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Potential barriers governing the ¹²C formation and decay through quasimolecular shapes

G. Royer, A. Escudie, and B. Sublard

Laboratoire Subatech, UMR: IN2P3/CNRS-Université-Ecole des Mines, Nantes 44, France (Received 10 February 2014; revised manuscript received 18 June 2014; published xxxxxx)

The L-dependent potential barriers that govern the 8Be and 12C formation and decay through quasimolecular shapes have been determined using a generalized liquid-drop model and adjusted to reproduce the experimental Q value. For the ternary channel of ¹²C, the energies of prolate linear chain configurations and oblate triangular configurations of three α particles have been compared. The triangular shape with three α nuclei in contact allows the experimental rms radius and the negative quadrupole moment of the ¹²C ground state to be reproduced. The difference between the energies of the minima in the prolate and oblate ternary shape paths are very close to the energy of the excited Hoyle state of the 12C nucleus.

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I. INTRODUCTION

Hydrogen burning in stars leads to a dense and hot core of helium that fuels the nucleosynthesis of the heavier elements. The "triple- α " capture phenomenon has been advanced to explain the formation of the ¹²C nuclei. In a first stage of this process two α particles resonate in the ground state of ${}^{8}\text{Be}$. The half-life of this state $(8.2 \times 10^{-17} \text{s})$ allows the capture of a third particle before it disintegrates leading to the 0_2^+ excited Hoyle state of ${}^{12}\text{C}$ ($E^* = 7.6542 \text{ MeV}$). The probability of such a process is non-negligible because this excitation energy is very close to the $Q_{\alpha+8\text{Be}} = 7.3666 \text{ MeV}$ and $Q_{3\alpha} = 7.2747$ MeV thresholds. The knowledge of the shape of the ¹²C nucleus in its ground and excited states is of great importance to fully understand this fusion reaction.

Theoretically, after calculating transition densities derived from the three- α resonating-group wave functions it was concluded that the shape of the ground state of ¹²C is oblate [1]. Within an isomorphic shell model it has been assumed that both the ground state and the first 0+ excited state can be associated with an α chain composed of three particles in a row [2], but the decay width of the Hoyle state is not reproduced. Calculations using antisymmetrized molecular dynamics and Fermionic molecular dynamics without assuming α clustering have allowed the low-lying spectrum of ¹²C to be reproduced [3,4]. It has also been found that the 0^+_2 Hoyle state has a Bose-Einstein dilute 3α condensatelike structure [5,6]. Recent ab initio lattice calculations have led to a compact triangular configuration for the ¹²C ground state and the first excited state 2_1^+ state and to a "bent-arm" or obtuse triangular configuration of α clusters for the Hoyle state and the second excited 2^+_2 state [7]. The no core shell model has shown that the collective states and states with clusterlike substructures can emerge out of a fully microscopic shell model framework [8]. The Hoyle state has also been described in terms of a local potential ${}^{8}\mathrm{Be} + \alpha$ cluster model [9].

Experimentally, the value of the root-mean-square charge radius of the ground state of ¹²C is $\langle r^2 \rangle^{1/2} = 2.47$ fm [10]. The electric quadrupole moment of the ¹²C ground state is $Q_0 = -22^+_-10 \ e \ \text{fm}^2$ assuming that the nuclear charge distribution is spheroidal with K = 0 [11], which indicates a substantial oblate deformation incompatible with the linear

chain configuration of three α particles. To populate the 55 Hoyle state of ¹²C [12,13] fragmentation of quasiprojectiles 56 in the reaction ⁴⁰Ca + ¹²C at 25 MeV/nucleon was employed; ⁵⁷ $7.5 \pm 4\%$ of the particle decays of the Hoyle state correspond 58 to direct decays in three equal-energy α particles and thus 59 fulfill the decay criteria of an α-particle condensate. Moreover, 60 events with increased kinetic energy dispersion in the ¹²C ₆₁ center of mass, which amount to 9.5 ± 4%, point toward 62 the occurrence of a second molecular configuration, a linear 63 α-chain type. Different ratios have also been provided [14]. 64 Beyond the excited 0⁺₂ Hoyle state, evidence has been observed 65 for a possible 2+ state at 9.6(1) MeV with a width of 66 600(100) keV [15]. Analyzing (α, α') cross-section data, a 67 2^+ excitation of the Hoyle state and the α -condensate state 68 at $E_x = 9.84 \pm 0.06$ MeV with a width of 1.01 ± 0.15 MeV 69 have also been found [16].

The purpose of this work is to determine the L-dependent 71 potential barriers governing the evolution of the 8Be nucleus of 72 the ${}^{8}\text{Be} + {}^{4}\text{He}$ system and the ${}^{4}\text{He} + {}^{4}\text{He} + {}^{4}\text{He}$ oblate trian- 73 gular and prolate longitudinal configurations in the framework 74 of a generalized liquid-drop model (GLDM) and of binary and 75 ternary quasimolecular shapes.

II. GENERALIZED LIQUID-DROP MODEL

This version of the liquid-drop model has been used 78 previously to determine the fusion barriers and cross sections 79 [17,18], the binary [19] and ternary [20] fission barriers 80 and characteristics, and the α-decay potential barriers and 81 half-lives [21].

The GLDM energy is the sum of the volume, surface, 83 Coulomb, and nuclear proximity energies. For a one-body 84 shape nucleus, the first three contributions are given by

$$E_V = -15.494(1 - 1.8I^2)A \text{ MeV},$$
 (1)

$$E_S = 17.9439(1 - 2.6I^2)A^{2/3} \frac{S}{4\pi R_0^2} \text{ MeV},$$
 (2)

where I = (N - Z)/A is the relative neutron excess and S is 86 the surface of the deformed nucleus, and

$$E_C = 0.6e^2(Z^2/R_0)B_C. (3)$$

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⁸⁸ The Coulomb-shape-dependent function B_C is expressed as

$$B_C = \frac{15}{16\pi^2 R_0^5} \int d\tau \int \frac{d\tau'}{|r - r'|}.$$
 (4)

By using the axial symmetry of the system and complete elliptic integrals it reduces to

$$B_C = 0.5 \int (V(\theta)/V_0)(R(\theta)/R_0)^3 \sin\theta d\theta.$$
 (5)

 $V(\theta)$ is the electrostatic potential at the surface and V_0 is the surface potential of the sphere. The nuclear radius is defined

$$R_0 = (1.28A^{1/3} - 0.76 + 0.8A^{-1/3}) \text{ fm}.$$
 (6)

This formula was derived from the droplet model and from the proximity energy values. 95

All along the entrance or decay channels the proximity energy term takes into account the effects of the nuclear attractive forces between nucleons being studied in a neck, in the case of a deformed one-body shape or across the gap and in the case of two or three nuclei. This is an additional term to the surface energy which takes into account only the effects the nuclear forces in a half-space. This proximity term is necessary to reproduce the fusion barrier heights, beyond the pure Coulomb peak approximation. It is particularly important when there are two or three spherical nuclei in contact and for quasimolecular one-body shapes where the necks are narrow and well developed. When the proximity energy is taken into account, the potential barrier is smooth even at the contact point and the top of the barrier corresponds to separated nuclei maintained in unstable equilibrium by the balance between the repulsive Coulomb forces and the attractive nuclear proximity forces. As examples, the symmetric fission barrier of a ²³⁴U nucleus through compact and creviced shapes is lowered by around 40 MeV by the proximity energy [22,23] and then the barrier height is comparable to the experimental data. The proximity forces lower of 5.7 MeV the barrier against α emission from a ²⁶⁴Hs nucleus, the displacement of the barrier top to a more external position being of 2.1 fm [21].

The proximity energy reads

$$E_{\text{prox}}(r) = 2\gamma \int \Phi \left[D(r,h)/b \right] 2\pi h dh, \tag{7}$$

where r is the distance between the mass centers, Φ is the proximity function of Feldmeier [24], h is the transverse distance varying from the neck radius for one-body shapes 122 and zero for separated nuclei to the height of the neck border, b is the surface width (b = 0.99 fm), D is the distance between the opposite surfaces on a line parallel to the separation axis (see Ref. [17]), and γ is the surface parameter:

$$\gamma = 0.9517(1 - k_s I^2) \text{ MeV fm}^{-2}.$$
 (8)

The experimental Q value which incorporates the microscopic corrections plays a main role. It has been taken into account empirically in adding the difference between the experimental and the theoretical Q values deduced from the GLDM at the macroscopic potential energy of the mother spherical nucleus with a linear attenuation factor vanishing at

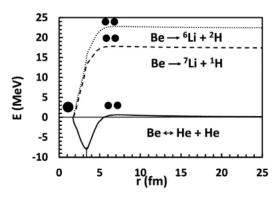


FIG. 1. Potential barriers governing the ⁸Be ↔ ⁴He + ⁴He, $^8\text{Be} \rightarrow ^7\text{Li} + ^1\text{H}$, and $^8\text{Be} \rightarrow ^6\text{Li} + ^2\text{H}$ reactions versus the distance between the mass centers (at L=0). The vertical dash indicates the contact point between the two nuclei.

the contact point of the two or three fragments or incoming 133

To describe the evolution of one sphere to two spheres in 135 contact assuming volume conservation, elliptic lemniscatoids have been retained because they allow the progressive formation of a deep neck while keeping almost spherical ends [17]. A generalization of this shape sequence permits one to also describe the prolate ternary path that leads from a sphere to three aligned spheres in contact [20] and then to simulate the linear chain configurations of three α particles. The oblate ternary fission or fusion has been described from the contact point between three α particles arranged on an equilateral triangle and which separate in keeping the same triangular configuration [25]. The proximity energy is maximized for such shape sequences.

III. 8Be NUCLEUS

First, the ⁸Be nucleus is considered. The potential barriers 149 of the three reactions ${}^8\text{Be} \leftrightarrow {}^4\text{He} + {}^4\text{He}, {}^8\text{Be} \leftrightarrow {}^7\text{Li} + {}^1\text{H},$ 150 and $^8{\rm Be} \leftrightarrow {}^6{\rm Li} + {}^2{\rm H}$ are displayed in Fig. 1 and the characteristics are given in Table I. The figure displays the deformation 152

TABLE I. Characteristics of different ⁸Be entrance or decay channels. r_{sph} and r_{cont} are, respectively, the distance between the mass centers of the two parts of the system at the sphere and at the contact point while $r_{E_{\min}}$ and $r_{E_{\max}}$ indicate the position of the minimum and maximum of the potential barriers.

	$r_{\rm sph}$	$r_{E_{\min}}$	$r_{\rm cont}$	$r_{E_{\max}}$	∞
⁸ Be ↔ ⁴ He + ⁴ He					
r (fm)	1.65	3.39	3.49	7.45	
E (MeV)	O	-7.95	-7.84	0.62	-0.0918
$^8\mathrm{Be} ightarrow ^7\mathrm{Li} + {}^1\mathrm{H}$					
r (fm)	1.73		3.33	6.89	
E (MeV)	O		12.94	17.82	17.25
$^8\text{Be} \rightarrow ^6\text{Li} + ^2\text{H}$					
r (fm)	1.69		3.42	7.38	
E (MeV)	0		15.43	22.81	22.28

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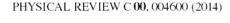
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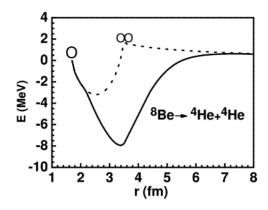


FIG. 2. Comparison between the deformation energies calculated without (broken curve) and with (full curve) a proximity energy term for the ${}^{8}\text{Be} \leftrightarrow {}^{4}\text{He} + {}^{4}\text{He}$ reaction.

energy relatively to the sphere energy, which explains that the potential barriers start from the same energy point. For the largest deformations the energy corresponds to the Q value of the fusion process. The top of the barriers corresponds to two separated spheres. The possibility of resonant states exists in the ${}^{4}\text{He} + {}^{4}\text{He}$ channel.

The influence of the proximity energy term is underlined in Fig. 2. The unrealistic pure Coulomb peak is given by the dashed curve. The maximum corresponds to the contact point. When the effects of the proximity forces are taken into account the energy at the contact point diminishes by around 9.4 MeV while the barrier top is shifted 4 fm.

Within this macroscopic model the decay constant is simply given by $\lambda = v_0 P$. The assault frequency v_0 has been taken as $v_0 = 10^{20} \text{ s}^{-1}$. The barrier penetrability *P* is calculated within the action integral:

$$P = \exp\left[-\frac{2}{\hbar} \int_{r_{\rm in}}^{r_{\rm out}} \sqrt{2B(r)[E(r) - E_{\rm g.s.}]} dr\right]. \tag{9}$$

The inertia B(r) is related to the reduced mass by

$$B(r) = \mu \{ 1 + 24 \exp[-3.25(r - R_{\rm sph})/R_0] \}, \tag{10}$$

where R_{sph} is the distance between the mass centers of the future fragments in the initial sphere; $R_{sph}/R_0 = 0.75$ in the symmetric case. For shapes near the ground state the inertia is largely above the irrotational flow value because a large amount of internal reorganization occurs at level crossings. For highly deformed shapes the reduced mass is reached asymptotically. Such a prescription for the inertia parameter has allowed the fission half-lives of the actinide nuclei to be precisely reproduced [19]. A more detailed discussion of this parameter may be found in Ref. [26].

The partial half-life is finally obtained by $T_{1/2} = \frac{\ln 2}{\lambda}$. Here, the instability of the 8Be nucleus against its symmetric decay leads to a theoretical half-life of 5.7×10^{-16} s, a value close to the experimental value 8.2×10^{-17} s. The rotational energy is given by

$$E_{\text{rot}} = \hbar^2 l(l+1)/2J,$$
 (11)

assuming a rigid moment of inertia. The L-dependent barriers are displayed in Fig. 3. The indicated energy is the sum of

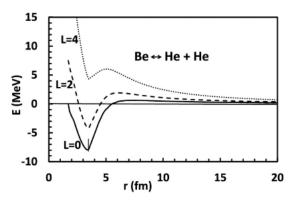


FIG. 3. Potential barriers of the 8Be ↔ 4He + 4He reaction as a function of the angular momentum (in \hbar units).

the deformation energy and of the rotational energy. The 187 theoretical energies of the 2 and 4 states are, respectively, 188 3.78 and 12.25 MeV, not too far from the experimental values, 189 3.03 and 11.35 MeV, of the energies of the 2+ and 4+ states. 190 Nevertheless, this potential does not allow us to reproduce the 191 half-life for the L = 2 level.

IV. 12C NUCLEUS

Several binary channels governing the ¹²C evolution are 194 compared in Fig. 4 and the characteristics are given in 195 Table II. The respective Q values are -7.365, -25.19, 196 -26.28, and -28.17 MeV. Resonant states are possible in 197 the very specific $^{12}\text{C} \leftrightarrow {}^{8}\text{Be} + {}^{4}\text{He}$ channel. They correspond 198 to a quasimolecular one-body shape formed by two nuclei 199 connected by a narrow neck.

The potential barriers corresponding to the direct aligned 201 3α fusion and the $^8\mathrm{Be} + ^4\mathrm{He}$ fusion reaction are compared in 202 Fig. 5. The Q values are almost identical, respectively, 7.2747 203 and 7.3666 MeV. The proximity energy between three aligned 204 α particles is stronger than the proximity energy between an 205 assumed spherical ⁸Be nucleus and an α particle because there 200 are two necks for the ternary configuration. The proximity 207 forces act at larger values of the distance r in the ternary case, 208 which explains the crossing of the curves at r = 8 fm.

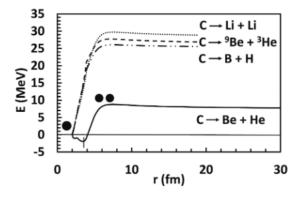


FIG. 4. Potential barriers governing the ¹²C ↔ ⁸Be + ⁴He, $^{12}\text{C} \rightarrow ^{10}\text{B} + ^{2}\text{H}, ^{12}\text{C} \rightarrow ^{9}\text{Be} + ^{3}\text{He}, \text{and} ^{12}\text{C} \rightarrow ^{6}\text{Li} + ^{6}\text{Li} \text{ reactions}$ versus the distance between the mass centers (at L=0). The vertical dash indicates the contact point between the two nuclei.

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TABLE II. Same as Table I but for the 12C nucleus reactions.

	$r_{\rm sph}$	$r_{E_{\min}}$	$r_{\rm cont}$	$r_{E_{\max}}$	∞
$^{12}\text{C} \leftrightarrow ^{8}\text{Be} + ^{4}\text{He}$					
r (fm)	1.91	3.41	3.96	7.43	
E (MeV)	0.00	-1.95	-0.63	8.77	7.365
	$r_{ m cms}$		$r_{\rm eme}$	$r_{E_{\max}}$	∞
$^{12}C \rightarrow {}^{10}B + {}^{2}H$					
r (fm)	1.98		3.81	7.49	
E (MeV)	0.00		18.26	26.06	25.19
$^{12}\text{C} \rightarrow ^{9}\text{Be} + ^{3}\text{He}$					
r (fm)	1.94		3.90	7.12	
E (MeV)	0.00		20.97	27.73	26.28
$^{12}C \rightarrow ^{6}Li + ^{6}Li$					
r (fm)	1.89		4.0	7.48	
E (MeV)	0.00		19.63	29.44	28.17

The *L*-dependent potential barriers in the prolate ternary shape path are shown in Fig. 6. A minimum persists even at relatively high angular momenta.

Experimentally, the value of the electric quadrupole moment of the $^{12}\mathrm{C}$ ground state is $Q_0 = -22 \pm 10~e~\mathrm{fm^2}$ assuming that the nuclear charge distribution is spheroidal with K = 0 [11], which indicates a substantial oblate deformation incompatible with the linear chain configuration of three α particles. The other fundamental property is the root-mean-square charge radius $\langle r^2 \rangle^{1/2} = 2.47~\mathrm{fm}$ for the $^{12}\mathrm{C}$ nucleus [10].

To study these oblate ternary configurations three spherical α particles have been placed in contact on an equilateral triangle (see Fig. 7) and later separated and moved away from each other in keeping the regular triangular configuration. At the contact point, the rms radius is $\langle r^2 \rangle^{1/2} = 2.43$ fm and the electric quadrupole moment is $Q_0 = -24.4 e \, \mathrm{fm}^2$, both in very good agreement with the experimental data.

All along the deformation path the rms radius is connected with the distance l from the center of each fragment to the mass center of the total system by [25]

$$\langle r^2 \rangle = \frac{3}{5} R_0^2 3^{-2/3} + l^2.$$
 (12)

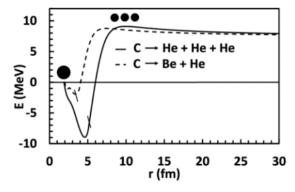


FIG. 5. Comparison between the potential barriers governing the $^{12}\text{C} \leftrightarrow ^8\text{Be} + ^4\text{He}$ and $^{12}\text{C} \leftrightarrow ^4\text{He} + ^4\text{He}$ binary and prolate ternary reactions.

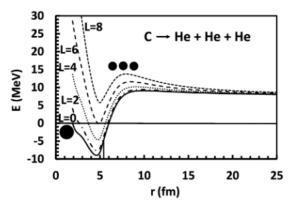


FIG. 6. Potential barriers of the ¹²C ↔ ⁴He + ⁴He + ⁴He reaction as a function of the angular momentum and for a linear chain configuration.

The L-dependent potential barriers seen by this oblate 231 configuration of three α particles are displayed in Fig. 8. 222 For such a shape the proximity energy between the nucleons 233 under study is very important; $E_{prox} = -28.2 \text{ MeV}$ at the 234 contact point. For the linear chain, there are only two necks 235 and the proximity energy is only −18.8 MeV at the touching 236 point. Therefore the characteristics of the oblate configuration 237 of three α particles in contact at the top of an equilateral 238 triangle seem compatible with the experimental data available 239 on the ground state of the ¹²C nucleus. Furthermore the ²⁴⁰ difference between the energy of the minima of the potential 241 barrier of the 3α linear chain and the minima of the oblate 242 equilateral configuration is 7.36 MeV, a value very close to 243 the energy of the excited Hoyle state. This is in favor of a 244 linear chain configuration for the Hoyle state. Then the L=2 245 and L=4 excited states of the prolate longitudinal chain have 246 energies of, respectively, 8.7 and 11.7 MeV compared with the 247 experimental value of the 2+ state at 9.6(1) MeV with a width 248 of 600(100) keV [15].

The feasibility of such a liquid-drop approach for such light systems is evidently questionable. At least, one may be confident with the calculation of the proximity energy because it allows one to reproduce precisely the fusion barrier heights and positions of symmetric and very asymmetric light systems such as ${}^9\text{Be} + {}^{10}\text{B}$, ${}^4\text{He} + {}^{44}\text{Ca}$, ${}^4\text{He} + {}^{233}\text{U}$ [27] and also to 255

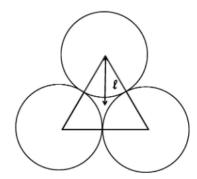


FIG. 7. Oblate ternary configuration of three α particles in contact. l is the distance between the mass center of an α particle and the mass center of the whole system.

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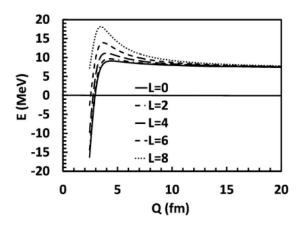


FIG. 8. L-dependent potential barriers for the $^{12}\text{C} \leftrightarrow ^{4}\text{He} +$ ⁴He + ⁴He reaction and a triangular configuration. Q is the rms radius.

determine precisely the α -decay potential barriers [21] with the help of the experimental Q value. One may also wonder that such a liquid-drop model is available (when taking also into account other terms) to reproduce the mass of light nuclei even though the accuracy is lower than that for heavier nuclei [28].

Another open question is the availability of such an approach 261 for such distorted quasimolecular or two-body and three-body 262 shapes. The question is the same for microscopic theories using 263 mean fields.

As stated in the Introduction, much more elaborated 265 microscopic quantum theories have been developed recently. 266 They allow one to determine accurate density profiles and, in 267 particular, to obtain one-body "bent-arm" or obtuse triangular 268 configurations. The reproduction of the transition from one- 259 body to two- or three-body shapes or the fusion process is 270 more difficult and time-consuming.

V. SUMMARY AND CONCLUSION

In conclusion, within a GLDM taking into account the 273 proximity energy and adjusted to reproduce the experimental 274 Q value, the L-dependent potential barriers for the binary ²⁷⁵ $^{12}\text{C} \leftrightarrow ^{8}\text{Be} + ^{4}\text{He}$ and $^{12}\text{C} \leftrightarrow ^{4}\text{He} + ^{4}\text{He}$ prolate and 276 oblate ternary reactions have been calculated. The oblate 277 triangular configuration of three α particles in contact is 278 compatible with the experimental rms radius and electric 279 quadrupole moment while the linear configuration of three 280 aligned α particles allows one to reproduce roughly the energy 281 of the excited 0⁺ Hoyle state and the energy of the excited 2⁺ Hoyle state.

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