeasured.

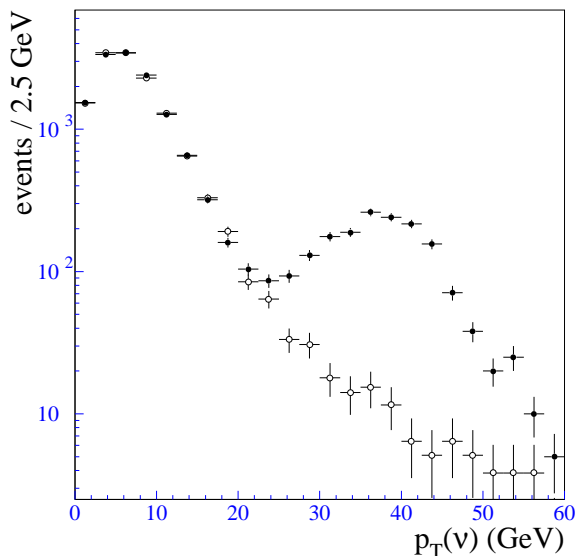


FIG. 41. The p_T spectra of a sample of events passing electron identification cuts (●) and a sample of events failing the cuts (○).

²We have used $k_\eta = 1$ in the mass analysis.

We estimate this background from the \cancel{p}_T spectrum of data events with an electromagnetic cluster. Electromagnetic clusters in events with low \cancel{p}_T are almost all due to jets. Some of these clusters satisfy our electron selection criteria and fake an electron. From the shape of the \cancel{p}_T spectrum for these events we determine how likely it is for these events to have sufficient \cancel{p}_T to enter our W sample.

We determine this shape by selecting isolated electromagnetic clusters that have $\chi^2 > 200$ and the 4-variable likelihood $\lambda_4 > 30$. Nearly all electrons fail this cut, so that the remaining sample consists almost entirely of hadrons. We use data collected using a trigger without the \cancel{p}_T requirement to study the efficiency of this cut for jets. If we normalize the background spectrum after correcting for residual electrons to the electron sample, we obtain an estimate of the hadronic background in an electron candidate sample. Figure 41 shows the \cancel{p}_T spectra of both samples, normalized for $\cancel{p}_T < 10$ GeV. We find the hadronic background fraction of the total W sample after all cuts to be $f_{\text{had}} = (3.64 \pm 0.78)\%$. The error receives contributions from the uncertainty in the relative normalization of the two samples at low \cancel{p}_T , the statistics of the failed electron sample, and the uncertainty in the residual contamination of the failed electron sample by true electrons. We fit the distributions of the background events with $\cancel{p}_T > 30$ GeV to estimate the shape of the background contributions to the $p_T(e)$, $p_T(\nu)$, and m_T spectra (Fig. 42). We use the statistical error of the fits to estimate the uncertainty in the background shapes.

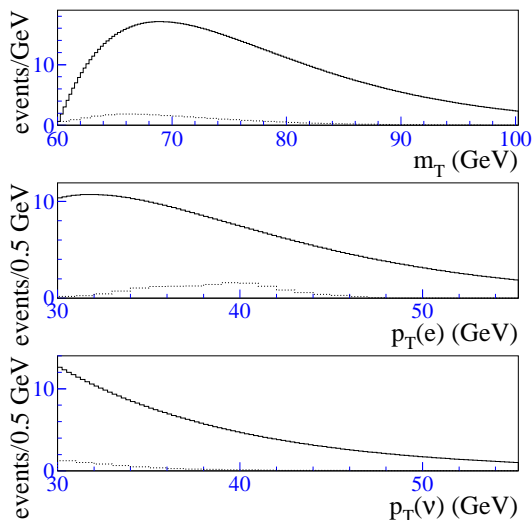


FIG. 42. Shapes of m_T , $p_T(e)$, and $p_T(\nu)$ spectra from hadron (—) and Z boson (- -) backgrounds with the proper relative normalization.

C. $Z \rightarrow ee$

To estimate the fraction of $Z \rightarrow ee$ events that satisfy the W boson event selection, we use a Monte Carlo sample of approximately 100,000 $Z \rightarrow ee$ events generated with the HERWIG program and a detector simulation based on GEANT. The boson p_T spectrum

generated by HERWIG agrees reasonably well with the calculation in Ref. [29] and with our Z boson p_T measurement [50]. $Z \rightarrow ee$ decays typically enter the W sample when one electron satisfies the W cuts and the second electron is lost or mismeasured, causing the event to have large \cancel{p}_T .

An electron is most frequently mismeasured when it goes into the regions between the CC and one of the ECs, which are covered only by the hadronic section of the calorimeter. These electrons therefore cannot be identified, and their energy is measured in the hadronic calorimeter. Large \cancel{p}_T is more likely for these events than when both electrons hit the EM calorimeters.

We make the W and Z selection cuts on the Monte Carlo events, and normalize the number of events passing the W cuts to the number of W data events, scaled by the ratio of selected Z data and Monte Carlo events. We estimate the fraction of Z events in the W sample to be $f_Z = (0.26 \pm 0.02)\%$. The uncertainties quoted include systematic uncertainties in the matching of momentum scales between Monte Carlo and collider data. Figure 42 shows the distributions of $p_T(e)$, $p_T(\nu)$, and m_T for the Z events with one lost or mismeasured electron that satisfy the W selection.

X. MASS FITS

A. Maximum Likelihood Fitting Procedure

We use a binned maximum likelihood fit to extract the W mass. Using the fast Monte Carlo program, we compute the m_T , $p_T(e)$, and $p_T(\nu)$ spectra for 200 hypothesized values of the W mass between 79.7 and 81.7 GeV. For the spectra we use 250 MeV bins. The statistical precision of the spectra for the W mass fit corresponds to about 8 million W decays. When fitting the collider data spectra, we add the background contributions with the shapes and normalizations described in Sec. IX to the signal spectra. We normalize the spectra within the fit interval and interpret them as probability density functions to compute the likelihood

$$L(m) = \prod_{i=1}^N p_i^{n_i}(m), \quad (10.1)$$

where $p_i(m)$ is the probability density for bin i , assuming $M_W = m$, and n_i is the number of data entries in bin i . The product runs over all N bins inside the fit interval. We fit $-\ln[L(m)]$ with a quadratic function of m . The value of m at which the function assumes its minimum is the fitted value of the W mass and the 68% confidence level interval is the interval in m for which $-\ln[L(m)]$ is within half a unit of its minimum.

B. Electron p_T Spectrum

We fit the $p_T(e)$ spectrum in the region $32 < p_T(e) < 50$ GeV. The interval is chosen to span the Jacobian peak. The data points in Fig. 43 represent the $p_T(e)$ spectrum from the

W sample. The solid line shows the sum of the simulated W signal and the estimated background for the best fit, and the shaded region indicates the sum of the estimated hadronic and $Z \rightarrow ee$ backgrounds. The maximum likelihood fit gives

$$M_W = 80.547 \pm 0.128 \text{ GeV} \quad (10.2)$$

for the W mass. Figure 44 shows $-\ln(L(m)/L_0)$ for this fit, where L_0 is an arbitrary number.

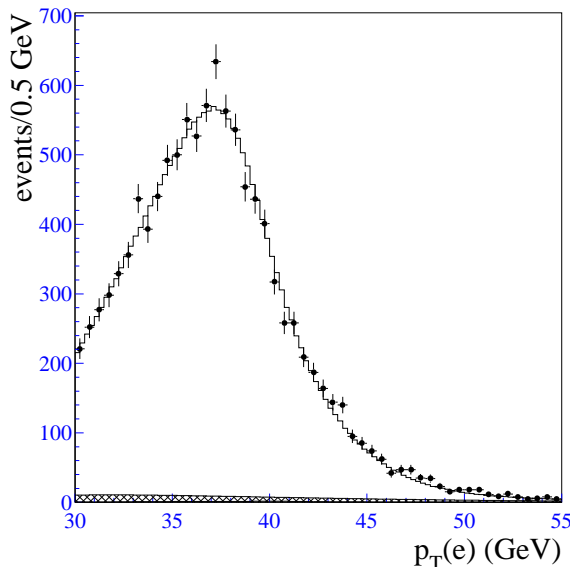


FIG. 43. Spectrum of $p_T(e)$ from the W data. The superimposed curve shows the maximum likelihood fit and the shaded region the estimated background.

As a goodness-of-fit test, we divide the fit interval into 0.5 GeV bins, normalize the integral of the probability density function to the number of events in the fit interval, and compute $\chi^2 = \sum_{i=1}^N (y_i - P_i)^2 / y_i$. The sum runs over all N bins, y_i is the observed number of events in bin i , and P_i is the integral of the normalized probability density function over bin i . The parent distribution is the χ^2 distribution for $N - 2$ degrees of freedom. For the spectrum in Fig. 43 we compute $\chi^2 = 46$. For 36 bins there is a 8% probability for $\chi^2 \geq 46$. Figure 45 shows the contributions $\chi_i = (y_i - P_i) / \sqrt{y_i}$ to χ^2 for the 36 bins in the fit interval.

Figure 46 shows the sensitivity of the fitted mass value to the choice of fit interval. The points in the two plots indicate the observed deviation of the fitted mass from the value given in Eq. 10.2. We expect some variation due to statistical fluctuations in the spectrum and systematic uncertainties in the probability density functions. We estimate the effect due to statistical fluctuations using Monte Carlo ensembles. We expect the fitted values to be inside the shaded regions indicated in the two plots with 68% probability. The dashed lines indicate the statistical error for the nominal fit. Figure 46 shows that the probability density function provides a good description of the observed spectrum.

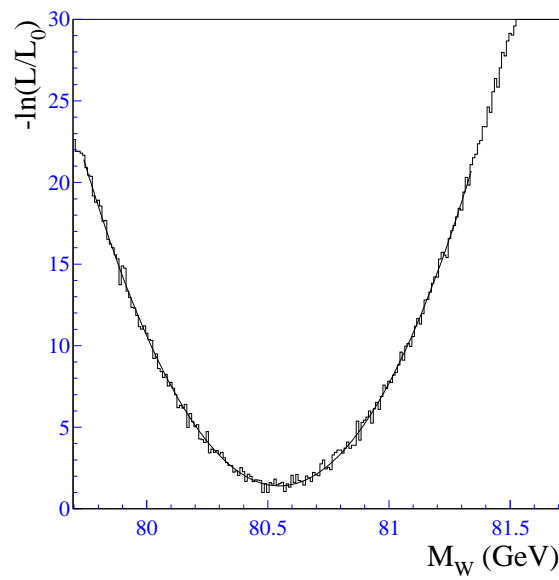


FIG. 44. The likelihood function for the $p_T(e)$ fit.

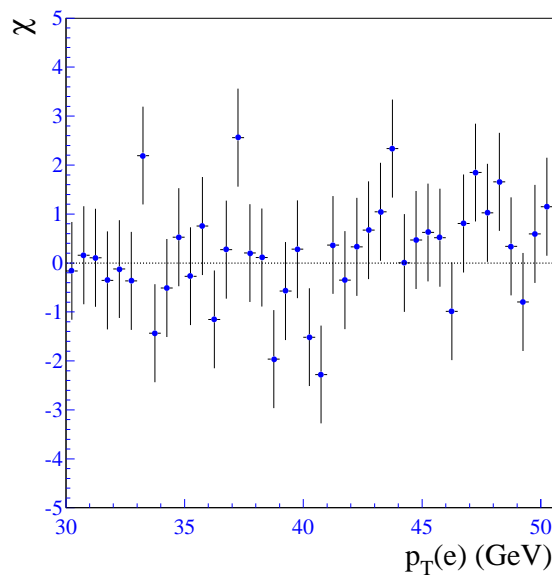


FIG. 45. The χ distribution for the fit to the $p_T(e)$ spectrum.

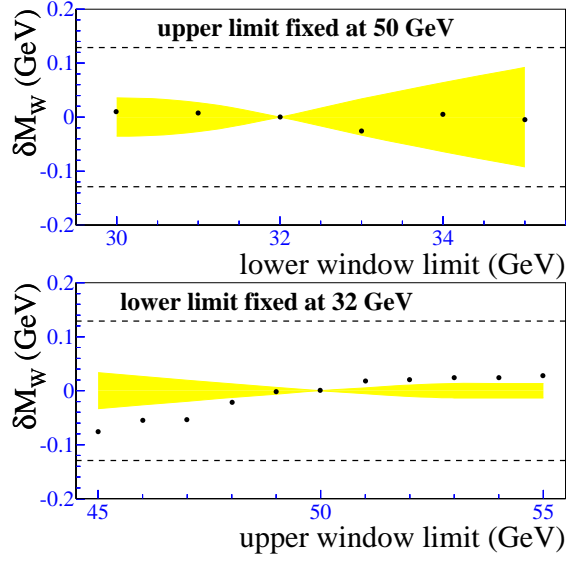


FIG. 46. Variation of the fitted mass with the $p_T(e)$ fit window limits. See text for details.

C. Transverse Mass Spectrum

The m_T spectrum is shown in Fig. 47. The points are the observed spectrum, the solid line shows signal plus background for the best fit, and the shaded region indicates the estimated background contamination. We fit in the interval $65 < m_T < 90$ GeV. Figure 48 shows $-\ln(L(m)/L_0)$ for this fit where L_0 is an arbitrary number. The best fit occurs for

$$M_W = 80.757 \pm 0.107 \text{ GeV}. \quad (10.3)$$

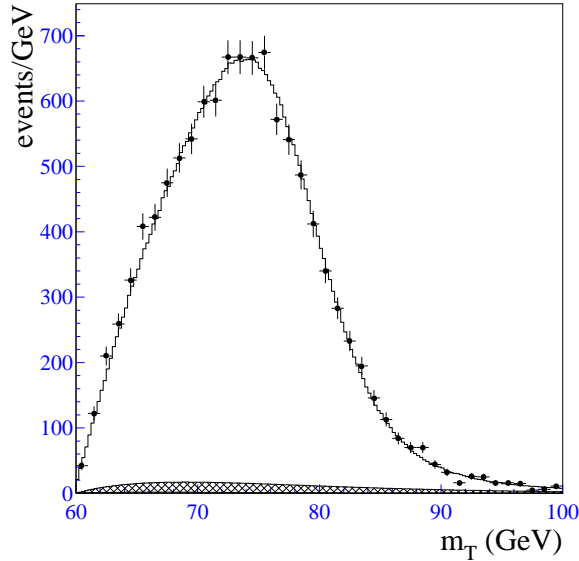


FIG. 47. Spectrum of m_T from the W data. The superimposed curve shows the maximum likelihood fit and the shaded region shows the estimated background.

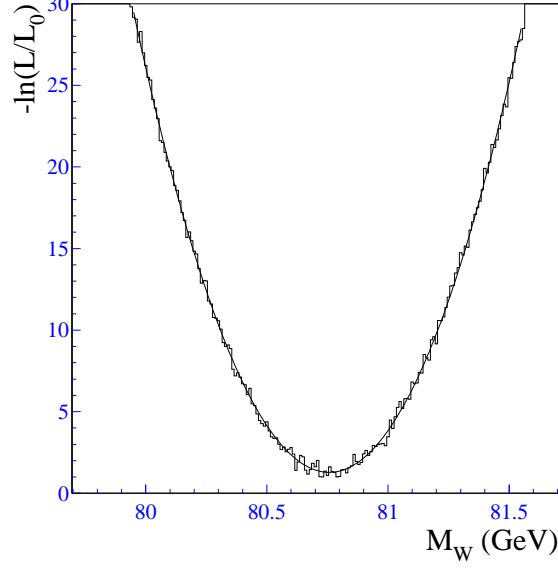


FIG. 48. The likelihood function for the m_T fit.

Figure 49 shows the deviations of the data from the fit. Summing over all bins in the fitting window, we get $\chi^2 = 17$ for 25 bins. For 25 bins there is a 81% probability to obtain a larger value. Figure 50 shows the sensitivity of the fitted mass to the choice of fit interval.

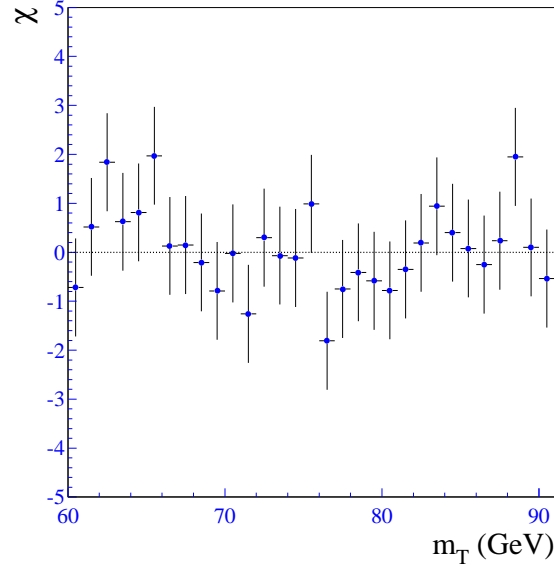


FIG. 49. The χ distribution for the fit to the m_T spectrum.

D. Neutrino p_T Spectrum

Figure 51 shows the neutrino p_T spectrum. The points are the observed spectrum, the solid line shows signal plus background for the best fit, and the shaded region indicates the

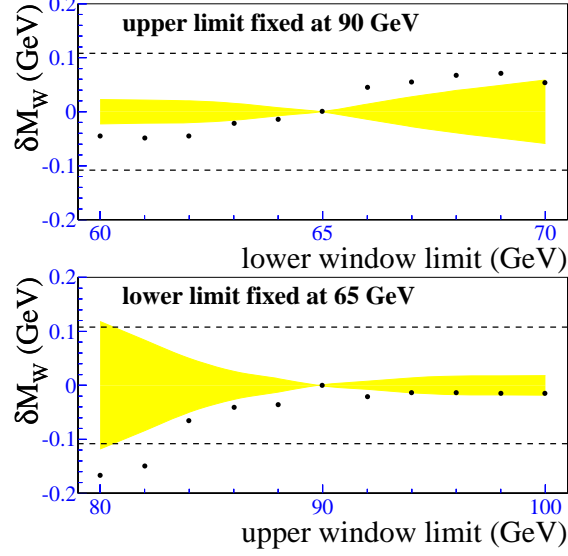


FIG. 50. Variation of the fitted mass with the m_T fit window limits. See text for details.

estimated background contamination. We fit in the interval $32 < p_T(\nu) < 50$ GeV. Figure 52 shows $-\ln(L(m)/L_0)$ for this fit where L_0 is an arbitrary number. The best fit occurs for

$$M_W = 80.740 \pm 0.159 \text{ GeV}. \quad (10.4)$$

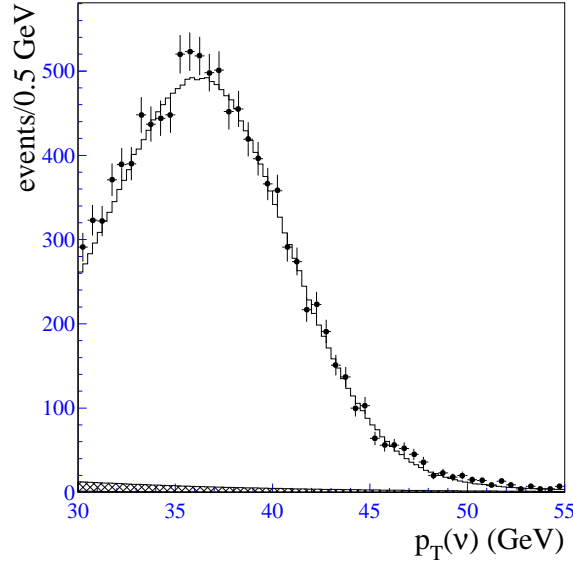


FIG. 51. Spectrum of $p_T(\nu)$ from the W data. The superimposed curve shows the maximum likelihood fit and the shaded region shows the estimated background.

Figure 53 shows the deviations of the data from the fit. Summing over all bins in the fitting window, we get $\chi^2 = 37$ for 36 bins. For 36 bins there is a 33% probability to obtain a larger value. Figure 54 shows the sensitivity of the fitted mass to the choice of fit interval.

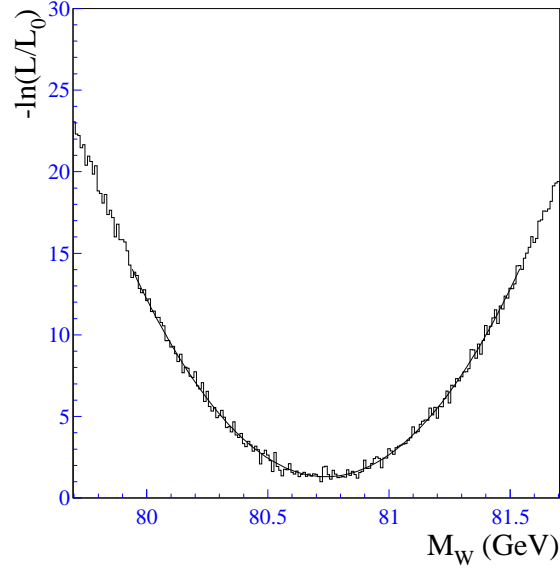


FIG. 52. The likelihood function for the $p_T(\nu)$ fit.

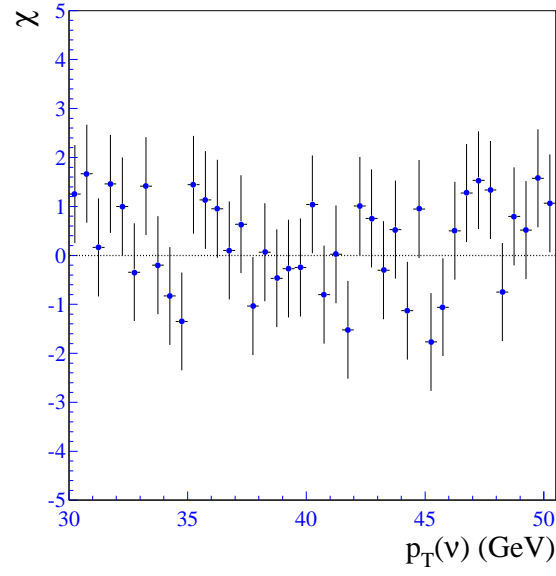


FIG. 53. The χ distribution for the fit to the $p_T(\nu)$ spectrum.

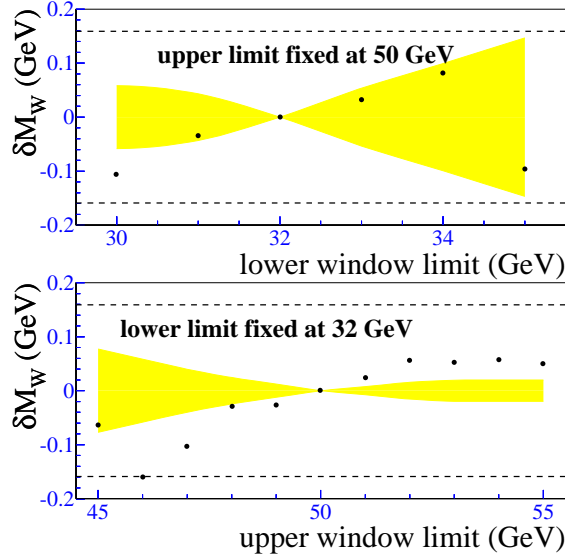


FIG. 54. Variation of the fitted mass with the $p_T(\nu)$ fit window limits. See text for details.

XI. CONSISTENCY CHECKS

A. North vs South Calorimeters

Since the detector is north-south symmetric, we expect the measurements made with the north and south calorimeters separately to be consistent. We find

$$\begin{aligned}
 M_W^{\text{ECN}} - M_W^{\text{ECS}} &= 88 \pm 215 \text{ MeV } (m_T \text{ fit}) \\
 M_W^{\text{ECN}} - M_W^{\text{ECS}} &= -116 \pm 258 \text{ MeV } (p_T^e \text{ fit}) \\
 M_W^{\text{ECN}} - M_W^{\text{ECS}} &= 107 \pm 318 \text{ MeV } (p_T^\nu \text{ fit})
 \end{aligned} \tag{11.1}$$

where the uncertainty is statistical only.

B. Time Dependence

We divide the W boson data sample into five sequential calendar time intervals such that the subsamples have equal number of events. We generate resolution functions for the luminosity distribution of these five subsamples. We fit the transverse mass and lepton p_T spectra from the W samples in each time bin. The fitted masses are plotted in Fig. 55 where the time bins are labelled by run blocks. The errors shown are statistical only. We compute the χ^2 with respect to the W mass fit to the entire data sample. The χ^2 per degree of freedom (dof) for the $p_T(e)$ fit is 7.0/4 and for the $p_T(\nu)$ fit is 1.5/4. The m_T fit has a χ^2/dof of 2.1/4.

Since the luminosity was increasing with time throughout the run, the time slices correspond roughly to luminosity bins.

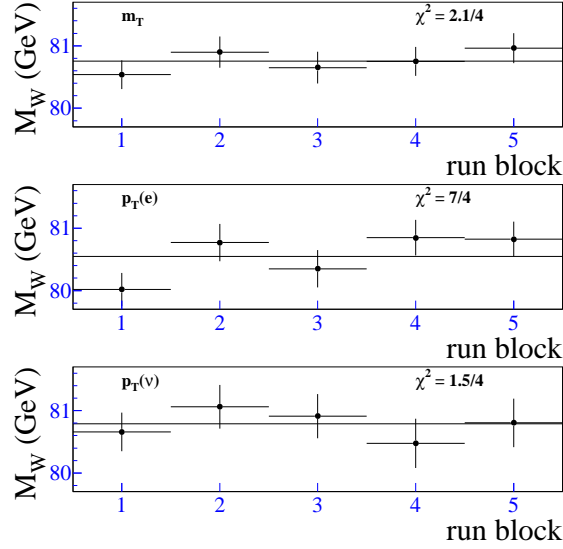


FIG. 55. The fitted W boson masses in bins of run blocks from the m_T , $p_T(e)$, and $p_T(\nu)$ fits. The solid line is the central value for the respective fit over the entire sample. The W fit statistical error for each subsample is shown. The average instantaneous luminosity in the bins is 4.2, 6.1, 7.1, 9.3 and 10.1 respectively, in units of $10^{30}/\text{cm}^2/\text{s}$.

C. Dependence on u_T Cut

We change the cuts on the recoil momentum u_T and study how well the fast Monte Carlo simulation reproduces the variations in the spectra. We split the W sample into subsamples with $u_{\parallel} > 0$ GeV and $u_{\parallel} < 0$ GeV, and fit the subsamples with corresponding Monte Carlo spectra generated with the same cuts. The difference in the fitted masses from the two subsamples corresponds to 0.3σ , 0.8σ and 1.3σ for the m_T , $p_T(e)$, and $p_T(\nu)$ fits respectively, based on the statistical uncertainty alone. Although there is significant variation among the shapes of the spectra for the different cuts, the fast Monte Carlo models them well.

D. Dependence on Fiducial Cuts

We fit the m_T spectrum from the W sample and the $m(ee)$ spectrum from the Z sample for different pseudorapidity cuts on the electron direction. Keeping the upper $|\eta_{\text{det}}(e)|$ cut fixed at 2.5, we vary the lower $|\eta_{\text{det}}(e)|$ cut from 1.5 to 1.7. Similarly, we vary the upper $|\eta_{\text{det}}(e)|$ cut from 2.0 to 2.5, keeping the lower $|\eta_{\text{det}}(e)|$ cut fixed at 1.5. Figures 56–58 show the change in the W mass versus the $\eta_{\text{det}}(e)$ cut using the electron energy scale calibration from the corresponding Z sample. The shaded region indicates the statistical error. Within the uncertainties, the mass is independent of the $\eta_{\text{det}}(e)$ cut.

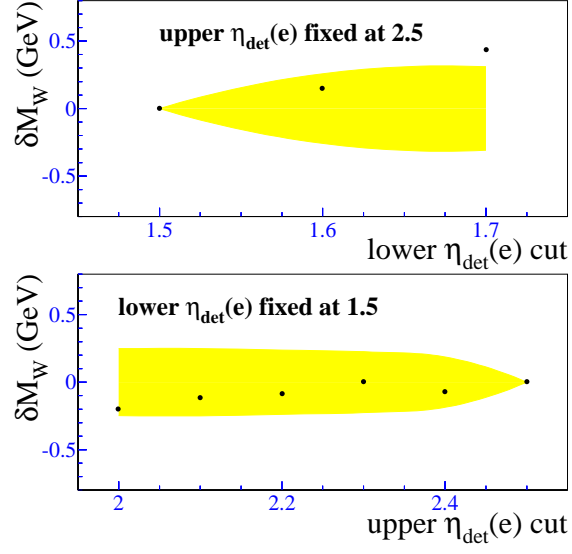


FIG. 56. The variation in the W mass from the $p_T(e)$ fit versus the $\eta_{\text{det}}(e)$ cut. The shaded region is the expected statistical variation.

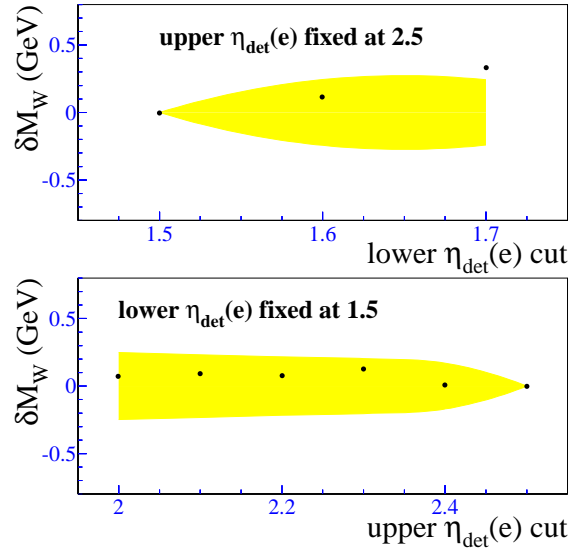


FIG. 57. The variation in the W mass from the m_T fit versus the $\eta_{\text{det}}(e)$ cut. The shaded region is the expected statistical variation.

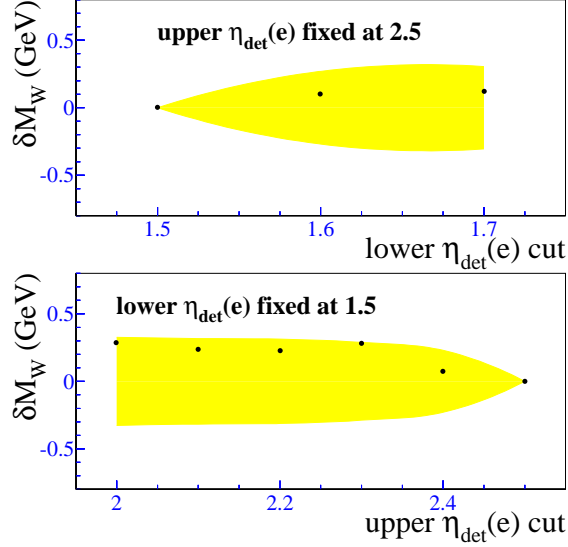


FIG. 58. The variation in the W mass from the $p_T(\nu)$ fit versus the $\eta_{\text{det}}(e)$ cut. The shaded region is the expected statistical variation.

E. Z Boson Transverse Mass Fits

As a consistency check, we fit the transverse mass distribution of the $Z \rightarrow ee$ events, reconstructed using each electron and the recoil. The measured energy of the second electron is ignored, both in the data and in the Monte Carlo used to obtain the templates. Each Z event is treated (twice) as a W event, where the neutrino transverse momentum is recomputed using the first electron and the recoil. One of the two electrons is required to be in the EC. The fitting range is $70 < m_T < 90$ GeV for the CC/EC events and $70 < m_T < 100$ GeV for the EC/EC events. Figure 59 shows the results. The CC/EC fit yields $M_Z = 92.004 \pm 0.895(\text{stat})$ GeV with $\chi^2/\text{dof} = 7/9$. The EC/EC fit yields $M_Z = 91.074 \pm 0.299(\text{stat})$ GeV with $\chi^2/\text{dof} = 16/14$. The average fitted mass is $M_Z = 91.167 \pm 0.284(\text{stat})$ GeV. The fits are good and the fitted masses are consistent with the input Z mass.

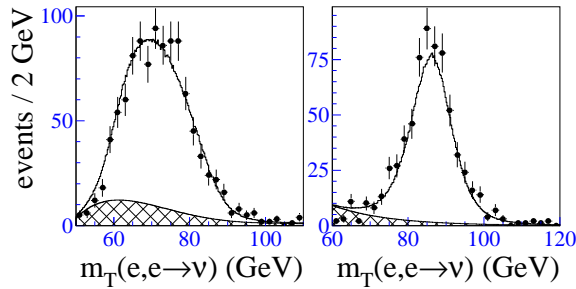


FIG. 59. Spectra of the Z boson transverse mass, from the CC/EC data (left) and the EC/EC data (right). The superimposed curves show the maximum likelihood fits and the shaded regions show the estimated backgrounds.

XII. UNCERTAINTIES IN THE MEASUREMENT

Apart from the statistical error in the fitted W mass, uncertainties in the various inputs needed for the measurement lead to uncertainties in the final result. Some of these inputs are discrete (such as the choice of the parton distribution function set) and others are parameterized by continuous variables. For a different choice of pdf set, or a shift in the value of an input parameter by one standard deviation, the expected shift in the fitted W mass is computed by using the fast Monte Carlo to generate spectra with the changed parameter and fitting the spectra with the default templates. The expected shifts due to various input parameter uncertainties (given in Table VI) or choice of pdf set are discussed in detail below, and are summarized in Tables VII and VIII. The shifts in the fitted mass obtained from the different kinematic spectra may be in opposite directions, in which case they are indicated with opposite signs.

TABLE VI. Errors on the parameters in the W mass analysis. The correlation coefficient between α_{rec} and β_{rec} is -0.98 ; that between s_{rec} and α_{mb} is -0.60 .

parameter	error
parton luminosity β	0.001 GeV^{-1}
photon coalescing radius R_0	7 cm
W width	59 MeV
ECEM offset δ_{EC}	0.7 GeV
ECEM scale α_{EC}	0.00187
FDC radial scale β_{FDC}	0.00054
FDC-EC radial scale β_{EC}	0.0003
ECEM constant term c_{EC}	$^{+0.006}_{-0.01}$
recoil response ($\alpha_{\text{rec}}, \beta_{\text{rec}}$)	(0.06, 0.02)
recoil resolution ($s_{\text{rec}}, \alpha_{\text{mb}}$)	(0.14 $\text{GeV}^{1/2}$, 0.028) \oplus (0.0, 0.01)
u_{\parallel} correction $\Delta u_{\parallel}/\delta\eta\delta\phi$	28 MeV
u_{\parallel} efficiency slope s	0.0012 GeV^{-1}

Since the most important parameter, the EM energy scale, is measured by calibrating to the Z mass, we are measuring the ratio of the W and Z boson masses. There can be significant cancellation in uncertainties between the W and Z masses if their variation due to an input parameter change is very similar. For those parameters that affect the fitted Z mass, Tables VII and VIII also show the expected shift in the fitted Z mass. The signed W and Z mass shifts are used to construct a covariance matrix between the various fitted W mass results, which is used to obtain the final W mass value and uncertainty; thus simple combination of the uncertainties in Tables VII and VIII is inappropriate. This is discussed in detail in Section XIII.

TABLE VII. Variation in the fitted M_W and M_Z (in MeV) for the forward electron sample due to variation in the model input parameters by the respective uncertainties.

Source	δM_Z (CC/EC)	δM_Z (EC/EC)	δM_W (m_T)	δM_W (p_T^e)	δM_W (p_T^ν)
statistics	124	221	107	128	159
$p_T(W)$ spectrum			22	37	44
MRSR2 [47]			-11	-21	-43
MRS(A') [43]			-7	-43	-19
CTEQ5M [48]			14	9	-17
CTEQ4M [49]			1	-21	22
CTEQ3M [44]			13	30	28
parton					
luminosity β	8	7	9	11	18
R_0	10	13	9	17	12
2γ	5	10	5	10	0
W width			10	10	10
ECEM offset	284	421	437	433	386
ECEM scale					
variation 0.0025	114	228	201	201	201
CCEM scale					
variation 0.0008	37	0	0	0	0
FDC radial scale	8	36	43	37	28
FDC-EC radial scale	10	52	57	54	48
ECEM constant					
term c_{EC}	0	0	45	29	78
hadronic					
response			11	20	-50
hadronic					
resolution			40	4	203
$u_{ }$ correction	20	30	18	34	-6
$u_{ }$ efficiency			4	-22	40
background					
normalization	0	11	12	15	25
background					
shape	0	5	16	23	78

TABLE VIII. Variation in the fitted M_W and M_Z (in MeV) for the central electron sample due to variation in the model input parameters by the respective uncertainties.

Source	δM_Z (CC/CC)	δM_Z (CC/EC)	δM_W (m_T)	δM_W (p_T^e)	δM_W (p_T^ν)
statistics	75	124	70	85	105
$p_T(W)$ spectrum			10	50	25
MRSR2 [47]			5	26	3
MRS(A') [43]			-5	16	-31
CTEQ5M [48]			-8	6	-22
CTEQ4M [49]			10	11	-18
CTEQ3M [44]			0	64	-9
parton					
luminosity β	4	8	9	11	9
R_0	19	10	3	6	0
2γ	10	5	3	6	0
W width			10	10	10
CC EM offset	387	467	367	359	374
CDC scale	29	33	38	40	52
uniformity			10	10	10
CCEM constant					
term c_{CC}			23	14	27
hadronic					
response			20	16	-46
hadronic					
resolution			25	10	90
u_{\parallel} correction			15	15	20
u_{\parallel} efficiency			2	-9	20
backgrounds			10	20	20

A. Statistical Uncertainties

Tables VII and VIII list the uncertainties in the W mass measurement due to the finite sizes of the W and Z samples used in the fits to the m_T , $p_T(e)$, $p_T(\nu)$, and $m(ee)$ spectra. The statistical uncertainty due to the finite Z sample propagates into the W mass measurement through the electron energy scale α_{EC} .

Since the m_T , $p_T(e)$ and $p_T(\nu)$ fits are performed using the same W data set, the results from the three fits are statistically correlated. The correlation coefficients between the respective statistical errors are calculated using Monte Carlo ensembles, and are shown in Table IX.

TABLE IX. The statistical correlation coefficients obtained from Monte Carlo ensemble tests fitting the W boson mass for 260 samples of 11,089 events each.

	correlation matrix		
	m_T	$p_T(e)$	$p_T(\nu)$
m_T	1	0.634	0.601
$p_T(e)$	0.634	1	0.149
$p_T(\nu)$	0.601	0.149	1

B. W Boson Production and Decay Model

1. Sources of Uncertainty

Uncertainties in the W boson production and decay model arise from the following sources: the phenomenological parameters in the calculation of the $p_T(W)$ spectrum, the choice of parton distribution functions, radiative decays, and the W boson width. In the following we describe how we assess the size of the systematic uncertainties introduced by each of these. We summarize the size of the uncertainties in Tables VII and VIII.

2. W Boson p_T Spectrum

In Sec. VIII of Ref. [4], we described our constraint on the W boson p_T spectrum. This constraint was obtained by studying the Z boson p_T spectrum, which can be measured well using the two electrons in $Z \rightarrow ee$ decays. For any chosen parton distribution function, the parameters of the theoretical model were tuned so that the predicted Z boson p_T spectrum after simulating all detector effects agreed with the data. The precision with which the parameters could be tuned was limited by the statistical uncertainty and the uncertainty in the background. These parameter values were used to predict the W boson p_T spectrum.

The uncertainties in the fitted W boson mass for the CC W sample due to the uncertainty in the W boson p_T spectrum were listed in Ref. [4], and are reproduced in Table VIII. The corresponding uncertainty in the EC analysis is given in Table VII. The CC and EC W mass uncertainty from this source is assumed to be fully correlated.

3. Parton Distribution Functions

To quantify the W mass uncertainty due to variations in the input parton distribution functions, we select the MRS(A'), MRSR2, CTEQ5M, CTEQ4M and CTEQ3M sets to compare to MRST. We select these sets because their predictions for the lepton charge asymmetry in W decays and the neutron-to-proton Drell-Yan ratio span the range of consistency with the measurements from CDF [51] and E866 [52]. These measurements constrain the ratio of u and d quark distributions, which has the most influence on the W rapidity spectrum.

Using these parton distribution function sets as input to the fast Monte Carlo model, we generate m_T and lepton p_T spectra. For each chosen parton distribution function set we use the appropriate W boson p_T spectrum as used in our CC W mass analysis. We then fit the generated spectra in the same way as the spectra from collider data, i.e. using MRST parton distribution functions. Table VII lists the variation of the fitted EC W mass values relative to MRST. The CC and EC W mass uncertainty from this source is taken to be fully correlated, taking the relative signs of the mass shifts into account.

We find that the combination of the CC and EC W boson mass measurements is less sensitive to pdf variations, than for the CC measurement alone. The pdf uncertainty on the CC measurement is 11 MeV. The pdf uncertainty on the CC+EC combined measurement is 7 MeV. As expected, the larger combined rapidity coverage makes the observed transverse mass and transverse momentum distributions less sensitive to the longitudinal boost of the W boson.

4. Parton Luminosity

The uncertainty of 10^{-3} GeV^{-1} in the parton luminosity slope β (Sec. V) translates into an uncertainty in the fitted W and Z boson masses. We estimate the sensitivity in the fitted W and Z masses by fitting Monte Carlo spectra generated with different values of β . The uncertainty in β is taken to be fully correlated between the CC and EC W mass analyses.

5. Radiative Decays

We assign an error to the modeling of radiative decays based on varying the detector parameter R_0 (Sec. V). R_0 defines the maximum separation between the photon and electron directions above which the photon energy is not included in the electron shower. In general, radiation shifts the fitted mass down for the transverse mass and electron fits, because for a fraction of the events the photon energy is subtracted from the electron. Hence increasing R_0 decreases the radiative shift. Both the fitted W and Z masses depend on R_0 . To estimate the

systematic error, we fit Monte Carlo spectra generated with different values of R_0 . GEANT detector simulations show that, for an R_0 variation of ± 7 cm, the electron-photon cluster overlap changes to give the maximum variation in the electron identification efficiency. The changes in the mass fits when varying R_0 by ± 7 cm are listed in Table VII.

There are also theoretical uncertainties in the radiative decay calculation. Initial state QED radiation is not included in the calculation of Ref. [40]. However, initial state radiation does not affect the kinematic distributions used to fit the mass in the final state. Finally, the calculation includes only processes in which a single photon is radiated. We use the code provided by the authors of Ref. [53] to estimate the shift introduced in the measured W and Z masses by neglecting two-photon emission. The estimated shifts in the W and Z fitted masses due to two-photon radiation are shown in Table VII. Since this effect is an order of magnitude smaller than the statistical uncertainty in our measurement we do not correct for it, but add it in quadrature to the uncertainty due to radiative corrections. The uncertainty in the radiative correction is taken to be fully correlated between the CC and EC W mass analyses.

6. W Boson Width

The uncertainty on the fitted W mass corresponds to the uncertainty in the measured value of the W boson width $\Gamma_W = 2.062 \pm 0.059$ GeV [35]. We take this uncertainty to be fully correlated between the CC and EC W mass analyses.

Our recent measurement of the W width [54] considerably improves the precision of Γ_W and would reduce the W mass uncertainty from this source. However, since this is already a small source of uncertainty, the impact on the total W mass uncertainty is small.

C. Detector Model Parameters

The uncertainties on the parameters of the detector model determined in Secs. VI–VII translate into uncertainties in the W mass measurement. We study the sensitivity of the W mass measurement to the values of the parameters by fitting the data with spectra generated by the fast Monte Carlo with input parameters modified by ± 1 standard deviation.

Table VII lists the uncertainties in the measured EC W mass due to the individual parameters. For each item the uncertainty is determined to typically 5 MeV. To achieve this precision, 10–20 million $W \rightarrow e\nu$ decays are simulated for each item.

The residual calorimeter nonlinearity is parametrized by the offset δ_{EC} . The electron momentum resolution is parametrized by c_{EM} . The electron angle calibration includes the effects of the parameters β_{FDC} and β_{EC} , discussed in Section VI. The recoil response is parameterized by α_{rec} and β_{rec} . The recoil resolution is parameterized by s_{rec} and α_{mb} . Electron removal refers to the bias Δu_{\parallel} introduced in the u_{\parallel} measurement by the removal of the cells occupied by the electron. Selection bias refers to the u_{\parallel} efficiency.

D. Backgrounds

We determine the sensitivity of the fit results to the assumed background normalizations and shapes by repeating the fits to the data with background shapes and normalizations modified by ± 1 standard deviation. Table VII lists the uncertainties introduced in the EC W boson mass measurement.

XIII. COMBINED EC AND CC W BOSON MASS ERROR ANALYSIS

The measurement of the W mass requires the knowledge of many parameters in our model of the W production, decay and detector response. These parameters are constrained by measurements, and in some cases by theoretical input. The W mass error analysis involves the propagation of the measurement or theoretical uncertainties to the error matrix on the parameters, which is then propagated further to the error matrix on the CC and EC W mass measurements. The error matrix allows us to combine the fitted W mass values using the different data samples and techniques into a single value with a combined error.

We identify the following parameters of relevance to the W mass measurements in the EC and CC:

- W mass statistical errors $\delta\omega_{CC}$ and $\delta\omega_{EC}$
- EM scales α_{CC} and α_{EC}
- EM offset parameters δ_{CC} and δ_{EC}
- FDC scale β_{FDC} and FDC-EC relative scale β_{EC}
- CDC scale β_{CDC}
- EM resolutions (constant terms) c_{CC} and c_{EC}
- recoil response \vec{a}_{rec} representing jointly the response parameters α_{rec} and β_{rec}
- recoil resolution \vec{q}_{rec} representing jointly the hadronic sampling term s_{rec} and the effects of the underlying event α_{mb}
- backgrounds b_{CC} and b_{EC}
- $u_{||}$ corrections u_{CC} and u_{EC}
- $u_{||}$ efficiencies ε_{CC} and ε_{EC}
- radiative corrections as a function of coalescing radius R_0
- parton luminosity β
- theoretical modeling \vec{t}

We take the EM scales, EM offsets, angular scales, $u_{||}$ corrections, parton luminosity and the radiative correction to be a set of parameters that jointly determine the measured W and Z masses. We also take the EM resolution parameters as a correlated set. We take the CC and EC backgrounds and $u_{||}$ efficiencies to be uncorrelated. The recoil modelling and the theoretical modelling (including pdf's, $p_T(W)$ spectrum, parton luminosity, radiative corrections and W width) are treated as being common between the CC and the EC analyses. For all correlated parameters the sign of the W mass correlation is determined by the relative sign of the mass shifts.

The following measurements provide information on the values of these parameters

- The Z mass measurements $M_Z^{\text{CC/CC}}$, $M_Z^{\text{CC/EC}}$ and $M_Z^{\text{EC/EC}}$
- FDC radial calibration θ_{FDC} and FDC-EC relative radial calibration θ_{EC}
- CDC z calibration θ_{CDC}
- CC and EC EM offset measurements o_{CC} and o_{EC}
- Gaussian width fitted to Z boson peak $\sigma_Z^{\text{CC/CC}}$, $\sigma_Z^{\text{CC/EC}}$ and $\sigma_Z^{\text{EC/EC}}$
- p_T balance in Z events
- width of p_T balance in Z events
- measurements of $u_{||}$ correction and $u_{||}$ efficiency
- constraints on theoretical model (boson p_T from $D\bar{O}$ data, W width from world data including $D\bar{O}$ data, and pdf's and parton luminosity from world data)

We express the variations on the various calibration quantities (such as Z mass, EM offset, and angular scales, collectively referred to as \vec{C}) and the Z width measurements as a linear combination of the variations on the parameters

$$\begin{aligned}\delta\vec{C} &= \Delta_C \delta\vec{p} \\ \delta\vec{\sigma}_Z &= \Delta_\sigma \delta\vec{c}_{\text{EM}}\end{aligned}\tag{13.1}$$

where

$$\begin{aligned}\delta\vec{C} &= (\delta M_Z^{\text{CC/CC}}, \delta M_Z^{\text{CC/EC}}, \delta M_Z^{\text{EC/EC}}, \delta\theta_{\text{FDC}}, \delta\theta_{\text{EC}}, \\ &\quad \delta\theta_{\text{CDC}}, \delta o_{\text{CC}}, \delta o_{\text{EC}}, \delta R_0, \delta u_{\text{CC}}, \delta u_{\text{EC}}, \delta\beta), \\ \delta\vec{p} &= (\delta\alpha_{\text{CC}}, \delta\alpha_{\text{EC}}, \delta\beta_{\text{FDC}}, \delta\beta_{\text{EC}}, \delta\beta_{\text{CDC}}, \\ &\quad \delta\delta_{\text{CC}}, \delta\delta_{\text{EC}}, \delta R_0, \delta u_{\text{CC}}, \delta u_{\text{EC}}, \delta\beta)\end{aligned}\tag{13.2}$$

and

$$\begin{aligned}\delta\vec{\sigma}_Z &= (\delta\sigma_Z^{\text{CC/CC}}, \delta\sigma_Z^{\text{CC/EC}}, \delta\sigma_Z^{\text{EC/EC}}), \\ \delta\vec{c}_{\text{EM}} &= (\delta c_{\text{CC}}, \delta c_{\text{EC}}).\end{aligned}\tag{13.3}$$

The Δ matrices contain the partial derivatives of the observables with respect to the parameters.

Similarly, the variations on the W mass are related linearly to the parameter variations

$$\begin{aligned}
\delta \vec{M}_W &= \Delta_W \delta \vec{p} \\
&+ \Delta_{\sigma_W} \delta \vec{c}_{\text{EM}} \\
&+ \Delta_{\text{recoil scale}} \delta \vec{a}_{\text{rec}} \\
&+ \Delta_{\text{recoil resolution}} \delta \vec{q}_{\text{rec}} \\
&+ \Delta_{\text{background}} \delta \vec{b} \\
&+ \Delta_u \delta \vec{u} \\
&+ \Delta_\varepsilon \delta \vec{\varepsilon} \\
&+ \Delta_{\text{theory}} \delta \vec{t} \\
&+ \delta \vec{\omega}
\end{aligned} \tag{13.4}$$

where $\delta \vec{M}_W = (\delta M_W^{\text{CC}}, \delta M_W^{\text{EC}})$.

Knowing the components of $\delta \vec{C}$ and $\delta \vec{\sigma}_Z$, we compute the covariance matrix for the parameters in \vec{p} and \vec{c}_{EM} . Since there are more measurements than parameters, we use the generalized least squares fitting procedure for this purpose. We then propagate the parameter covariance matrices into the covariance matrix for the CC and EC W mass measurements using equation 13.4, by identifying the covariance matrix with the expected value of $\delta \vec{M}_W (\delta \vec{M}_W)^T$, where T indicates the transpose. The various contributions to $\delta \vec{M}_W$ are independent, hence they contribute additively to the total covariance matrix.

The CC W mass measurements [4] were obtained using the MRS(A') parton distribution functions. We adjust these measurements by the estimated shifts (see Table VIII) when using the MRST parton distribution functions. Thus we use the following W mass values extracted from the CC data to combine with our EC measurements:

$$\begin{aligned}
M_W^{\text{CC}} &= 80.443 \text{ GeV } (m_T \text{ fit}) \\
M_W^{\text{CC}} &= 80.459 \text{ GeV } (p_T(e) \text{ fit}) \\
M_W^{\text{CC}} &= 80.401 \text{ GeV } (p_T(\nu) \text{ fit})
\end{aligned} \tag{13.5}$$

The combined W mass M_W for a set of n W mass measurements m_i and their covariance matrix V is given by

$$M_W = \left(\sum_{i,j=1}^n H_{ij} m_j \right) / \left(\sum_{i,j=1}^n H_{ij} \right), \tag{13.6}$$

where $H \equiv V^{-1}$ and i, j run over the W mass measurements being combined. The combined error is given by

$$\sigma(M_W) = \left(\sum_{i,j=1}^n H_{ij} \right)^{-1/2}, \tag{13.7}$$

and the χ^2 for the combination is given by

$$\chi^2 = \sum_{i,j=1}^n (m_i - M_W) H_{ij} (m_j - M_W). \tag{13.8}$$

XIV. RESULTS

We use the covariance matrix described above to obtain the total uncertainty on the EC W mass measurements and to combine our CC and EC measurements. We obtain the following results for the transverse mass fit

$$\begin{aligned} M_W^{\text{EC}} &= 80.757 \pm 0.107(\text{stat}) \pm 0.204(\text{syst}) \text{ GeV} \\ &= 80.757 \pm 0.230 \text{ GeV} \end{aligned} \quad (14.1)$$

and

$$M_W = 80.504 \pm 0.097 \text{ GeV (CC and EC combined)}. \quad (14.2)$$

The χ^2 for the CC+EC m_T combination is 1.5 for one degree of freedom, with a probability of 23%.

Similarly, for the $p_T(e)$ fit we obtain

$$\begin{aligned} M_W^{\text{EC}} &= 80.547 \pm 0.128(\text{stat}) \pm 0.203(\text{syst}) \text{ GeV} \\ &= 80.547 \pm 0.240 \text{ GeV} \end{aligned} \quad (14.3)$$

and

$$M_W = 80.480 \pm 0.126 \text{ GeV (CC and EC combined)}. \quad (14.4)$$

The χ^2 for the CC+EC $p_T(e)$ combination is 0.1 with a probability of 74%.

For the $p_T(\nu)$ fit we obtain

$$\begin{aligned} M_W^{\text{EC}} &= 80.740 \pm 0.159(\text{stat}) \pm 0.310(\text{syst}) \text{ GeV} \\ &= 80.740 \pm 0.348 \text{ GeV} \end{aligned} \quad (14.5)$$

and

$$M_W = 80.436 \pm 0.171 \text{ GeV (CC and EC combined)}. \quad (14.6)$$

The χ^2 for the CC+EC $p_T(\nu)$ combination is 1.0 with a probability of 32%.

The combination of the m_T , $p_T(e)$ and $p_T(\nu)$ fit values for the EC give the combined EC W mass result

$$M_W = 80.691 \pm 0.227 \text{ GeV}. \quad (14.7)$$

The χ^2/dof is 4.0/2, with a probability of 14%.

We combine all six measurements (CC and EC fits with the three techniques) to obtain the combined 1994–1995 measurement

$$M_W = 80.498 \pm 0.095 \text{ GeV}. \quad (14.8)$$

The χ^2/dof is 5.1/5, with a probability of 41%. The consistency of the six results indicates that we understand the ingredients of our model and their uncertainties. Including the measurement from the 1992–1993 data gives the 1992–1995 data measurement:

TABLE X. W mass uncertainties (in MeV) in the EC measurement and the combined CC+EC measurement from the 1994–1995 data.

Source	EC	CC+EC
W statistics	108	61
Z statistics	181	59
calorimeter linearity	52	25
calorimeter uniformity	–	8
electron resolution	42	19
electron angle calibration	20	10
recoil response	17	25
recoil resolution	42	25
electron removal	4	12
selection bias	5	3
backgrounds	20	9
pdf	17	7
parton luminosity	2	4
$p_T(W)$	25	15
$\Gamma(W)$	10	10
radiative corrections	1	12

$$M_W = 80.482 \pm 0.091 \text{ GeV}. \quad (14.9)$$

Table X lists the DØ W mass measurement uncertainties from the 1994–1995 end calorimeter data alone and the combined 1994–1995 central and end calorimeter data.

The DØ measurement is in good agreement with other measurements and is more precise than previously published results. Table XI lists previously published measurements with uncertainties below 500 MeV, except previous DØ measurements which are subsumed into this measurement. A global fit to all electroweak measurements excluding the direct W mass measurements predicts $M_W = 80.367 \pm 0.029$ GeV [11]. Figure 60 gives a graphical representation of these data.

TABLE XI. Previously published measurements of the W boson mass.

measurement	M_W (GeV)	reference
CDF 90	79.910 ± 0.390	[55]
UA2 92	80.360 ± 0.370	[12]
CDF 95	80.410 ± 0.180	[13]
L3 99	80.610 ± 0.150	[14]
ALEPH 99	80.423 ± 0.124	[15]
OPAL 99	80.380 ± 0.130	[16]
DELPHI 99	80.270 ± 0.145	[17]
DØ 99 combined (this result)	80.482 ± 0.091	

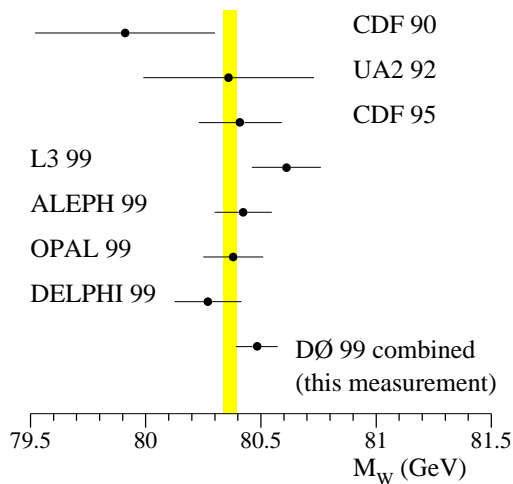


FIG. 60. A comparison of this measurement with previously published W boson mass measurements (Table XI). The shaded region indicates the predicted W boson mass value from global fits to the Z boson lineshape data [11].

We evaluate the radiative corrections Δr , defined in Eq. 1.1. Our measurement of M_W from Eq. 14.9 leads to

$$\Delta r = -0.0322 \pm 0.0059, \quad (14.10)$$

5.5 standard deviations from the tree level value, demonstrating the need for higher-order electroweak loop corrections. In Fig. 61 we compare the measured W boson and top quark masses [20] from DØ with the values predicted by the standard model for a range of Higgs mass values [56]. Also shown is the prediction from the calculation in Ref. [22] for a model involving supersymmetric particles assuming the chargino, Higgs, and left-handed selectron masses are greater than 90 GeV. The measured values are in agreement with the prediction of the standard model, and in even better agreement with a supersymmetric extension of the standard model.

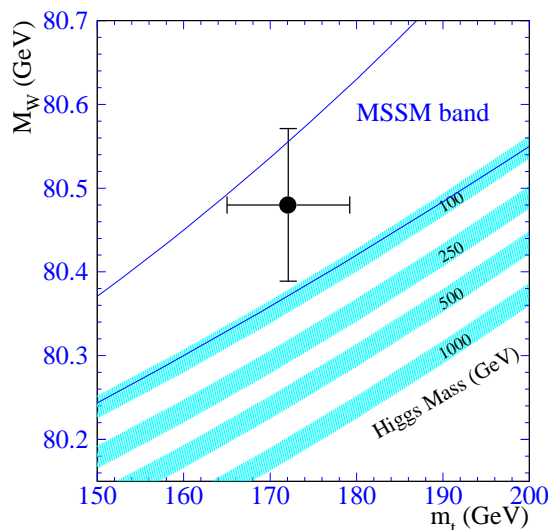


FIG. 61. A comparison of the W boson and top quark mass measurements by the DØ collaboration with the standard model predictions for different Higgs boson masses [56]. The width of the bands for each Higgs boson mass value indicates the uncertainty due to the error in $\alpha(M_Z^2)$. Also shown is the range allowed by the MSSM [22].

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