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Recent results on charmonium (-like) spectroscopy at LHCb

Chen Chen

Aix Marseille Univ, CNRS/IN2P3, CPPM, Marseille, France

(On behalf of the LHCb collaboration)

QWG 2022

30 Sep 2022, GSI Darmstadt



Charmonium(-like) spectroscopy

- Rich structures

- Conventional $c\bar{c}$ states

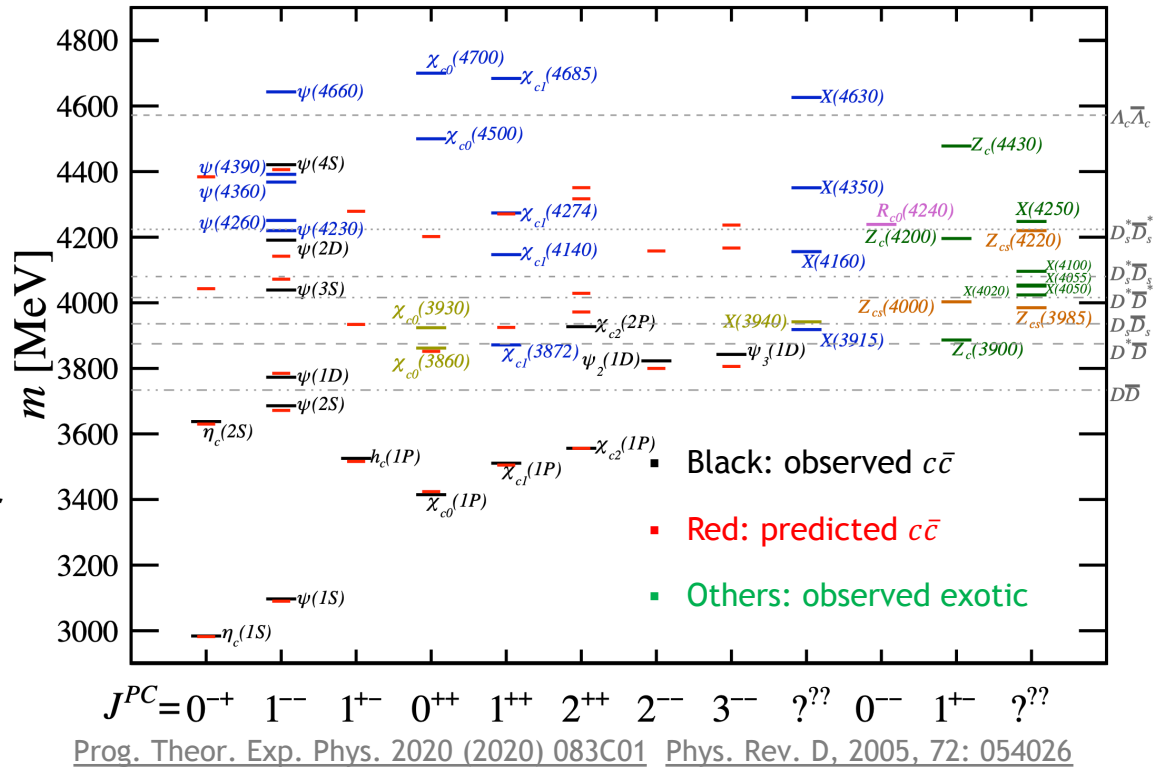
- Predominantly decay into $D^{(*)}\bar{D}^{(*)}$ if mass above threshold

- OZI allowed

- Exotic candidates

- May have large fraction for $c\bar{c} + h/\gamma$ decay process

- OZI suppressed for conventional states



- Puzzles to resolve by theorists and experimentists

- Identification of conventional/exotic nature of some states
 - Inner structure of exotic candidates

- More new particles may rise in experiment

- Open charm: $D^{(*)}\bar{D}^{(*)}$, $D_s^{(*)}\bar{D}_s^{(*)}$, ...
 - Hidden charm: $c\bar{c} + h/\gamma$

Topics in this talk

- Charmonium(-like) states in B decays

- A near-threshold $D_s^+ D_s^-$ structure in $B^+ \rightarrow D_s^+ D_s^- K^+$

LHCb-PAPER-2022-018

LHCb-PAPER-2022-019

In preparation

- Study of $J/\psi\eta$ resonances in $B^+ \rightarrow J/\psi\eta K^+$

J. High Energ. Phys. 2022, 46 (2022)

LHCb experiment

- Dedicated for precise and efficient heavy-hadron reconstruction

- Single-arm and forward design

- Powerful particle identification

- $\epsilon(K \rightarrow K) \sim 95\%$ with $\epsilon(\pi \rightarrow K) \sim 5\%$
 - $\epsilon(\mu \rightarrow \mu) \sim 97\%$ with $\epsilon(\pi \rightarrow \mu) \sim 1 - 3\%$

- High momentum resolution

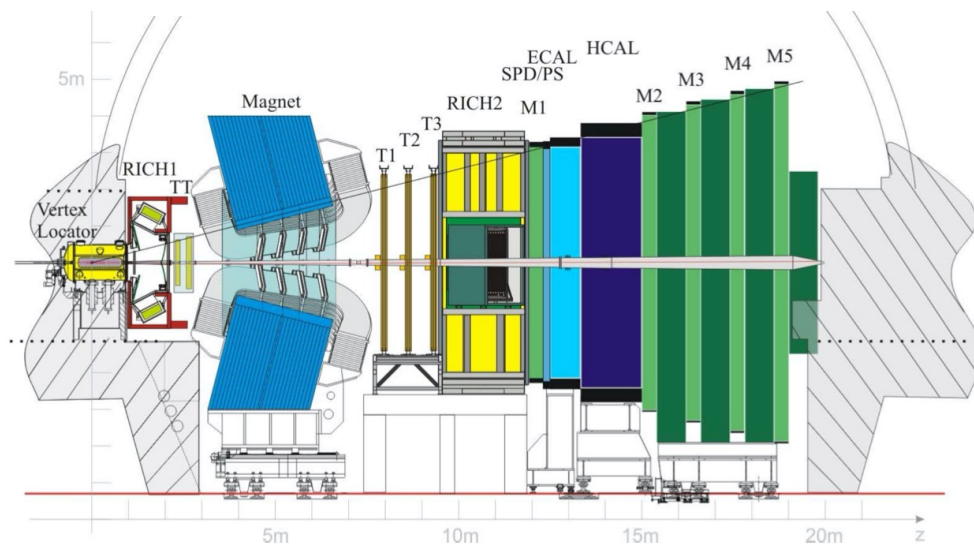
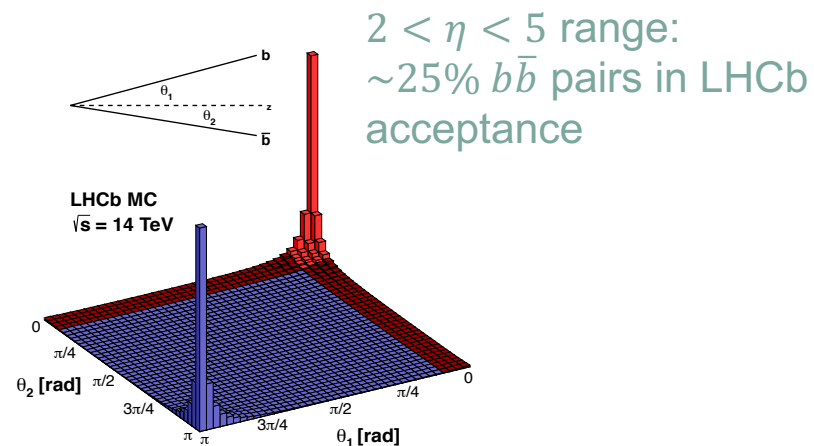
- $\Delta p/p = 0.4 \sim 0.6\%$ (5 – 100 GeV/c)
 - $\sigma_{m_B} \sim 10 \text{ MeV}$ for $B \rightarrow D\bar{D}K$ (m_D constrained)

- High spatial resolution

- $\sigma_{IP} \sim 20 \mu\text{m}$; $\sigma_{PV,x/y} \sim 10 \mu\text{m}$; $\sigma_{PV,z} \sim 60 \mu\text{m}$

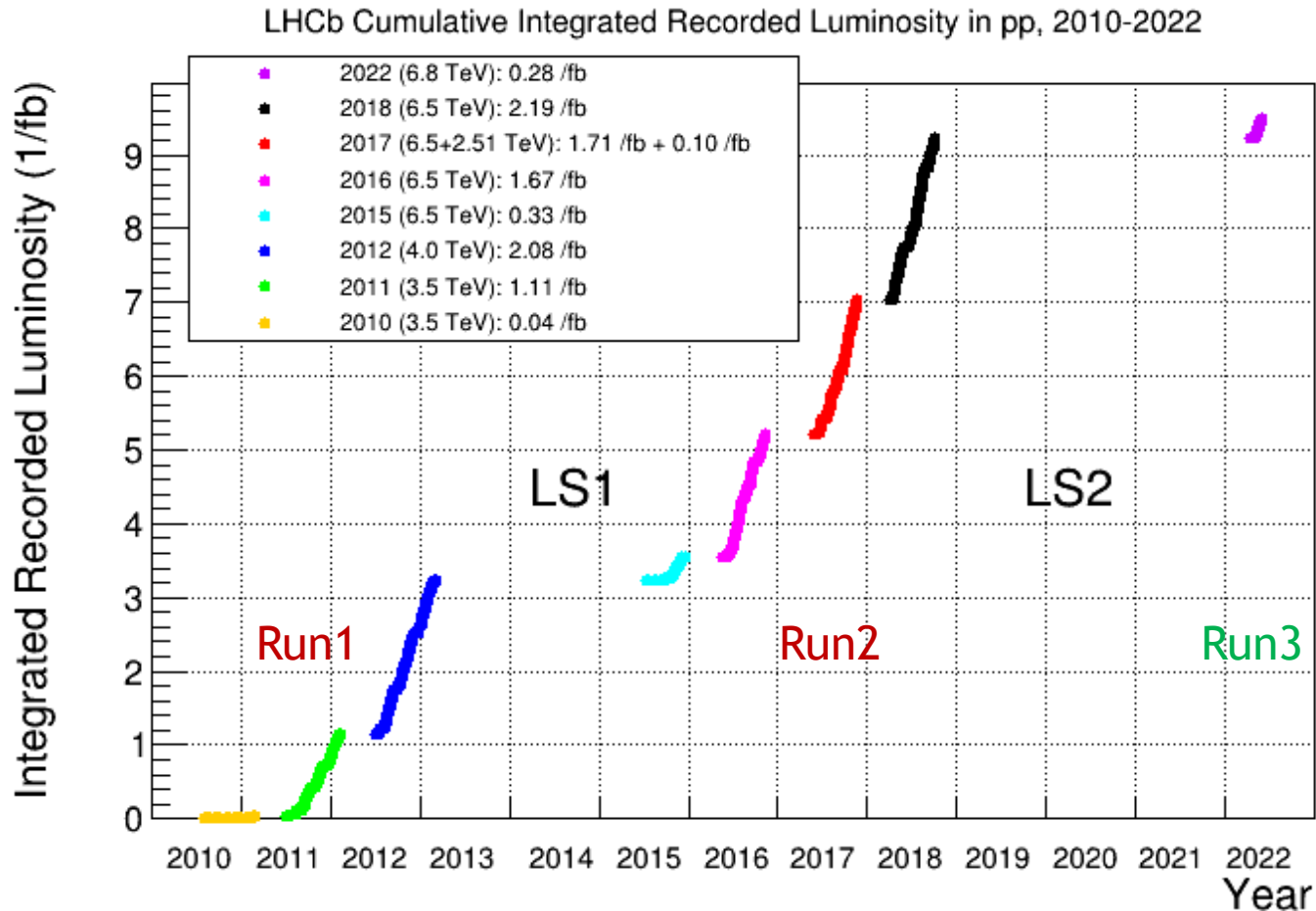
Ideal platform for studies of B decays presented in this talk

- ✓ High efficiency
- ✓ High resolution
- ✓ Low background



LHCb dataset

- Run1: 3 fb^{-1} pp collision @ 7, 8 TeV
- Run2: 6 fb^{-1} pp collision @ 13 TeV
- Run3: ongoing from 2022



A near-threshold $D_s^+ D_s^-$ structure in $B^+ \rightarrow D_s^+ D_s^- K^+$

LHCb-PAPER-2022-018

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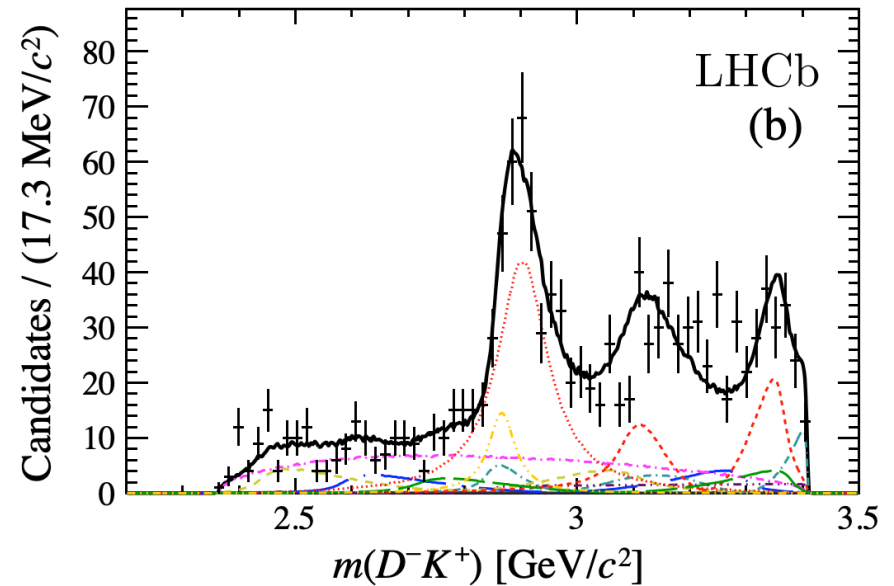
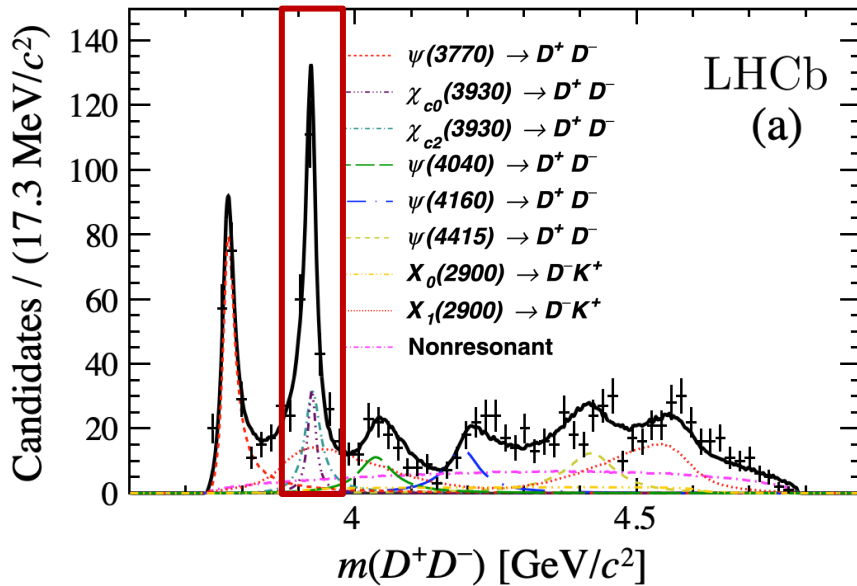
In preparation



What motivates this study?

$$B^+ \rightarrow D^+ D^- K^+$$

Phys.Rev.D102(2020) 112003, Phys. Rev. Lett. 125 (2020) 242001



▪ $\chi_{c0}(3930) \rightarrow D^+ D^-$:

- It is suggested to be the same particle as $\chi_{c0}(3915) \rightarrow J/\psi \omega$ [PDG 2020](#)
 - Exotic nature?

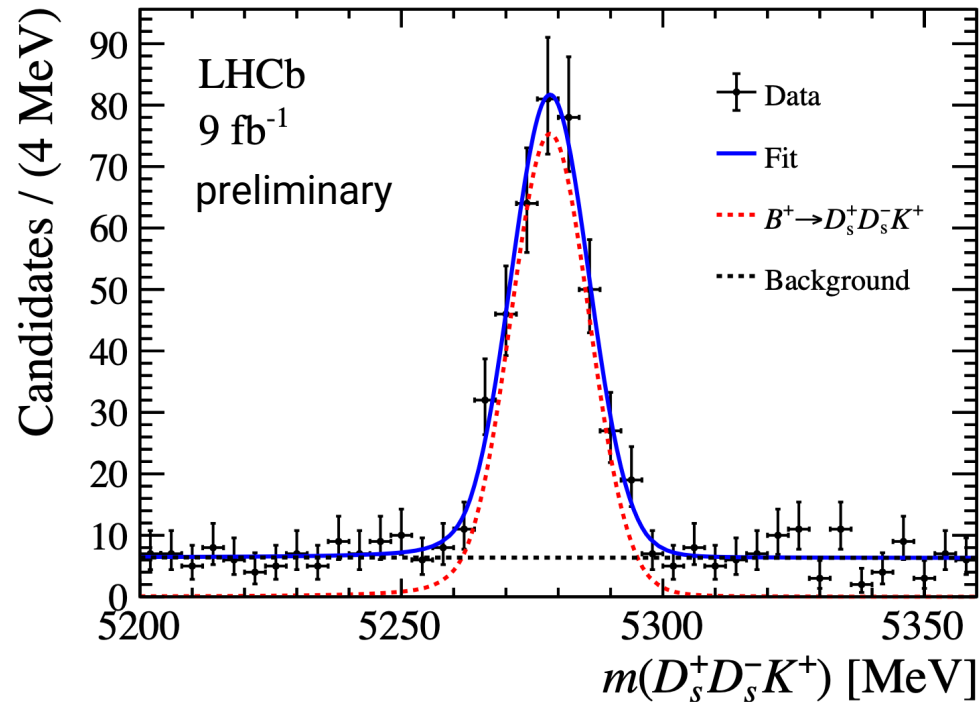
- Some theories suggest $\chi_{c0}(3930)/\chi_{c0}(3915)$ to be a $c\bar{c}s\bar{s}$ tetraquark candidate

To search for $\chi_{c0}(3930) \rightarrow D_s^+ D_s^-$ in $B^+ \rightarrow D_s^+ D_s^- K^+$

[JHEP 06 \(2021\) 035](#)
[Sci. Bull., 2021, 66: 1413](#)

$B^+ \rightarrow D_s^+ D_s^- K^+$ dataset

- **Dataset:** full Run1 + Run2 data, $\mathcal{L} = 9 \text{ fb}^{-1}$
- **Reconstruction:** $B^+ \rightarrow D_s^+ D_s^- K^+$, $D_s^\pm \rightarrow K^\mp K^\pm \pi^\pm$

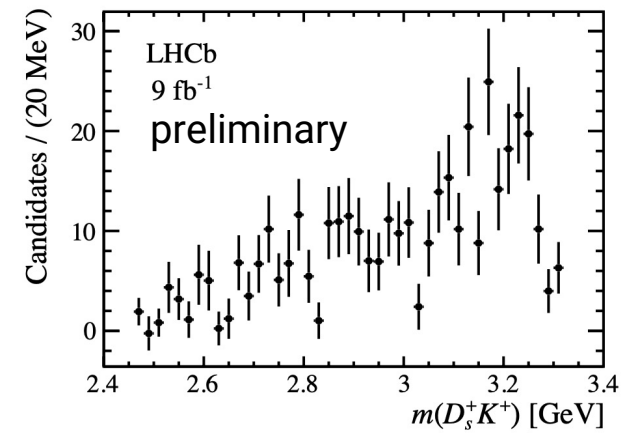
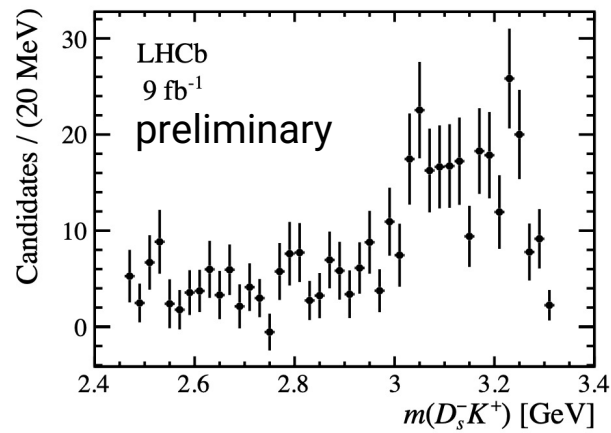
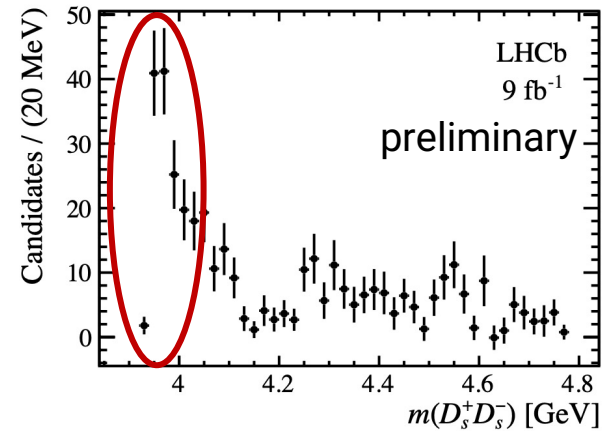
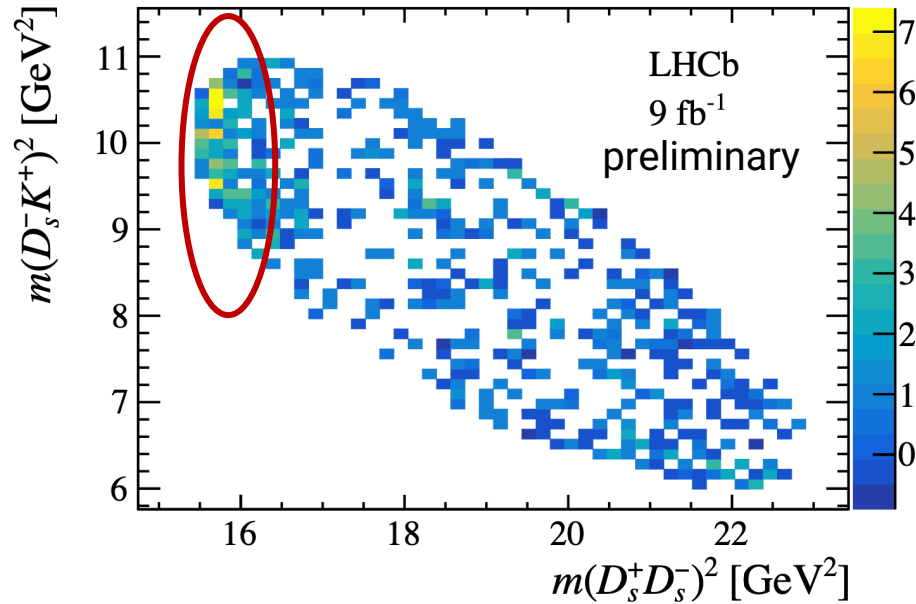


$$N_{sig} = 360 \pm 22$$

Purity: 84%

Near-threshold structure in $D_s^+ D_s^-$

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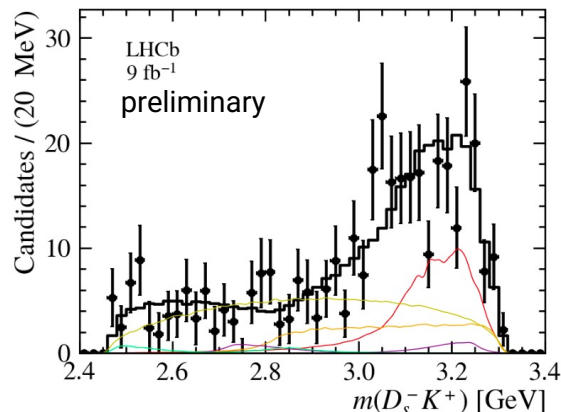
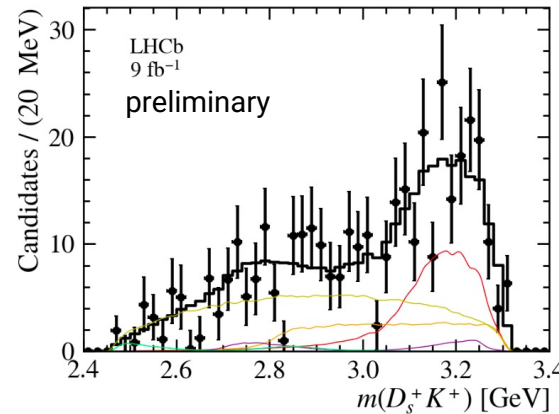
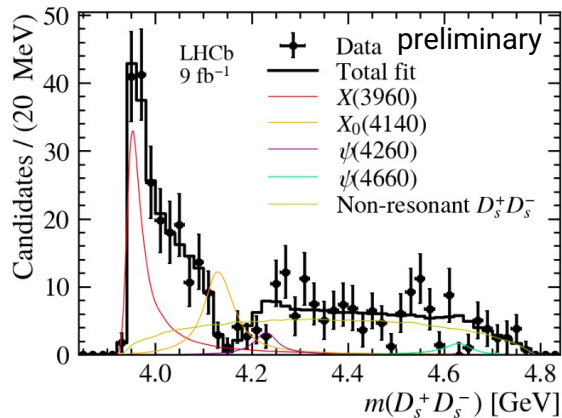
Background subtracted

Observation of $X(3960)$ in $D_s^+ D_s^-$

LHCb-PAPER-2022-018
LHCb-PAPER-2022-019

- Amplitude analysis
- Default model
 - 0^{++} : $X(3960)$, $X_0(4140)$, non-resonant (NR)
 - 1^{--} : $\psi(4260)$, $\psi(4660)$

$\psi(4260)$ is $\psi(4230)$ in PDG2022



- ✓ $X(3960)$ describes the near-threshold peak
- ✓ $X_0(4140)$ accounts for the dip at ~ 4.14 GeV via interference

Background subtracted

Amplitude fit result

LHCb-PAPER-2022-018

LHCb-PAPER-2022-019

Component	J^{PC}	M_0 (MeV)	Γ_0 (MeV)	\mathcal{F} (%)	\mathcal{S} (σ)
$X(3960)$	0^{++}	$3956 \pm 5 \pm 10$	$43 \pm 13 \pm 8$	$25.4 \pm 7.7 \pm 5.0$	12.6 (14.6)
$X_0(4140)$	0^{++}	$4133 \pm 6 \pm 6$	$67 \pm 17 \pm 7$	$16.7 \pm 4.7 \pm 3.9$	3.8 (4.1)
$\psi(4260)$	1^{--}	4230 (fixed)	55 (fixed)	$3.6 \pm 0.4 \pm 3.2$	3.2 (3.6)
$\psi(4660)$	1^{--}	4633 (fixed)	64 (fixed)	$2.2 \pm 0.2 \pm 0.8$	3.0 (3.2)
NR	0^{++}	-	-	$46.1 \pm 13.2 \pm 11.3$	3.1 (3.4)

- First uncertainty statistical, and second systematic
- Fixed parameters taken from PDG 2018/2020 ($\psi(4260)$ is $\psi(4230)$ in PDG2022)

- \mathcal{F} : fit fraction
- \mathcal{S} : significance

(numbers in brackets don not include systematic effect)

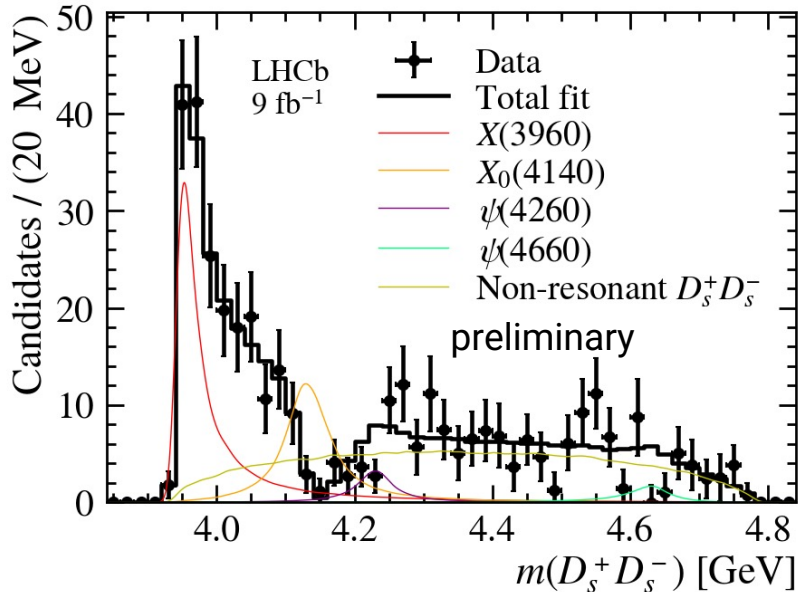
- **Spin-parity tests:**

- $X(3960)$: 0^{++} favored; 1^{--} and 2^{++} rejected by at least 9σ
- $X_0(4140)$: 0^{++} favored; 1^{--} and 2^{++} rejected by at least 3.5σ

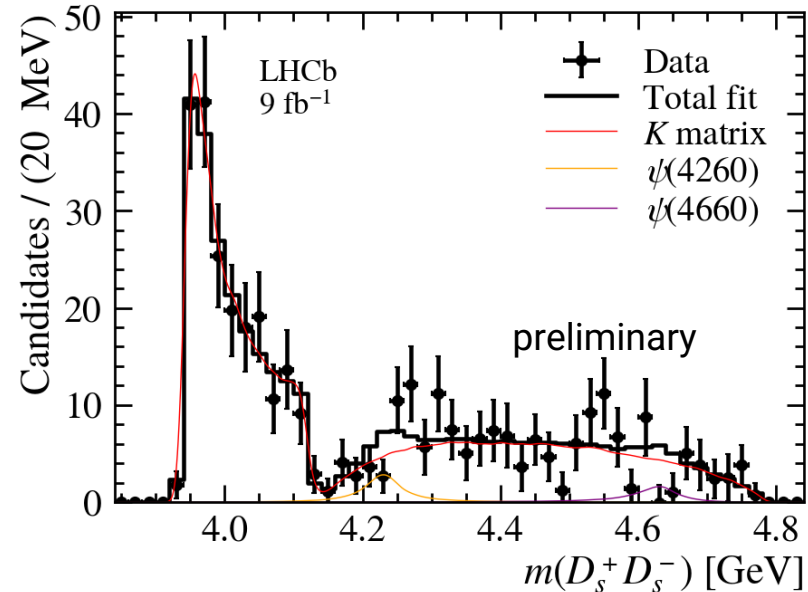
Alternative K -matrix model

- Dip around 4.14 GeV near the $J/\psi\phi$ threshold

Background subtracted



The default model:
modelled by a new
resonance, $X_0(4140)$



Can also be described by
considering $J/\psi\phi \rightarrow D_s^+ D_s^-$
rescattering in the K -matrix
formula

No definitive conclusion on existence of $X_0(4140)$

$X(3960)$ and $\chi_{c0}(3930)$

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LHCb-PAPER-2022-019

- $X(3960)$: $M_0 = 3955 \pm 6 \pm 11$ MeV; $\Gamma_0 = 48 \pm 17 \pm 10$ MeV; $J^{PC} = 0^{++}$
- $\chi_{c0}(3930)$: $M_0 = 3924 \pm 2$ MeV; $\Gamma_0 = 17 \pm 5$ MeV; $J^{PC} = 0^{++}$

Phys.Rev.D102(2020) 112003, Phys. Rev. Lett. 125 (2020) 242001

- Are they the same particle? If yes

$\mathcal{F}\mathcal{F}$: Fit fractions in the two B^+ decays

$$\frac{\Gamma(X \rightarrow D^+ D^-)}{\Gamma(X \rightarrow D_s^+ D_s^-)} = \frac{\mathcal{B}(B^+ \rightarrow D^+ D^- K^+) \mathcal{F}\mathcal{F}_{B^+ \rightarrow D^+ D^- K^+}^X}{\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+) \mathcal{F}\mathcal{F}_{B^+ \rightarrow D_s^+ D_s^- K^+}^X}$$
$$= 0.29 \pm 0.09 \text{ (stat)} \pm 0.10 \text{ (syst)} \pm 0.08 \text{ (ext)}$$

$\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+)$ also measured in this work

- $\Gamma(X \rightarrow D^+ D^-) < \Gamma(X \rightarrow D_s^+ D_s^-)$ implies the exotic nature of the state
 - Conventional charmonium predominantly decays into $D^{(*)} \bar{D}^{(*)}$
 - It is harder to excite an $s\bar{s}$ pair from vacuum compared with $u\bar{u}(d\bar{d})$

Summary on $X(3960) \rightarrow D_s^+ D_s^-$

LHCb-PAPER-2022-018

LHCb-PAPER-2022-019

- Observation of near-threshold structure $X(3960)$ in $B^+ \rightarrow$

$$D_s^+ D_s^- K^+ > 12\sigma$$

$$M_0 = 3955 \pm 6 \pm 11 \text{ MeV}; \Gamma_0 = 48 \pm 17 \pm 10 \text{ MeV}; J^{PC} = 0^{++}$$

- Assuming $X(3960)$ and $\chi_{c0}(3930)$ to be the same particle

$$\frac{\Gamma(X \rightarrow D^+ D^-)}{\Gamma(X \rightarrow D_s^+ D_s^-)} = 0.29 \pm 0.09 \pm 0.10 \pm 0.08$$

Indicating the exotic nature

Then it should be called $T_{\psi\phi_0}^f(39xx)$ following the new exotic naming scheme

[arXiv:2206.15233](https://arxiv.org/abs/2206.15233) & [Tim's talk](#)

- Future studies

- Precision measurements of $X(3960)$ and $\chi_{c0}(3930)$ properties -> to see if they are really the same particle
- $X(3960)/\chi_{c0}(3930)/\chi_{c0}(3915) \rightarrow J/\psi\omega$ -> more input to help reveal the nature of this state

Study of $J/\psi\eta$ resonances in $B^+ \rightarrow J/\psi\eta K^+$

J. High Energ. Phys. 2022, 46 (2022)



What motivates this study?

- Study charmonium(-like) states in $J/\psi\eta$

- X'_C : C-odd partner of $\chi_{c1}(3872)$

- Predicted by many theoretical works

[JPS Conf. Proc. 13 (2017) 020023, EPJ Web Conf. 137 (2017) 06002, ...]

- Searched for by Belle and BaBar

BaBar $\mathcal{B}(B^+ \rightarrow X'_C K^+) \times \mathcal{B}(X'_C \rightarrow J/\psi\eta) < 7.7 \times 10^{-6}$

Phys. Rev. Lett. 93 (2004) 041801

Belle $\mathcal{B}(B^+ \rightarrow X'_C K^+) \times \mathcal{B}(X'_C \rightarrow J/\psi\eta) < 3.8 \times 10^{-6}$

PTEP 2014 (2014) 043C01

- Other charmonium(-like) states

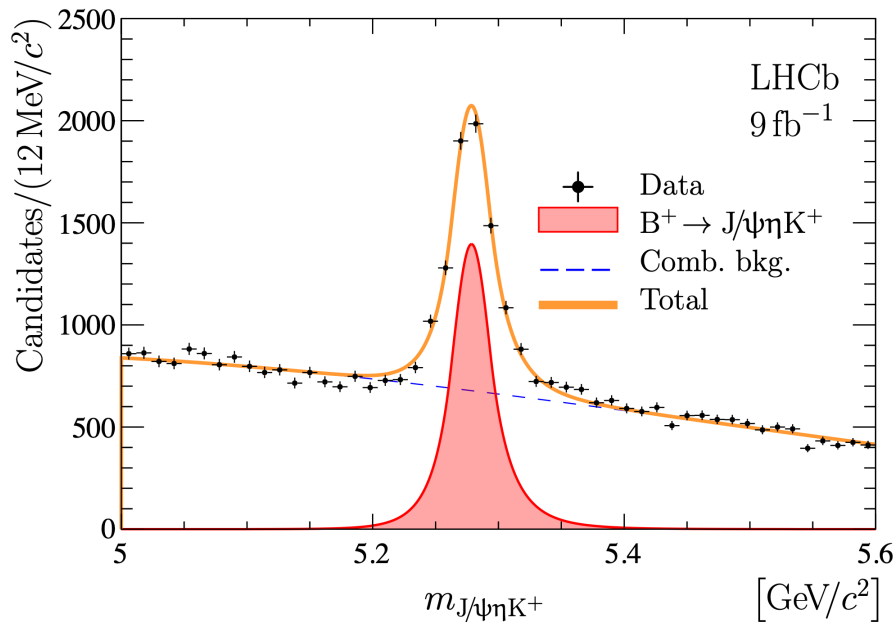
- $\psi_2(3823)$, $\psi(4040)$, etc

$B^+ \rightarrow J/\psi\eta K^+$ dataset

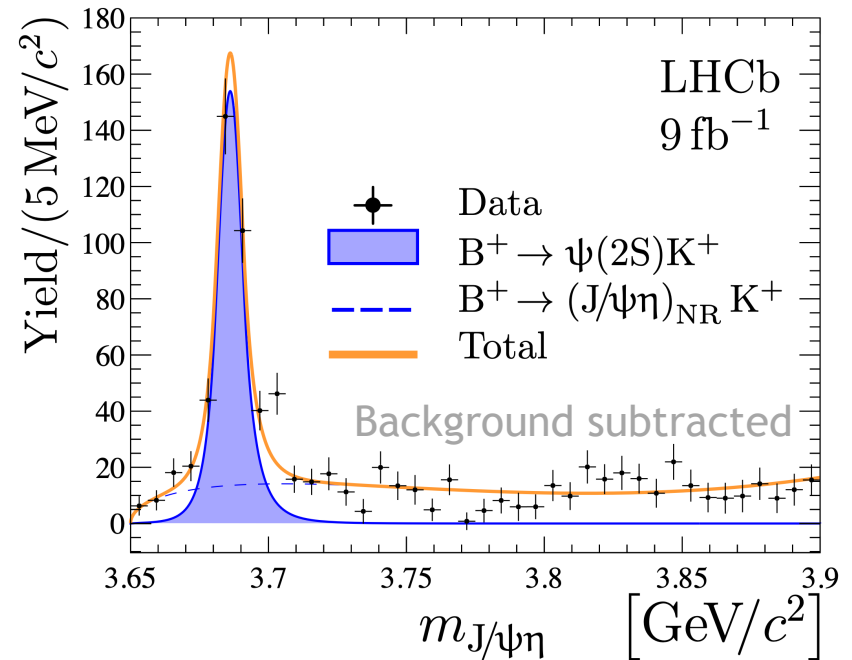
J. High Energ. Phys. 2022, 46 (2022)

- Full Run1 + Run2 data, $\mathcal{L} = 9 \text{ fb}^{-1}$
- $B^+ \rightarrow J/\psi\eta K^+, J/\psi \rightarrow \mu^+\mu^-, \eta \rightarrow \gamma\gamma$

$$N_{B^+}: (5.39 \pm 0.16) \times 10^3$$



Clear signature of $\psi(2S) \rightarrow J/\psi\eta$



Normalization for the fractions of other $J/\psi\eta$ states in the next slide

Resonances in the $J/\psi\eta$ system

J. High Energ. Phys. 2022, 46 (2022)

$$F_X \equiv \frac{\mathcal{B}(B^+ \rightarrow XK^+) \times \mathcal{B}(X \rightarrow J/\psi\eta)}{\mathcal{B}(B^+ \rightarrow \psi(2S)K^+) \times \mathcal{B}(\psi(2S) \rightarrow J/\psi\eta)}$$

- Evidence for $\psi_2(3823)$, $\psi(4040) \rightarrow J/\psi\eta$

First evidence $F_{\psi_2(3823)} = (5.95^{+3.38}_{-2.55}) \times 10^{-2} \quad 3.4\sigma$

$F_{\psi(4040)} = (40.6 \pm 11.2) \times 10^{-2} \quad 4.7\sigma$

Systematic uncertainty included

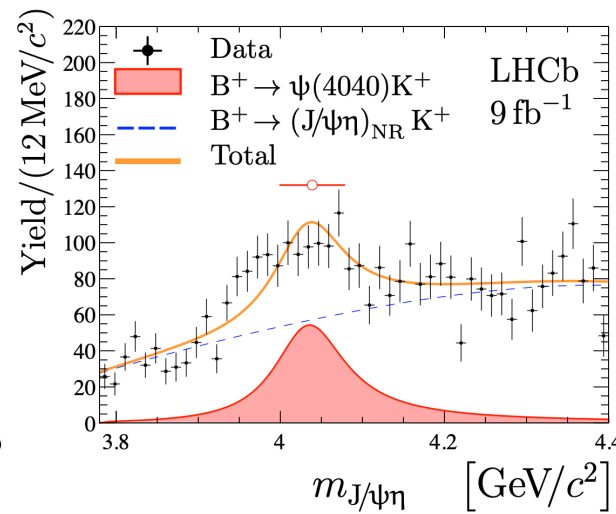
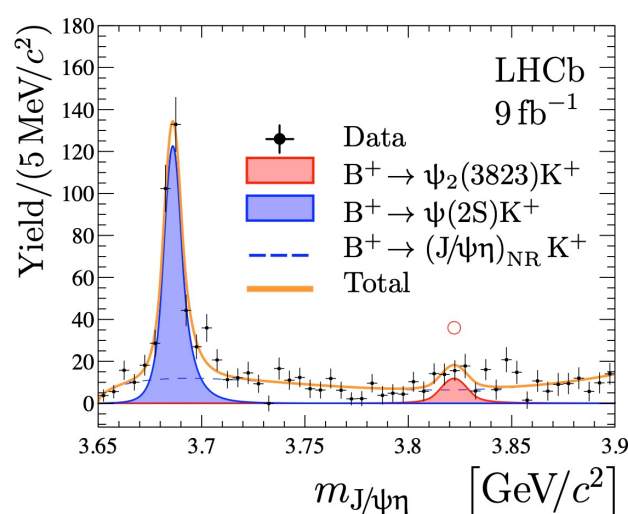
- Upper limit for other states

	Upper limit on 90% CL $F_X [10^{-2}]$	$B_X [10^{-7}]$
--	--	-----------------

$\psi(3770)$	2.2	4.6
$\psi_3(3842)$	2.9	6.1
$\psi(4160)$	4.2	8.7
$\psi(4415)$	4.6	9.6
R(3760)	2.0	4.1
R(3790)	3.2	6.7
$Z_c(3900)^0$	2.1	4.3
$\psi(4230)$	1.9	3.9
$\psi(4360)$	6.0	12.4
$\psi(4390)$	11.6	24.1
$Z_c(4430)^0$	6.1	12.7
X'_C	1.9	3.9

Upper limit is an order of magnitude smaller than the Belle and BaBar results

Phys. Rev. Lett. 93 (2004) 041801
PTEP 2014 (2014) 043C01



Background subtracted

Discussions on $\psi_2(3823)$ and $\psi(4040)$

[J. High Energ. Phys. 2022, 46 \(2022\)](#)

▪ $\psi_2(3823)$:

$$\frac{\mathcal{B}(\psi_2(3823) \rightarrow J/\psi\eta)}{\mathcal{B}(\psi_2(3823) \rightarrow J/\psi\pi^+\pi^-)} = 4.4^{+2.5}_{-1.9} \pm 0.9$$

- Inconsistent with the theoretical study

[Phys. Rev. D94 \(2016\) 034005](#)

▪ $\psi(4040)$:

$$\mathcal{B}(B^+ \rightarrow \psi(4040)K^+) = (1.64 \pm 0.45 \pm 0.23) \times 10^{-3} \quad \text{This work}$$

- Inconsistent with the upper limit set using $\psi(4040) \rightarrow \mu^+\mu^-$

[Phys. Rev. Lett. 111 \(2013\) 112003](#)

- $\psi(4040)$ and $\psi(4160)$ production rates are different in several modes

- $\psi(4040) \sim \psi(4160)$ in $B^+ \rightarrow D^+D^-K^+$

[Phys. Rev. D102 \(2020\) 112003](#)

- $\psi(4040) < \psi(4160)$ in $B^+ \rightarrow \mu^+\mu^-K^+$

[Phys. Rev. Lett. 111 \(2013\) 112003](#)

- $\psi(4040) > \psi(4160)$ in $B^+ \rightarrow J/\psi\eta K^+$ (this work)

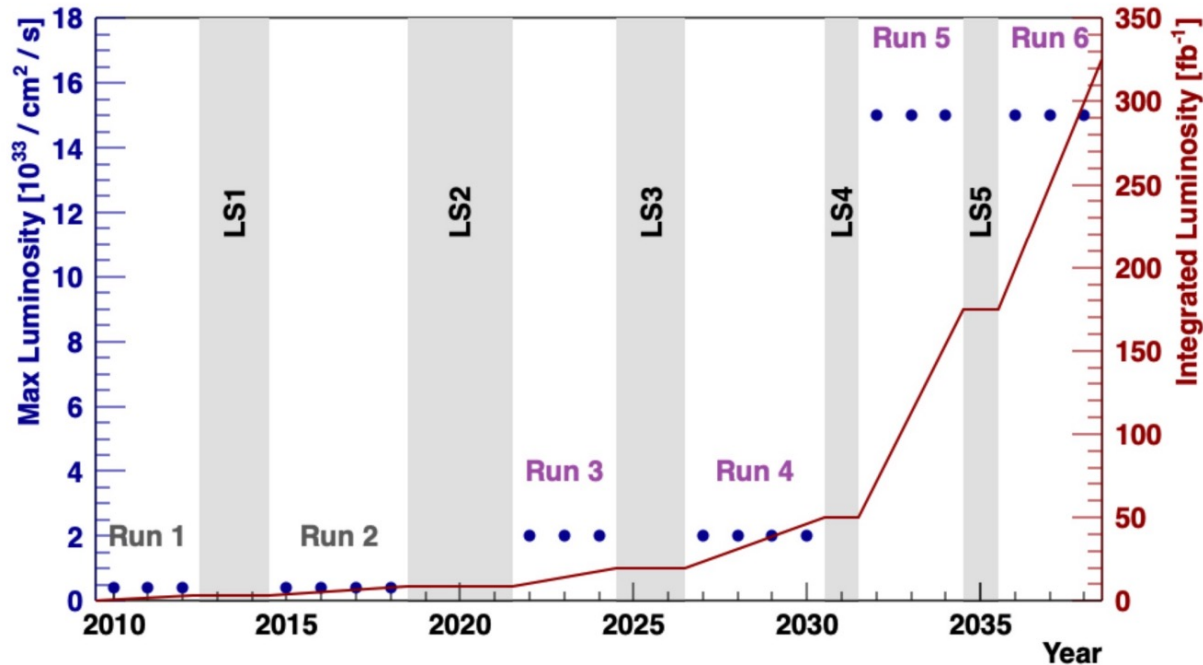
Future studies to resolve these puzzles

Summary

- Recent results on charmonium(-like) spectroscopy at LHCb
 - Observation of near-threshold structure $X(3960)$ in $B^+ \rightarrow D_s^+ D_s^- K^+$
 - An interesting exotic candidate
Same state as $\chi_{c0}(3930)/\chi_{c0}(3915)$?
- Investigation of $J/\psi\eta$ system in $B^+ \rightarrow J/\psi\eta K^+$
 - Evidence for $\psi_2(3823), \psi(4040) \rightarrow J/\psi\eta$
 - Upper limits on branching fractions of some other charmonium(-like) states
e.g. C-odd partner of $\chi_{c1}(3872)$

Prospects

- We are now boosting our data to a new level



- Precision measurements on $X(3960)/\chi_{c0}(3930)$ properties
- More states in $B^+ \rightarrow J/\psi\eta K^+$ may rise
- Opportunities to investigate more $c\bar{c} + h$ and open charm final states
 - e.g. $J/\psi\omega$, $\Lambda_c^+\bar{\Lambda}_c^-$

Thank you for your attention!

Backup slides



Systematic uncertainties in $B^+ \rightarrow D_S^+ D_S^- K^+$ AmAn

LHCb-PAPER-2022-018

LHCb-PAPER-2022-019

Source	$X(3960)$			$X_0(4140)$			$\psi(4260)$	$\psi(4660)$	NR
	M_0	Γ_0	\mathcal{F}	M_0	Γ_0	\mathcal{F}	\mathcal{F}	\mathcal{F}	\mathcal{F}
Trigger	0	0	0.6	0	0	0.1	0.0	0.0	0.7
Simulation statistics	2	1	0.7	1	1	0.5	0.0	0.0	1.7
Particle identification	0	0	0.5	0	2	0.0	0.0	0.0	0.7
Additional components	1	3	3.4	3	5	2.5	3.2	0.7	10.1
Hadron size	0	1	0.0	1	1	0.1	0.0	0.0	0.1
Fixed parameters	1	2	2.8	4	4	2.9	0.1	0.1	3.7
$X(3960)$ model	10	7	1.6	0	1	0.7	0.0	0.0	2.1
<i>sFit</i> bias	1.9	1.5	1.5	2.6	1.1	0.4	0.3	0.3	2.1
Total	10	8	5.0	6	7	3.9	3.2	0.8	11.3

K-matrix model for $X(3960)$

LHCb-PAPER-2022-018
LHCb-PAPER-2022-019

$$\begin{pmatrix} \mathcal{M}_{D_s^+ D_s^- \rightarrow D_s^+ D_s^-} & \mathcal{M}_{D_s^+ D_s^- \rightarrow J/\psi \phi} \\ \mathcal{M}_{J/\psi \phi \rightarrow D_s^+ D_s^-} & \mathcal{M}_{J/\psi \phi \rightarrow J/\psi \phi} \end{pmatrix} \equiv \begin{pmatrix} \mathcal{K}_{11} & \mathcal{K}_{12} \\ \mathcal{K}_{21} & \mathcal{K}_{22} \end{pmatrix}$$

$$\mathcal{K}_{ab}(m) = \sum_R \frac{g_b^R g_a^R}{M_R^2 - m^2} + f_{ab}$$

$$\mathcal{P}_b(m) = \sum_R \frac{\beta_R g_b^R}{M_R^2 - m^2} + \beta_b$$

$$\mathcal{M}_a = \sum_b (I - i\rho\mathcal{K})_{ab}^{-1} \mathcal{P}_b$$

Contribution	J^{PC}	M_R (MeV)	g_1^R (MeV)	Γ_ψ (MeV)	\mathcal{F} (%)
$ \mathcal{M}_1 ^2$	0^{++}	3957 ± 14	1350 ± 344		94.7 ± 0.4
$\psi(4260)$	1^{--}	4230 [59]		55 [59]	3.2 ± 0.5
$\psi(4660)$	1^{--}	4633 [31]		64 [31]	2.1 ± 0.2
β_R		$(1, 0i)$	β_1	$(-1.2, 2.5i) \pm (4.5, 3.1i)$	
β_2		$(-137.2, -1.5i) \pm (2.7, 218.6i)$	f_{11}	0.8 ± 1.2	
$f_{12} = f_{21}$		0.1 ± 0.1	f_{22}	8.0 ± 5.1	

Large
uncertainties.
Larger data
sample is
needed

K-matrix model for $X(3960)$

LHCb-PAPER-2022-018
LHCb-PAPER-2022-019

$$\begin{pmatrix} \mathcal{M}_{D_s^+ D_s^- \rightarrow D_s^+ D_s^-} & \mathcal{M}_{D_s^+ D_s^- \rightarrow J/\psi \phi} \\ \mathcal{M}_{J/\psi \phi \rightarrow D_s^+ D_s^-} & \mathcal{M}_{J/\psi \phi \rightarrow J/\psi \phi} \end{pmatrix} \equiv \begin{pmatrix} \mathcal{K}_{11} & \mathcal{K}_{12} \\ \mathcal{K}_{21} & \mathcal{K}_{22} \end{pmatrix}$$

$$\mathcal{K}_{ab}(m) = \sum_R \frac{g_b^R g_a^R}{M_R^2 - m^2} + f_{ab}$$

$$\mathcal{P}_b(m) = \sum_R \frac{\beta_R g_b^R}{M_R^2 - m^2} + \beta_b$$

$$\mathcal{M}_a = \sum_b (I - i\rho\mathcal{K})_{ab}^{-1} \mathcal{P}_b$$

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$f_{12} = f_{21}$		0.1 ± 0.1	f_{22}	8.0 ± 5.1	

Large
uncertainties.
Larger data
sample is
needed

$\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+)$

- Essential input to calculate the width fraction

$$\frac{\Gamma(X \rightarrow D^+ D^-)}{\Gamma(X \rightarrow D_s^+ D_s^-)} = \frac{\mathcal{B}(B^+ \rightarrow D^+ D^- K^+) \mathcal{F}\mathcal{F}_{B^+ \rightarrow D^+ D^- K^+}^X}{\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+) \mathcal{F}\mathcal{F}_{B^+ \rightarrow D_s^+ D_s^- K^+}^X}$$

FF: Fit fraction

- Relative measurement

$$\mathcal{R} \equiv \frac{\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+)}{\mathcal{B}(B^+ \rightarrow D^+ D^- K^+)} = \frac{N_{\text{sig}}^{\text{corr}}}{N_{\text{con}}^{\text{corr}}} \left[\frac{\mathcal{B}(D^+ \rightarrow K^- \pi^+ \pi^+)}{\mathcal{B}(D_s^+ \rightarrow K^- K^+ \pi^+)} \right]^2$$

Know quantities from PDG

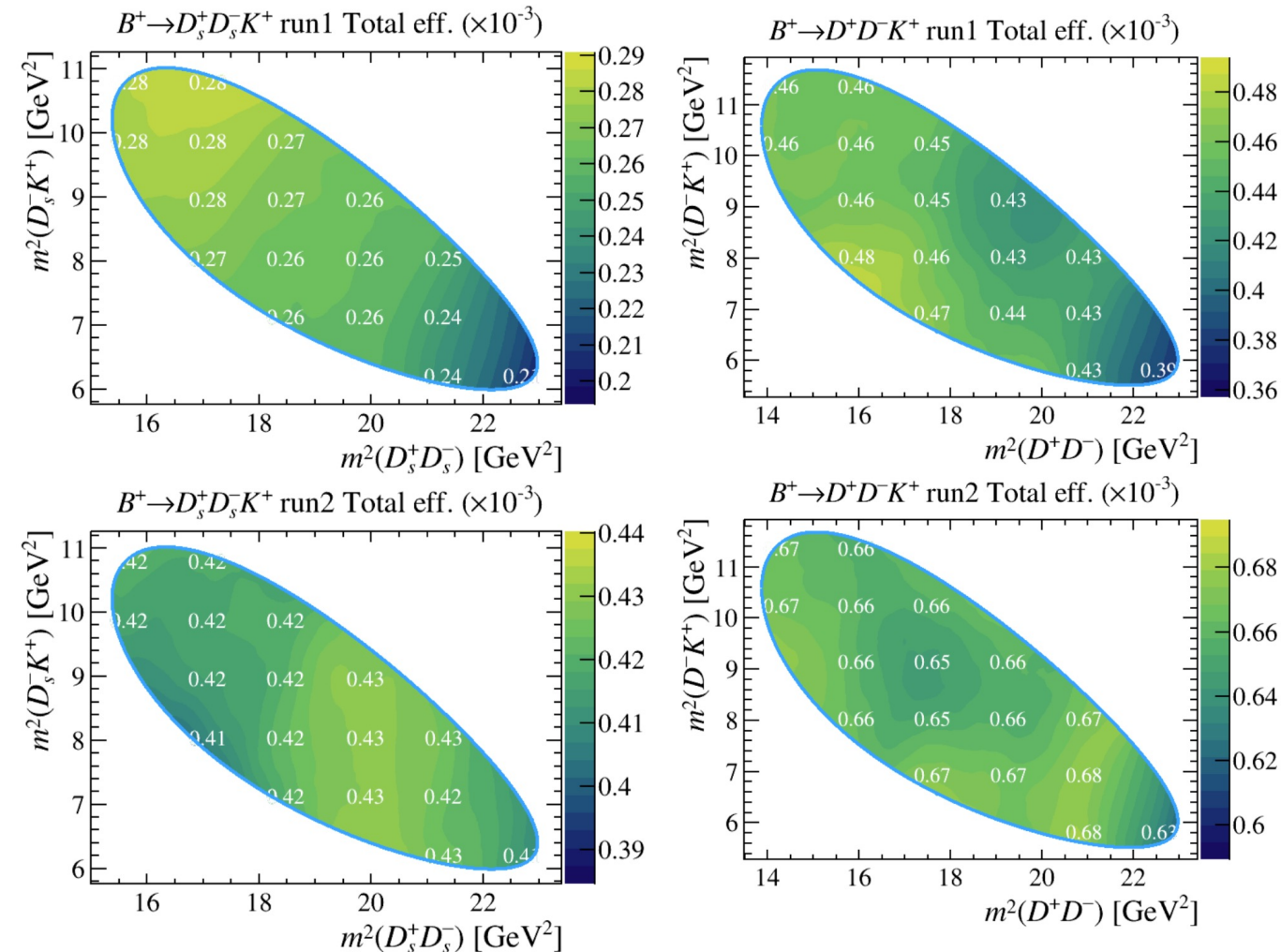
- $w_{\text{sig}}, w_{\text{con}}$: sWeights determined from B^+ mass fits to extract the signal components
- $\epsilon_{\text{sig}}, \epsilon_{\text{con}}$: efficiency obtained from MC simulation

$$N_{\text{sig}}^{\text{corr}} = \sum_i \frac{w_{\text{sig},i}}{\epsilon_{\text{sig},i}(m^2(D_s^+ D_s^-), m^2(D_s^- K^+))}$$

$$N_{\text{con}}^{\text{corr}} = \sum_i \frac{w_{\text{con},i}}{\epsilon_{\text{con},i}(m^2(D^+ D^-), m^2(D^- K^+))}$$

Efficiency

- **Denominator:** Generator-level MC sample without any cut
- **Numerator:** Fully reconstructed MC sample after all the selection



Kernel density estimation is employed to obtain the smooth efficiency functions

Branching fraction result

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$$\mathcal{R} = \frac{\mathcal{B}(B^+ \rightarrow D_s^+ D_s^- K^+)}{\mathcal{B}(B^+ \rightarrow D^+ D^- K^+)} = 0.525 \pm 0.033 \pm 0.027 \pm 0.034.$$

1. Stat.
2. Syst.
3. External

Systematic source	Relative uncertainty (%)
L0 trigger correction	2.3
Signal model variation	0.3
Background model variation	0.1
B^+ mass fit bias	0.1
Limited size of MC samples	0.5
KDE parameters	0.4
Charmless and single-charm background	2.9
PID resampling	2.8
BDT working point	1.6
Tracking efficiency	1.0
Multiple candidate removal	0.7
MC truth match efficiency	0.6
Total syst. (stat.)	5.1 (6.3)

Full $J/\psi\eta$ mass range

