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# Search for pair-produced heavy scalars in $\mathbf{Z}^{0}$ decays 

DELPHI Collaboration


#### Abstract

A search for charged Higgs bosons decaying into quarks is described, based on statistics of around 1.7 million hadronic $Z^{0}$ decays detected in DELPHI. Despite the very high background from standard hadronic decays of the $Z^{0}$, masses in the range up to $43.5 \mathrm{GeV} / c^{2}$ are excluded at the $95 \%$ confidence level. After combination with a search for leptonic decays, this mass limit is extended to cover all branching ratios. A similar analysis sets new limits on the possible production of any pair-produced heavy scalar decaying into a pair of jets, such as neutral Higgs bosons in a two doublet scheme and diquarks.


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[^0]
## 1 Introduction

The $Z^{0}$ boson decay is an ideal environment for the direct search for new particles. Heavy scalars are predicted by different models, in particular a charged Higgs boson is present in all non-minimal Standard Models. This analysis is devoted to a search for the pair production of such particles in $\mathrm{e}^{+} \mathrm{e}^{-}$collisions at the $\mathrm{Z}^{0}$ resonance.

The decay width of the $Z^{0}$ into a pair of charged Higgs particles in the framework of a two Higgs doublet scheme is given by [1]:

$$
\begin{equation*}
\Gamma\left(\mathrm{Z} \rightarrow \mathrm{H}^{+} \mathrm{H}^{-}\right)=\frac{G_{f} \mathrm{~m}_{\mathrm{Z}}^{3}}{6 \pi \sqrt{2}}\left(1 / 2-\sin ^{2} \theta_{W}\right)^{2}\left(1-4 \mathrm{~m}_{\mathrm{H}}^{2} / s\right)^{3 / 2} \tag{1}
\end{equation*}
$$

where $G_{f}$ is the Fermi constant, $\mathrm{m}_{\mathrm{H}}$ and $\mathrm{m}_{\mathrm{Z}}$ are the masses of the $\mathrm{H}^{ \pm}$and the $\mathrm{Z}^{0}$ bosons, and $\theta_{W}$ is the electroweak mixing angle.

The experiments at PETRA [2] have placed a lower limit on the mass of the charged Higgs boson at about $19 \mathrm{GeV} / \mathrm{c}^{2}$. The DELPHI Collaboration has already published an earlier analysis [3], which used about 12000 hadronic $Z^{0}$ decays and excluded the mass range from 18 to $29 \mathrm{GeV} / \mathrm{c}^{2}$. The results presented here focus on the higher mass range and have been obtained using the complete data sample collected by DELPHI from 1991 to 1993. Results from the other LEP experiments can be found in ref. [4].

Since the branching ratios for the decay $\mathrm{H}^{+} \rightarrow f \bar{f}$ are model dependent, a complete analysis should include all possible decays. The major part of the present analysis assumes that these scalars decay purely hadronically. Thus the search for $\mathrm{Z}^{0} \rightarrow \mathrm{H}^{+} \mathrm{H}^{-} \rightarrow q \overline{q^{\prime}} q^{\prime} \bar{q}$ is performed by analyzing four-jet hadronic final states. Section 2 describes the various steps of the analysis which are independent of the Higgs boson mass, while section 3 deals with the results that can be extracted as a function of the Higgs boson mass. In section 3.2 results from analyses of purely leptonic decays are given and combined in section 3.3 with those from the four jet analysis in order to give a result independent of the branching ratios.

Since this four-jet analysis relies only on the hypotheses that the heavy objects are produced in pairs, that they are scalars and that they decay into two quarks, it is possible to infer limits on the masses of other objects having similar properties (neutral Higgs particles in a general two doublet scheme and diquarks). Section 4 is devoted to such a study.

## 2 Strategy

Details concerning the components of the DELPHI detector can be found in ref. [6]. This analysis relied primarily on tracks of charged particles reconstructed using the Time Projection Chamber, the Inner and Outer Detectors and the forward chambers, on neutral particles depositing electromagnetic energy in the barrel electromagnetic calorimeter or the forward electromagnetic calorimeter or hadronic energy in the hadron calorimeter.

All data collected by DELPHI during 1991, 1992 and 1993 were used. This sample corresponds to an integrated luminosity of $70.6 \mathrm{pb}^{-1}$ (about 1.7 million hadronic $Z^{0}$ decays).

These data have been compared with more than 3 million $q \bar{q}$ events which were generated using the string fragmentation scheme from the JETSET Parton Shower model [5], together with $\mathrm{Z}^{0} \rightarrow \mathrm{H}^{+} \mathrm{H}^{-} \rightarrow c \bar{s} \bar{c} s$ events (around 1000 events at each of 6 different Higgs boson masses). It should be noted that this particular decay is expected to be by far the dominant hadronic decay of the Higgs boson. These generated events were processed through the DELPHI simulation package in order to measure the response of the detector.

The decay width given by expression (1) is relatively small and is evaluated in Table 1 for different $\mathrm{H}^{ \pm}$masses. The expected number of events has been computed taking into account the correct weighting of the different energies of the data sample. It is clear from Table 1 (and Figure 1) that the major difficulty of the analysis is to exclude as far as possible the huge background due to standard hadronic processes, while keeping a reasonable efficiency for the signal.

| $\mathrm{m}_{\mathrm{H}}$ <br> $\left(\mathrm{GeV} / c^{2}\right)$ | $\Gamma_{\mathrm{H}^{+} \mathrm{H}^{-}} / \Gamma_{\text {had }}$ | number of <br> expected evts <br> $/ 1.7 \times 10^{6}$ had. $\mathrm{Z}^{0}$ |
| :---: | :---: | :---: |
| 30 | $5.83 \times 10^{-3}$ | 10013 |
| 35 | $3.57 \times 10^{-3}$ | 6187 |
| 40 | $1.48 \times 10^{-3}$ | 2618 |
| 43 | $4.80 \times 10^{-4}$ | 889 |
| 45 | $4.43 \times 10^{-5}$ | 127 |

Table 1: Branching ratio and number of expected events

### 2.1 The four-jet picture

After the preliminary selection of hadronic events (at least 7 charged particle tracks pointing to the vertex region and at least 2 jets), events with at least four jets were kept. Jets were defined using both charged and neutral particles. The jet-finding algorithm YCLUS [7] was used with a normalized cut parameter $y_{\text {cut }}$ set to 0.02 . This value was chosen to select events having four well separated jets, which is the usual case for the signal (especially for high mass values), and is seldom expected for the QCD background. Some $75 \%$ of the signal events were retained (rather independent of the generated masses) but only $8.5 \%$ of the data and $7.6 \%$ of the $q \bar{q}$ simulated Monte Carlo. The observed difference between data and simulation showed a discrepancy of $11 \%$ in the four-jet content, as illustrated in fig. 2a, which shows the ratio of simulation to data as a function of the number of jets after the jet-finding algorithm with $y_{\text {cut }}=0.02$. A discrepancy of this size is within
the systematic error that can be expected from the error in $\alpha_{s}$ and the imperfect modeling of multijet final states implicit in the Parton Shower approach. Since the simulated $q \bar{q}$ sample is used in the following as the model for the background, in order to search for narrow structures in the di-jet mass spectrum, a further fine-tuning was necessary. This was achieved by using a slightly lower value of $y_{\text {cut }}$ for the simulated samples $(0.020)$ than for the data ( 0.0225 ). This resulted in a good agreement for the classification of hadronic events into 2, 3 and multi-jets, as shown in Figure 2b, and brought the di-jet mass spectra into closer agreement than before. The distributions of all other variables used in the analysis were checked, and were found not to be significantly affected. Figures 6a), 6b), 7 b ) and 7 c ) are examples of the results of these checks on crucial variables of the analysis.

Coming back to the selection of four jet events, an additional cut on shape variables was used to further suppress non-spherical events. Events were selected if $\mathrm{H}_{2}+\mathrm{H}_{4}<$ 0.6 where $\mathrm{H}_{2}$ and $\mathrm{H}_{4}$ are two Fox-Wolfram moments (these even numbered moments are expected to be 1 for the ideal two-jet topology and zero for isotropic events) [8]. The result of this four-jet filter was to keep $65 \%$ of the signal while $96.5 \%$ of the data (and of the $q \bar{q}$ simulation) were rejected.

When an event has more than 4 jets, the extra jets are normally due to relatively soft gluons. In order to handle these events in the same framework as events directly reconstructed as four-jet, they were reanalyzed using a version of YCLUS with the number of jets fixed to four.

Thus far in the analysis, all candidate events had the same 4-jet structure, and the signal-to-background ratio, $s / b$, was $\sim 1 / 100$ for $\mathrm{H}^{ \pm}$at $43 \mathrm{GeV} / c^{2}$.

Searching for pair production of heavy particles requires a pairing method and the computation of jet-jet masses. In order to achieve a precise mass reconstruction, a global constrained fit was performed on each event, imposing conservation of the total energymomentum with the extra constraint that two jet-jet masses be equal.

The details of such a fit are described in ref. [9]. Among the three possible pairings, the one giving the best $\chi^{2}$ was retained. Since the background mainly consists of $q \bar{q} g g$ events, this fit had a clear tendency to give a good $\chi^{2}$ for a $q g$ pairing with mass approaching the beam energy. Figure 3 shows the mass distributions obtained in fitting simulated signal events at three values of the $\mathrm{H}^{ \pm}$mass $\mathrm{m}_{\mathrm{H}}$. It is clear from that figure that a wrong pairing is chosen in around $20 \%$ of the cases. The full width at half-maximum was found to decrease as the mass of the expected object approached the beam energy, from $2.4 \mathrm{GeV} / c^{2}$ at $\mathrm{m}_{\mathrm{H}}=30 \mathrm{GeV} / c^{2}$ to $0.8 \mathrm{GeV} / c^{2}$ at $\mathrm{m}_{\mathrm{H}}=44.5 \mathrm{GeV} / c^{2}$. This fit gave better resolution and better efficiency than methods based on simple energy rescaling. It should also be noted that the intrinsic width of the charged Higgs boson is predicted to be negligible when compared with these resolutions.

Cuts necessary to ensure the overall quality of the data and of the constrained fit (5 constraints) were then applied. Events satisfying the following criteria were retained :

- the relative error on the momentum of all charged particles had to be less than $100 \%$,
- $30 \mathrm{GeV}<E_{\text {tot }}<100 \mathrm{GeV}$ where $E_{\text {tot }}$ is the total visible energy (before fit),
- charged multiplicity $\geq 2$ for each jet,
- that the fitted jet energies be positive,
- $\chi^{2}($ fit $) \leq 15$.

All these requirements constitute an overall quality cut, but $90 \%$ of the rejection is due to the $\chi^{2}$ requirement.

Each event was then described by a set of 17 variables, namely :

- global shape variables (sphericity, thrust, aplanarity, oblateness, the first four FoxWolfram moments)
- four fitted jet energies ( $E_{1}$ to $E_{4}$, sorted by increasing energy)
- a common di-jet mass M and a $\chi^{2}$ for the global fit
- three angles : a polar production angle $\theta$ and two di-jet opening angles ( $\alpha_{1}$ and $\alpha_{2}$ )

The distributions of some of these variables should exhibit differences between the signal and the background consisting mainly of $q \bar{q} g g$ events. These two types of events are shown schematically in Figure 4.

Expected differences are :

- the opening angles $(\alpha)$ should be smaller for the background than for the signal. Consequently, the distributions of all shape variables should show strong differences, the signal being dominant in the small thrust - high sphericity region. However, the preliminary cut on $\mathrm{H}_{2}+\mathrm{H}_{4}$ will weaken these differences.
- the least energetic jet is in general a gluon jet for a $q \bar{q} g g$ event. Thus its energy is on average smaller than that of the corresponding jet from $\mathrm{H}^{+} \mathrm{H}^{-}$, where the energies of the four quark jets are expected to be roughly equal.
- because of the scalar nature of the Higgs boson, the angular distribution of the $\mathrm{H}^{+}$ with respect to the $\mathrm{e}^{+}$incoming direction will be proportional to $\sin ^{2} \theta$, while for the background the usual $\left(1+\cos ^{2} \theta\right)$ behaviour is expected.


### 2.2 Discriminant variables

In a discriminant analysis between two groups, each variable has its own discriminating power, which can be expressed by the quantity :

$$
\lambda_{x}=\frac{n_{1} n_{2}}{\left(n_{1}+n_{2}\right)^{2}} \frac{\left(\bar{x}_{1}-\bar{x}_{2}\right)^{2}}{\sigma_{x}^{2}}
$$

where :

- $n_{1}$ and $n_{2}$ are the respective sizes of the two groups.
- $\bar{x}$ indicates the mean value of the variable for each group.
- $\sigma_{x}$ is the overall RMS deviation of variable $x$ (for the sample obtained by merging both groups).

In this analysis, the highest value of $\lambda$ was found to be $15 \%$ for the three highly correlated variables $E_{1}, E_{4}$ and their difference. The lowest jet energy $E_{1}$ was kept as the best discriminating variable. A second group of variables had values of $\lambda$ between 6 and $9 \%$. This group contained all shape variables, as well as $E_{2}, E_{3}$, and the opening angles of the di-jets. Sphericity $(\mathcal{S})$ was kept as second best discriminating variable because of its weak correlation with $E_{1}$. Among the remaining variables $\theta$ showed no correlation with $\mathcal{S}$ or $E_{1}$ while having a $\lambda$ sufficiently high ( $4.5 \%$ ) to improve the discrimination.

Figure 5 shows the distributions of these three variables for DELPHI data and for the simulations. A reasonable overall compatibility between experimental data and the $q \bar{q}$ simulation and a clear difference from the Higgs boson simulation were observed, providing a quantitative check of what was expected qualitatively in the previous section. It has been proven [10] that a single cut in a linear combination of appropriately chosen discriminating variables is always superior to a set of successive cuts in one variable at a time. The best linear combination of $E_{1}, \mathcal{S}$ and $\theta$ (let us call it $F$ ) was found by a Fisher linear discriminant analysis to be

$$
\begin{equation*}
F=3.65 \times\left(E_{1} / E_{1}^{\max }\right)+2.0 \times \mathcal{S}+2.8 \times\left(\theta / \theta^{\max }\right) \tag{2}
\end{equation*}
$$

when the coefficients are optimized for discriminating $44.5 \mathrm{GeV} / c^{2}$ Higgs particles from the background. Here $E_{1}^{\max }$ is half the beam energy and $\theta^{\max }$ is equal to $\pi / 2$. It should be noted that the choice of these three variables was independent of the mass of the charged Higgs boson and that the coefficients in the linear combination were rather insensitive to that mass, at least for masses greater than $40 \mathrm{GeV} / c^{2}$. Figure 6 shows the distributions of this new variable for the same samples as in Figure 5, exhibiting a clear difference between the $q \bar{q}$ Monte Carlo simulation and any Higgs boson signal. Figure 6 c also shows that there is no possibility to totally remove the background since in such a case, the remaining efficiency for the signal would be too low. A cut in $F$ at a value of 4.5 was found to be a good compromise in optimizing both the efficiency for the signal and the rejection factor for the background. The shaded histograms in Figure 5 show the effect of this cut on the original variables for all samples.

This strategy was applied to the available samples, the DELPHI data on one hand, and various simulated data on the other. The effects of the previously defined cuts are described in Table 2, together with their global efficiencies. It should be noted that despite a reduction of the background by a factor 200, the signal/background ratio was still very small (of the order of $3 \times 10^{-2}$ in the case of a $43 \mathrm{GeV} / c^{2}$ charged Higgs boson). The extraction of physical results from these samples is discussed in the next section.

|  | DELPHI <br> data | MC $q \bar{q}$ <br> $(\mathrm{PS})$ | $\mathrm{H}^{+} \mathrm{H}^{-}$ <br> $40 \mathrm{GeV} / c^{2}$ | $\mathrm{H}^{+} \mathrm{H}^{-}$ <br> $43 \mathrm{GeV} / c^{2}$ | $\mathrm{H}^{+} \mathrm{H}^{-}$ <br> $44.5 \mathrm{GeV} / c^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| normalized <br> statistics | $1,713,024$ | $1,713,024$ | 2618 | 889 | 268 |
| 4 jet filter <br> and quality cut | 51,097 | 51,180 | 1533 | 553 | 155 |
| $F \geq 4.5$ | $9203 \pm 96$ | $9045 \pm 69$ | $641 \pm 40$ | $265 \pm 17$ | $90 \pm 5$ |
| efficiency | $0.54 \%$ | $0.53 \%$ | $24.5 \%$ | $29.8 \%$ | $33.6 \%$ |

Table 2 : Selections and efficiencies
From Table 2, it is clear that the agreement between DELPHI data and $q \bar{q}$ simulation is satisfactory. In order to evaluate the systematic error on the simulation, the $\chi^{2}$ cut (from the kinematical fit) was varied over the range 5 to 20 , and the $F$ cut over the range

4 to 5 . A check was performed of the stability of the results : the MC/data ratio after the $F$ cut was found to be stable between .98 and .99 , so that the final results should not depend on the precise value of these cuts within the quoted ranges. From this check we estimated that the systematic error on the residual background obtained from the simulation was approximately $2 \%$, including the error on the normalization.

## 3 Results

### 3.1 Hadronic channel : Comparison of mass spectra

The di-jet mass spectra shown in Figure 7 lead to the following observations:

- The data and the residual simulated background have a clear tendency to peak near the kinematical limit (around $44 \mathrm{GeV} / c^{2}$ ), as already mentioned in the paragraph concerning the kinematical fit.
- Both data and residual background distributions are smooth. Fourth order polynomials are sufficient to fit these distributions from 28 to $44.5 \mathrm{GeV} / c^{2}$ very well as shown in Figure 7a) ( $\chi^{2} / \mathrm{ndf}=26.1 / 28$ for data and $24.6 / 28$ for the background $)$.
- Data and the $q \bar{q}$ simulation agree reasonably well, after the $y_{\text {cut }}$ fixing described in section 2.1 : indeed the ratio of the two distributions is flat and close to unity, in particular in the high mass region, as can be seen in Figure 7c.

In order to obtain a limit of sensitivity corresponding to the $95 \%$ confidence level for each possible mass, two different tests were performed : the first one was a direct comparison between observed data and expected background, while the second was an attempt to look for a possible signal without relying on the background simulation.

### 3.1.1 Significance of a difference

A test of the significance of the difference $(\Delta)$ between the observed number of events and the expected background in a given mass window of total width $2 \mathrm{GeV} / c^{2}$ was used to derive the sensitivity of the analysis. Since no narrow structure was expected in the $q \bar{q}$ background, a fourth order polynomial was fitted to the simulation results in order to reduce the statistical fluctuations due to the finite number of events used, and the $2 \%$ systematic error determined above was added quadratically to the statistical one deduced from the fit ${ }^{\dagger}$. The $95 \%$ confidence level for the upper bound of the difference $\Delta$ has been computed taking into account the fact that $\Delta$ has a physical lower bound of zero. Numerical values obtained for four mass hypotheses are displayed in the first part of Table 3. In addition, the same procedure was applied for all mass hypotheses from 28 to $44 \mathrm{GeV} / \mathrm{c}^{2}$ in 1 GeV steps. The limit of sensitivity, defined as the maximum signal at the $95 \%$ confidence level allowed by the observations, after correction for efficiency, was deduced, and is shown in Figure 8 as curve a.

[^1]| mass hypothesis | $37 \mathrm{GeV} / c^{2}$ | $40 \mathrm{GeV} / c^{2}$ | $43 \mathrm{GeV} / c^{2}$ | $44.5 \mathrm{GeV} / c^{2}$ |
| :---: | :---: | :---: | :---: | :---: |


| First method : significance of $\Delta=$ data - background |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| In this case, the mass is the centre of a 2 GeV $/ c^{2}$ window |  |  |  |  |
| expected signal | $376 \pm 40$ | $275 \pm 27$ | $155 \pm 12$ | $65 \pm 4$ |
| signal efficiency | $8.0 \%$ | $10.5 \%$ | $17.5 \%$ | $24.2 \%$ |
| observed data | $684 \pm 26$ | $1228 \pm 35$ | $2653 \pm 51$ | $3072 \pm 55$ |
| background | $584 \pm 17$ | $1138 \pm 24$ | $2737 \pm 38$ | $3148 \pm 41$ |
| fitted background | $593 \pm 9 \pm 12$ | $1137 \pm 12 \pm 23$ | $2753 \pm 19 \pm 55$ | $3143 \pm 20 \pm 63$ |
| $\Delta$ | $91 \pm 30$ | $91 \pm 43$ | $-100 \pm 78$ | $-71 \pm 86$ |
| sensitivity limit | 1750 | 140 | 162 | 100 |
| $95 \%$ CL upper limit for $\Delta$ | 1540 | 570 | 130 |  |
| s |  |  | 540 |  |


| Second method : fit data $+\alpha \times$ signal |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | $0.16 \pm 0.06$ | $0.00 \pm 0.07$ | $0.00 \pm 0.04$ | not stable |
| $95 \%$ CL upper lim. for $\alpha$ | 0.26 | 0.14 | 0.08 | not computable |
| sensitivity limit | 1220 | 370 | 71 | not computable |

Table 3 : Tests to establish the sensitivity limit of the analysis

### 3.1.2 Fit to the data

For each Higgs boson mass hypothesis, three successive fits were performed :

- First a Gaussian + constant fit was applied on the signal simulation, in a mass window of total width $4 \mathrm{GeV} / c^{2}$ centered at the generated mass. This fit will be further referred to as "signal".
- Then a fourth order polynomial was fitted to the data in a large window, inside of which the previous $4 \mathrm{GeV} / c^{2}$ was excluded. This fit will be further referred to as "data".
- Finally a global fit ("data" $+\alpha \times$ "signal") was done on the data either
- in a large window allowing the parameters of the polynomial and the parameter $\alpha$ to vary (six parameter fit),
- or in the 4 GeV window, using a two parameter ( $\alpha$ and $\beta$ ) fit, with $\beta$ being a normalization coefficient for "data".

Both fits gave similar results, for $\alpha$ and its error.
Numbers obtained for four different masses are displayed in Table 3. Similar fits were performed for all mass hypotheses from 28 to $43 \mathrm{GeV} / c^{2}$ in 1 GeV steps, using for "signal" interpolated values of the four parameters. From these fits the $95 \%$ confidence level for the maximum value of $\alpha$ compatible with the data was deduced and from this the limit (at the $95 \%$ confidence level) of sensitivity is drawn on Figure 8 (curve b). Three conclusions could be drawn :

- in the region 28 to $38 \mathrm{GeV} / c^{2}, \alpha$ is small and positive, and its upper limit is well below $30 \%$.
- in the region 38 to $43 \mathrm{Gev} / c^{2}, \alpha$ is found negative, which is a strong argument for a very low limit of sensitivity. When the fit was performed with a bounded parameter, $\alpha$ remained at its bound (zero) with a very small error.
- above $43 \mathrm{Gev} / c^{2}$, the method could not be applied because there were too few bins on the right hand side of the expected signal to get a stable result for the fit through the data.


### 3.1.3 Conclusion for the hadronic channel

From Figure 8, it is clear that the second method, which do not rely on a simulation of the background, gives roughly similar results to the first one, in the range of masses where it is applicable. The first method was found to be less sensitive than the second in the high mass region, but the second method fails to give a result above $43 \mathrm{GeV} / c^{2}$. The limit of sensitivity had been chosen as the one from the first method (curve a) for the low mass region (below $35.5 \mathrm{GeV} / \mathrm{c}^{2}$ ) and above $43 \mathrm{GeV} / c^{2}$ while the other method was used for the intermediate mass region. Thus, a $95 \%$ confidence level (CL) lower limit for the mass of a charged Higgs particle decaying hadronically was determined to be $43.5 \mathrm{GeV} / c^{2}$, and from the ratio of the sensitivity limit to the number of expected signal events a domain was excluded in the plane (Higgs boson mass vs. $\operatorname{Br}$ (Higgs $\rightarrow$ hadrons)) as shown on Figure 9, curve a.

### 3.2 Leptonic channel

If the branching fraction for the decay channel $\mathrm{H}^{+} \rightarrow \tau^{+} \nu_{\tau}$ is high, it is possible to search for events in which both charged Higgs particles decay leptonically. In this case the final state will consist of an acoplanar pair of low multiplicity jets coming from the decay of the $\tau$ 's. DELPHI has already reported the results of a search for this type of event in the previous publication on charged Higgs particle search [3], which has been updated in the context of a search for sleptons and charginos [11]; here the points of the analysis which are more relevant for the $\mathrm{H}^{+} \mathrm{H}^{-}$channel will be recalled.

The search was based on approximately $330,000 Z^{0}$ decays collected in 1990 and 1991. The selection criteria required that the event could be clustered into two jets, each with masses below $2 \mathrm{GeV} / \mathrm{c}^{2}$ and 1 to 3 charged particles, but with no more than 4 particles in total. The two jets were required to have a momentum greater than $3 \mathrm{GeV} / \mathrm{c}$ each and the acoplanarity angle between them was required to exceed $16^{\circ}$. Events where there was a photon at more than $15^{\circ}$ from both jets were rejected, as were those in which the component transverse to the beam axis of the total momentum of the charged particles was lower than $3.5 \mathrm{GeV} / c$. Four events survived the selection. However, they all
had two identified leptons of the same flavour (three $e e$ and one $\mu \mu$ ) as expected from photon-photon interactions, which constitute the main background process. Rejecting such combinations reduces the $\tau^{+} \tau^{-} \nu \nu$ signal by a factor of 0.92 . The total selection efficiency for a pair of charged Higgs bosons with a mass around $45 \mathrm{GeV} / c^{2}$ was calculated to be $31 \%$, including reconstruction losses. Since there were no candidate events, this excluded at $95 \%$ confidence level a charged Higgs boson with a mass lower than $45.4 \mathrm{GeV} / c^{2}$ for $\operatorname{Br}\left(\mathrm{H}^{+} \rightarrow \tau^{+} \nu_{\tau}\right)=1$, as well as the domain limited by curve b on Figure 9.

### 3.3 Global mass limit

Combining results from sections 3.1 and 3.2 , a new global mass limit in the plane $\mathrm{m}_{\mathrm{H}^{ \pm}}$ vs $\operatorname{Br}\left(\mathrm{H}^{ \pm} \rightarrow\right.$ hadrons $)$ can be deduced and is plotted in Figure 9. Taking into account the previously excluded mass range, the new lower limit on the mass of a charged Higgs boson, at the $95 \%$ confidence level, is $43.5 \mathrm{GeV} / c^{2}$, independent of its decay branching fraction into hadrons.

## 4 Inference for other pair-produced scalars

### 4.1 Neutral Higgs particles in a two doublet scheme

Since the jet-jet mass resolution is similar for the $c \bar{c}, b \bar{b}$ and $c \bar{s}$ systems, the same 4 -jet analysis allows a complementary search for the neutral Higgs bosons via $\mathrm{Z} \rightarrow \mathrm{hA} \rightarrow c \bar{c} c \bar{c}$ (the dominant decay when $\tan \beta \ll 1$ ), $\mathrm{Z} \rightarrow \mathrm{hA} \rightarrow c \bar{c} b \bar{b}$ or $\mathrm{Z} \rightarrow \mathrm{hA} \rightarrow b \bar{b} b \bar{b}$ under the restrictive condition that $h$ and $A$ have the same mass. In this case, the general formula of the production of a hA pair can be simplified to :

$$
\Gamma(\mathrm{Z} \rightarrow \mathrm{hA}) \approx 0.5\left(1-4 \mathrm{~m}_{\mathrm{h}}^{2} / \mathrm{m}_{\mathrm{Z}}^{2}\right)^{3 / 2} \Gamma(\mathrm{Z} \rightarrow \nu \bar{\nu}) \cos ^{2}(\alpha-\beta) \quad\left(\text { when } \mathrm{m}_{\mathrm{h}}=\mathrm{m}_{\mathrm{A}}\right)
$$

The results from Table 3 can thus be translated into limits on $\cos ^{2}(\alpha-\beta)$. Since limits on $\sin ^{2}(\alpha-\beta)$ can be derived from the Standard Model Higgs boson analysis [12], a given $m_{h}$ can be excluded provided the sum of the limits falls below 1. This sum was estimated to be $.76 \pm .02$ for $\mathrm{m}_{\mathrm{h}}=44 \mathrm{GeV} / c^{2}$ and $1.01 \pm .03$ for $\mathrm{m}_{\mathrm{h}}=44.5 \mathrm{GeV} / c^{2}$. Thus a $44.4 \mathrm{GeV} / \mathrm{c}^{2}$ neutral Higgs boson can be excluded at the $95 \%$ confidence level. This result also applies when $\mathrm{m}_{\mathbf{h}}$ is not strictly equal to $\mathrm{m}_{\mathrm{A}}$ because the constrained fitting procedure only begins to degrade when the mass difference exceeds $4 \mathrm{GeV} / \mathrm{c}^{2}$.

### 4.2 Diquarks

Diquarks appear in several theoretical approaches and models extending the Standard Model; recently [13] they appear in $\mathrm{E}_{6}$ inspired superstring theory as members of new supermultiplets of $\mathrm{E}_{6}$, which has been considered as an attractive basis for grand unification for a long time. In this formulation, each matter generation lies in a $\underline{27}$ representation and in addition to the light fermions of the SM and their SUSY partners, extra colourtriplet spin 0 and spin $1 / 2$ particles, $D$, are predicted for each family. There are two spin 0 new particles, $D_{0}$ and $D_{0}^{c}$, their charge being $-1 / 3$ and they could behave as either pure elementary leptoquarks $(\mathrm{L}=+1, \mathrm{~B}=+1 / 3)$ or pure elementary diquarks ( $\mathrm{L}=0$, $\mathrm{B}=-2 / 3)$. If the $D$ particles behave as diquarks, then the dominant decay modes would be $D_{0} \rightarrow \bar{q} \bar{q}^{\prime}, D_{0}^{c} \rightarrow q q^{\prime}$, and $D_{1 / 2} \rightarrow \bar{q} \bar{q}^{\prime} \chi$, where $\chi$ is the lightest supersymmetric neutral
particle. These $D_{0}$ decays may only be detectable in the $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow D_{0} \bar{D}_{0}\left(D_{0}^{c} \bar{D}_{0}^{c}\right)$ channels [14].

The expected cross section in each family, including QED and electroweak corrections, is smaller than the $\mathrm{H}^{+} \mathrm{H}^{-}$one by a factor 2 if the two diquarks of the same family are mass degenerate and there is no mixing between them, otherwise it is smaller by a factor of 4 .

The signature for pair production from the second family would be $\mathrm{e}^{+} \mathrm{e}^{-} \rightarrow D_{0} \bar{D}_{0} \rightarrow$ $\bar{c} \bar{s} c s$, which is similar to the one from a pair of charged Higgs particles decaying hadronically. Thus it is tempting to use the same analysis in a search for this process. However, diquarks are coloured objects and coloured strings develop in a different way from the case of a colorless Higgs boson pair. The effects of these different fragmentation schemes were studied in detail by comparing samples of generated $D_{0} \bar{D}_{0}$ and $\mathrm{H}^{+} \mathrm{H}^{-}$events at masses in the range $20-40 \mathrm{GeV} / c^{2}$ and fitting the distributions of the di-jet masses obtained after the 4 -jet global constrained fit described in section 2.1. The observed results were a broadening of the width and a shift of the di-jet mass for the $D_{0} \bar{D}_{0}$ events relative to the $\mathrm{H}^{+} \mathrm{H}^{-}$case. The broadening of the width decreased from $25 \%$ at $20 \mathrm{GeV} / \mathrm{c}^{2}$ to $12 \%$ at 40 $\mathrm{GeV} / c^{2}$ and the shift of the mass decreased from $12 \%$ at $20 \mathrm{GeV} / c^{2}$ to $0.5 \%$ at $40 \mathrm{GeV} / c^{2}$.

The same test as that of Table 3 (section 3.1.2) was applied, and the corresponding result is shown in Figure 10. The poorer sensitivity limit is due to the broadening of the width mentioned above and affects mainly the region below $37 \mathrm{GeV} / c^{2}$. From that figure, diquarks can be excluded at the $95 \%$ confidence level from 28 to $43 \mathrm{GeV} / \mathrm{c}^{2}$ if they are mass degenerate, and from 28 to $31.7 \mathrm{GeV} / c^{2}$ otherwise.

For lower diquark masses, a dedicated analysis [15] was performed using 387,000 hadronic $Z^{0}$ events $(1990+1991$ data), 231,000 hadronic simulated events and the existing "signal" of simulated $\mathrm{H}^{+} \mathrm{H}^{-}$events with masses $15-37 \mathrm{GeV} / c^{2}$. The same global 4 -jet constrained fit was applied and the same quality selection criteria were used (section 2.1). The di-jet mass distribution of the $\mathrm{H}^{+} \mathrm{H}^{-}$samples were smeared to take into account the broadening effect due to the different fragmentation scheme of the diquark pair.

Instead of the $F$ cut which was best adapted for higher masses, a set of kinematical cuts optimized for each of the various signal masses was applied, drastically reducing the QCD background. These included the energy difference between the fastest and the slowest jets, the sum of the decay angles of the two heavy objects, sphericity, etc. No signal was seen in the mass range $15-35 \mathrm{GeV} / \mathrm{c}^{2}$, as shown on Figure 11, thus excluding pair production of mass-degenerate diquarks of the second family in this same mass interval at the $95 \%$ confidence level, and of non-degenerate diquarks up to $28 \mathrm{GeV} / \mathrm{c}^{2}$. Thus, combining this result with the result above, and taking into account the fact that this analysis does not distinguish the jet flavors, a diquark of the $\mathrm{E}_{6}$ type can be excluded in the interval $15-43 \mathrm{GeV} / c^{2}$ at the $95 \%$ confidence level (mass degenerate without mixing) and in the interval 15-31.7 otherwise.

## 5 Conclusion

Based on an analysis of 1.7 million hadronic $Z^{0}$ decays, new lower limits have been set on the mass of possible heavy pair-produced scalar-particles. All these limits should be understood as $95 \%$ confidence level limits.

- For the charged Higgs boson, the limits are

$$
\begin{gathered}
\mathrm{m}_{\mathrm{H}^{ \pm}}>43.5 \mathrm{GeV} / c^{2} \quad \text { for } \mathrm{Br}\left(\mathrm{H}^{+} \rightarrow c \bar{s}\right)=1 \\
\text { and } \mathrm{m}_{\mathrm{H}^{ \pm}}>45.4 \mathrm{GeV} / c^{2} \\
\text { for } \mathrm{Br}\left(\mathrm{H}^{+} \rightarrow \tau^{+} \nu_{\tau}\right)=1
\end{gathered}
$$

leading to a combined limit of $43.5 \mathrm{GeV} / c^{2}$, irrespective of the Higgs boson decay branching ratios.

- For the neutral Higgs bosons in a two doublet model, the lower mass limit is

$$
\mathrm{m}_{\mathrm{h}}>44.4 \mathrm{GeV} / \mathrm{c}^{2} \quad \text { for } \mathrm{m}_{\mathrm{h}} \simeq \mathrm{~m}_{\mathrm{A}}
$$

- $\mathrm{E}_{6}$ diquarks have been excluded in the mass range $15-31.7 \mathrm{GeV} / c^{2}$, this range being extended up to $43 \mathrm{GeV} / c^{2}$ if these diquarks are degenerate in mass.

It should be noted that the present results set mass limits essentially at the LEP I kinematic limits.

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Figure 1: Distribution of Thrust for $\mathrm{H}^{+} \mathrm{H}^{-}$events (grey) for a Higgs particle mass of $40 \mathrm{GeV} / c^{2}$ and real data $\mathrm{Z}^{0} \rightarrow$ hadrons (plain). Note the vertical log scale.


Figure 2: MC/data ratio versus NJET found with YCLUS. The top figure is before fixing, the bottom one is after fixing as described in the text.


Figure 3: Mass distributions obtained after constrained fitting of simulated events for three Higgs boson masses. Full widths at half maximum are respectively 1.7 (1.1) (0.8) $\mathrm{GeV} / c^{2}$ at $\mathrm{m}_{\mathrm{H}}=40(43)(44.5) \mathrm{GeV} / c^{2}$.


Figure 4: Schematic diagrams of a) background, b) signal events.


Figure 5: On the left side, distributions of a) $E_{1}$ (energy of the least energetic jet), b) sphericity and c) $\theta$ ( $\mathrm{H}^{ \pm}$polar production angle) for data (crosses) and simulation (histograms). On the right side, the same distributions in the case of the hadronic decay of charged Higgs boson pairs ( $43 \mathrm{GeV} / \mathrm{c}^{2}$ ). Events passing the multi-dimensional cut (equ. (2)) are shaded.


Figure 6: Above, MC/data ratio as a function of $F$ (see equation (2) for definition), a) before and b) after $y_{\text {cut }}$ fixing. The fits of this ratio to a constant value give the following results : a) 0.885 and $\chi^{2}=44.3$ for 37 degrees of freedom and b) 0.999 and $\chi^{2}=43.2$ for the same number of degrees of freedom. Below (c), distribution of the variable $F$ for $q \bar{q}$ simulation (histogram), DELPHI data (crosses) and for a $43 \mathrm{GeV} / c^{2}$ charged Higgs boson (hatched histogram, not to scale). The cut at 4.5 is indicated by the vertical arrow.

Normalised di-jet masses after multidim. cut


Figure 7: a) Di-jet mass spectrum for DELPHI data (crosses) and result of a polynomial fit. b) and c) MC/data ratio as a function of the di-jet mass, respectively before and after $y_{\text {cut }}$ fixing. The fit results are : b) 0.925 and $\chi^{2}=15.7$ for 12 degrees of freedom, c) 0.996 and $\chi^{2}=11.5$ for 12 degrees of freedom. d) Comparison between di-jet mass spectra for simulation (histogram) and data (crosses), reproduced also on the three last plots. In the last three pictures, the unshaded areas are the expected signals for different Higgs boson masses : e) $30 \mathrm{GeV} / c^{2}$, f) $35 \mathrm{GeV} / c^{2}$, g) $40 \mathrm{GeV} / c^{2}$.


Figure 8: Limit of sensitivity of the hadronic analysis (two methods), compared with the total number of expected signal events, showing clearly the exclusion interval from 28 to $43.5 \mathrm{GeV} / c^{2}$. Curve a) is obtained by a direct comparison of data versus background and curve b) by a fit to data $+\alpha \times$ signal.


Figure 9: Excluded regions at $95 \%$ confidence in the plane $\mathrm{m}_{\mathrm{H} \pm} \mathrm{vs} \operatorname{Br}\left(\mathrm{H}^{ \pm} \rightarrow\right.$ hadrons $)$. The region above curve (a) is excluded by the hadronic analysis, while the region below curve (b) is excluded by the $\tau \tau$ analysis. The bold solid curve on the right hand side corresponds to the combined limit.


Figure 10: Limit of sensitivity of the diquark analysis, compared with the total number of expected signal events, showing clearly the exclusion interval from 28 to $43 \mathrm{GeV} / c^{2}$.

## Di-jet masses (diquarks search)



Figure 11: Comparison between di-jet mass spectra for simulation (shaded histogram) and data (crosses), together with the expected diquark signals (unshaded) for different diquark masses : a) $17.5 \mathrm{GeV} / c^{2}$ non-degenerate, b) $23 \mathrm{GeV} / c^{2}$ non-degenerate, c) 29 $\mathrm{GeV} / c^{2}$ degenerate and d) $36.5 \mathrm{GeV} / c^{2}$ degenerate diquarks.


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[^1]:    ${ }^{\dagger}$ For practical reasons, two fits were performed to the simulation, both with a fourth order polynomial : the first one, from 28 to $44 \mathrm{GeV} / c^{2}$ was used for masses up to $43 \mathrm{GeV} / c^{2}$, the second one from 40 to $46 \mathrm{GeV} / \mathrm{c}^{2}$ was necessary for the high mass region. Both fits gave similar results at $43 \mathrm{GeV} / \mathrm{c}^{2}$.

